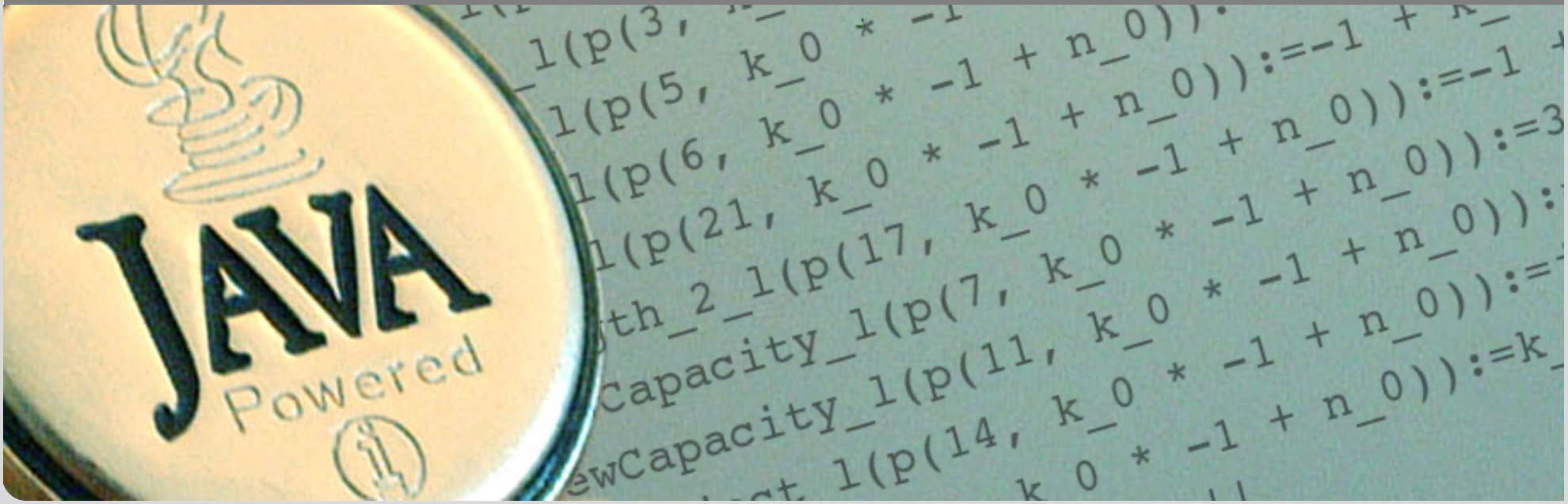
Applications of Formal Verification

Model Checking: Introduction to SPIN

Bernhard Beckert · Mattias Ulbrich | SS 2017

KIT – INSTITUT FÜR THEORETISCHE INFORMATIK



SPIN: Previous Lecture vs. This Lecture

Previous lecture

SPIN appeared as a PROMELA *simulator*

This lecture

Intro to SPIN as a *model checker*

What Does A Model Checker Do?

A Model Checker (MC) is designed to prove the user wrong.

MC tries its best to *find a counter example* to the correctness properties.
It is tuned for that.

MC does not try to prove correctness properties.
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But why then can a MC also *prove* correctness properties?

MC's *search* for counter examples is *exhaustive*.

$\Rightarrow$ *Finding no counter example proves stated correctness properties.*

What does ‘exhaustive search’ mean here?

exhaustive search
=
resolving non-determinism in all possible ways

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For model checking PROMELA code,
two kinds of non-determinism to be resolved:

- *explicit, local*:
  `if`/**`do`** statements

```
:: guardX -> ....
:: guardY -> ....
```

- *implicit, global*:
  scheduling of concurrent processes
  (see next lecture)

Model Checker for This Course: SPIN

SPIN: "*S*imple *P*romela *In*terpreter"

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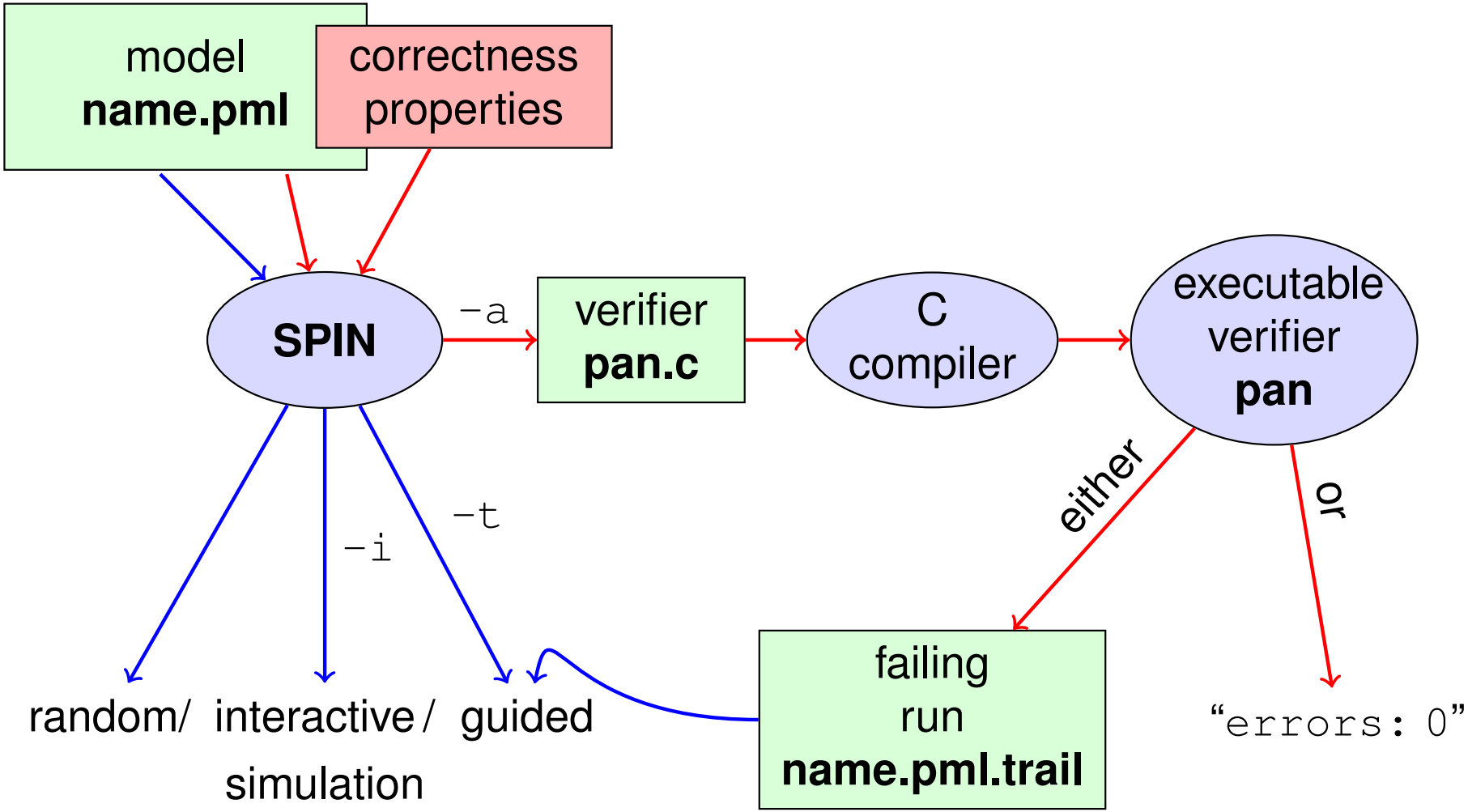
- simulating a model (randomly/interactively/guided)
- generating a *verifier*

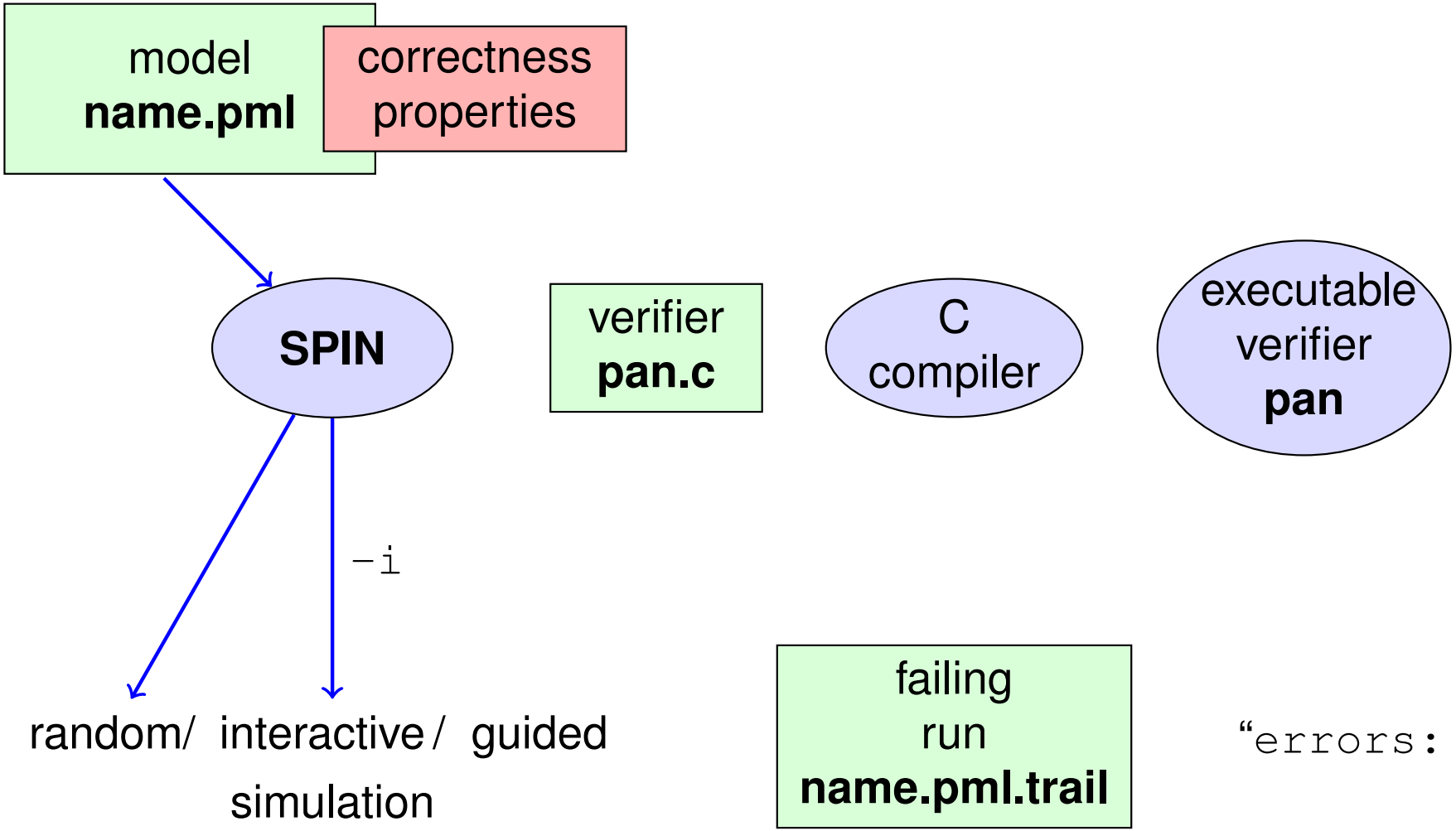
verifier generated by SPIN is a C program performing *model checking*:

- exhaustively *checks* PROMELA *model* against correctness properties
- in case the check is negative:
  generates a failing run of the model, to be simulated by SPIN

SPIN Workflow: Overview



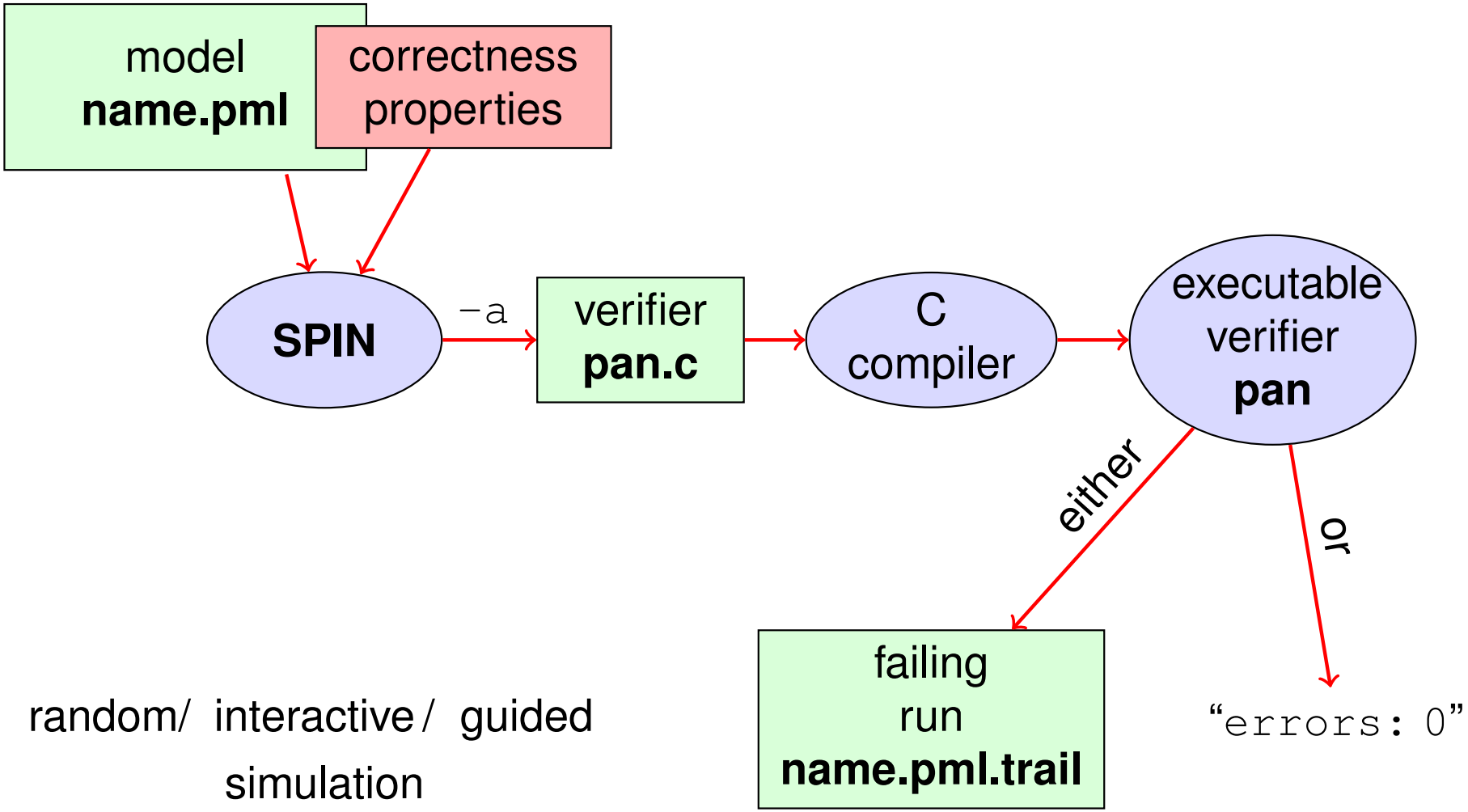
Plain Simulation with SPIN



Rehearsal: Simulation Demo

- run example, random and interactive
  `interleave.pml`, `zero.pml`

Model Checking with SPIN



random/ interactive / guided
simulation

Meaning of Correctness wrt. Properties

Given PROMELA model M, and correctness properties $C_1, \ldots, C_n$.

- Be R_M the set of all possible runs of M.
- For each correctness property C_i,
  R_{M,C_i} is the set of all runs of M satisfying C_i.
  $(R_{M,C_i} \subseteq R_M)$
- M is correct wrt. $C_1, \ldots, C_n$ iff $(R_{M,C_1} \cap \ldots \cap R_{M,C_n}) = R_M$.
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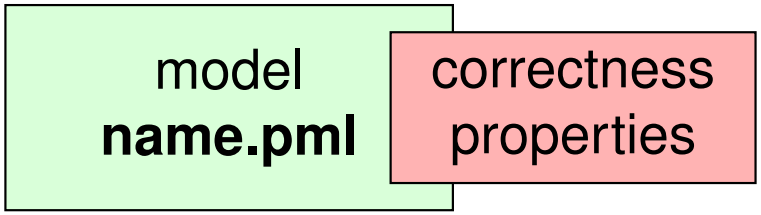
We know how to write models M.
But how to write Correctness Properties?

Stating Correctness Properties



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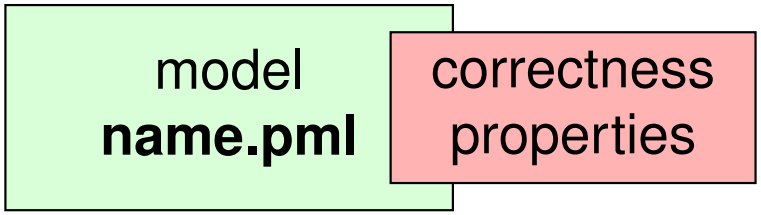

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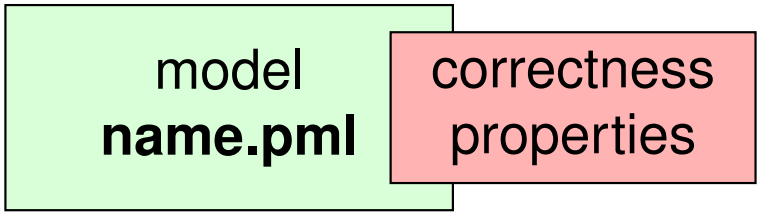

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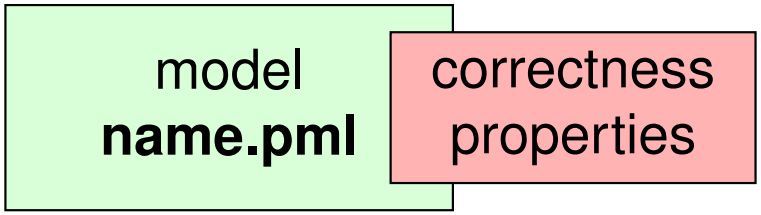

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  - `end` labels
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  - `progress` labels

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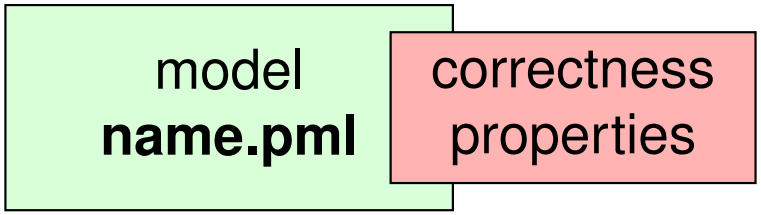

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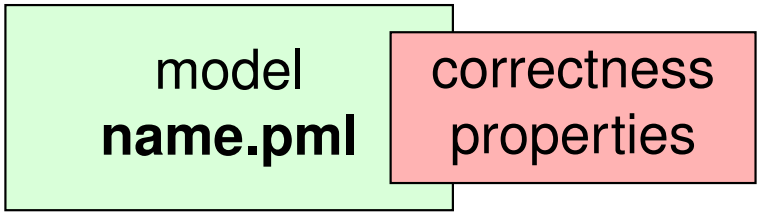
stating properties outside the model, using

- never claims
- temporal logic formulas

Stating Correctness Properties



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- *assertion statements* (today)
- meta labels
  - `end` *labels* (today)
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Assertion Statements

Definition (Assertion Statements)

Assertion statements in PROMELA are statements of the form

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...
stmt1;
assert(max == a);
stmt2;
...
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```
...
stmt1;
assert(max == a);
stmt2;
...
```

```
...
if
:: b1 -> stmt3;
         assert(x < y)
:: b2 -> stmt4
...
```

Meaning of Boolean Assertion Statements

`assert(`*expr*`)`

- has no effect if *expr* evaluates to true
- triggers an error message if *expr* evaluates to false

This holds in both, simulation and model checking mode.

Meaning of General Assertion Statements

`assert``(`*expr*`)`

- has no effect if *expr* evaluates to non-zero value
- triggers an error message if *expr* evaluates to 0

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Recall:

`bool true false` is syntactic sugar for

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Recall:

`bool`	**`true`**	**`false`**	is syntactic sugar for
`bit`	`1`	`0`	

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Recall:

`bool`	**`true`**	**`false`**
`bit`	`1`	`0`

is syntactic sugar for

$\Rightarrow$ general case covers Boolean case

Instead of using ‘printf’s for Debugging ...

```
/* after choosing a,b from {1,2,3} */
if
  :: a >= b -> max = a;
  :: a <= b -> max = b;
fi;
printf("the maximum of %d and %d is %d\n",
       a, b, max);
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Command Line Execution

(simulate, inject faults, add assertion, simulate again)

```
> spin max.pml
```

... we can employ Assertions

quoting from file **max.pml**:

```
/* after choosing a,b from {1,2,3} */
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Now, we have a first example with a formulated correctness property.

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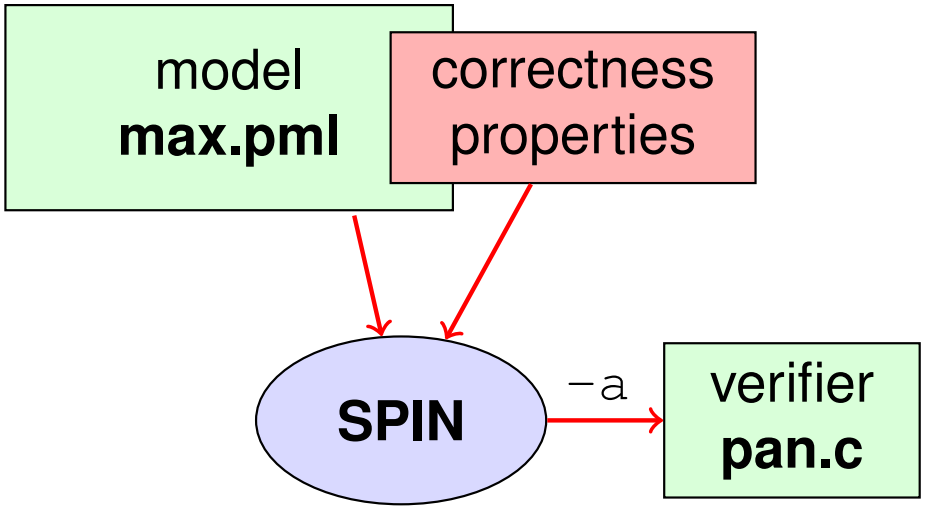
Now, we have a first example with a formulated correctness property.

We can do model checking, for the first time!

Generate Verifier in C



Command Line Execution

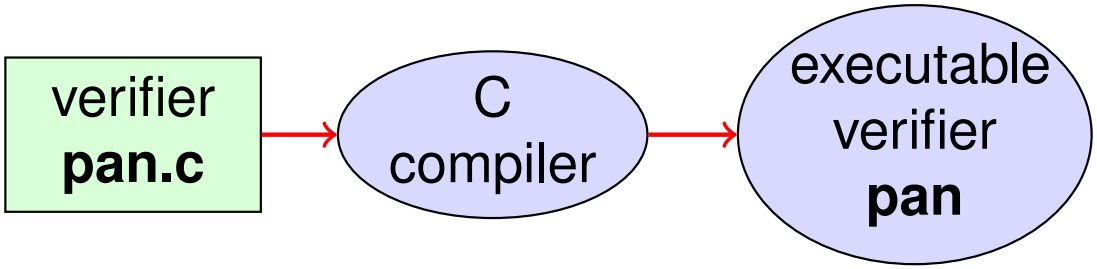
Generate Verifier in C

```
> spin -a max.pml
```

SPIN generates Verifier in C, called **pan.c**

(plus helper files)

Compile To Executable Verifier

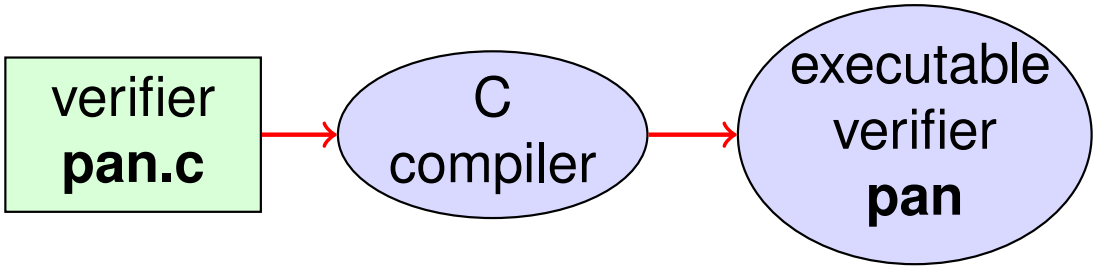


Command Line Execution

compile to executable verifier

```
> gcc -o pan pan.c
```

Compile To Executable Verifier



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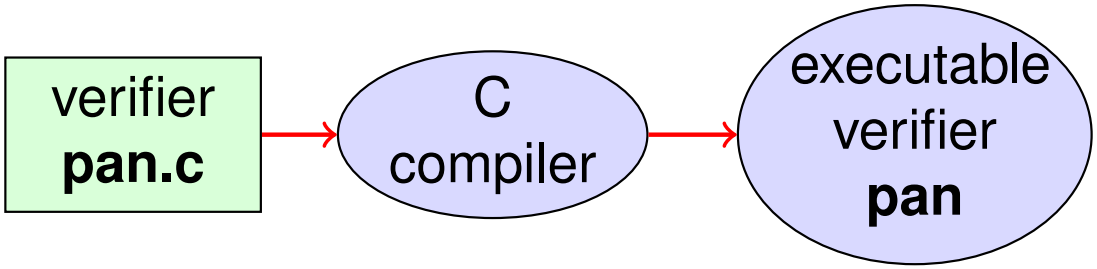

Command Line Execution

compile to executable verifier

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> gcc -o pan pan.c
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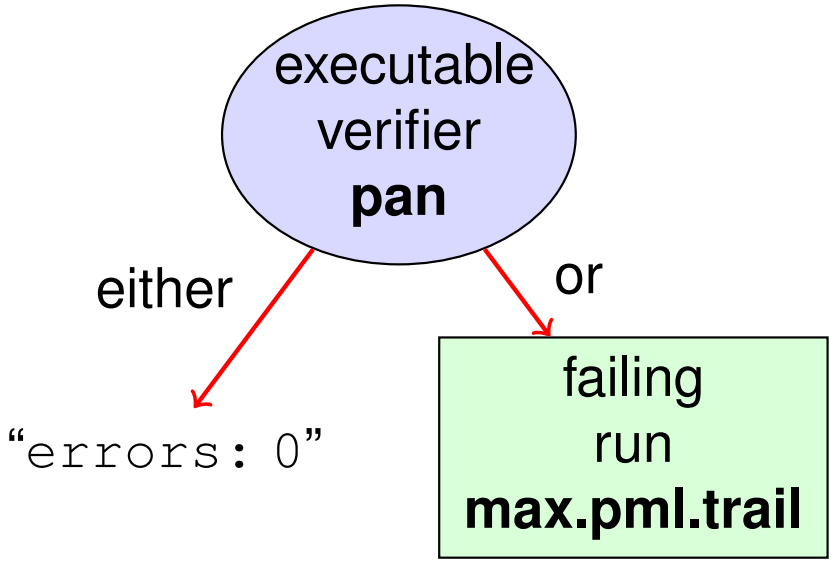
C compiler generates executable verifier **pan**

pan: historically "**p**rotocol **an**alyzer", now "**p**rocess **an**alyzer"

Run Verifier (= Model Check)



Command Line Execution

run verifier ***pan***

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> ./pan
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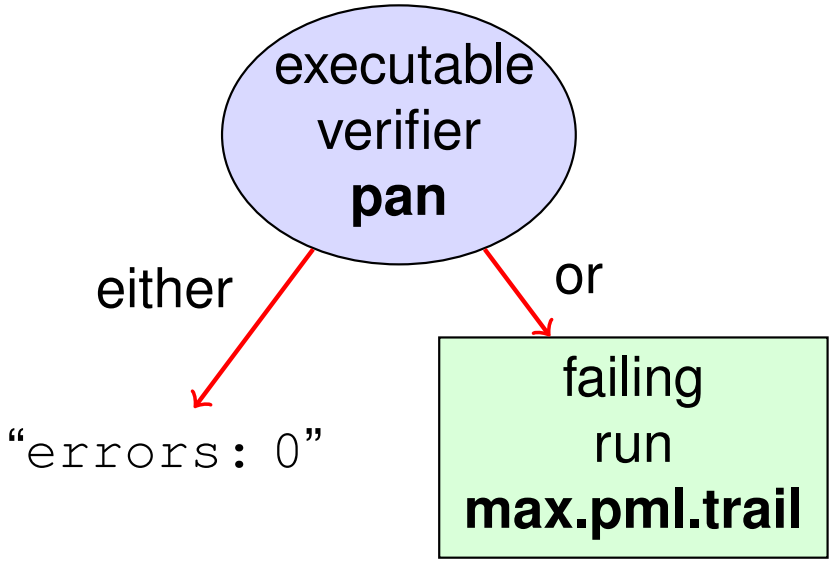

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- prints "`errors: 0`"

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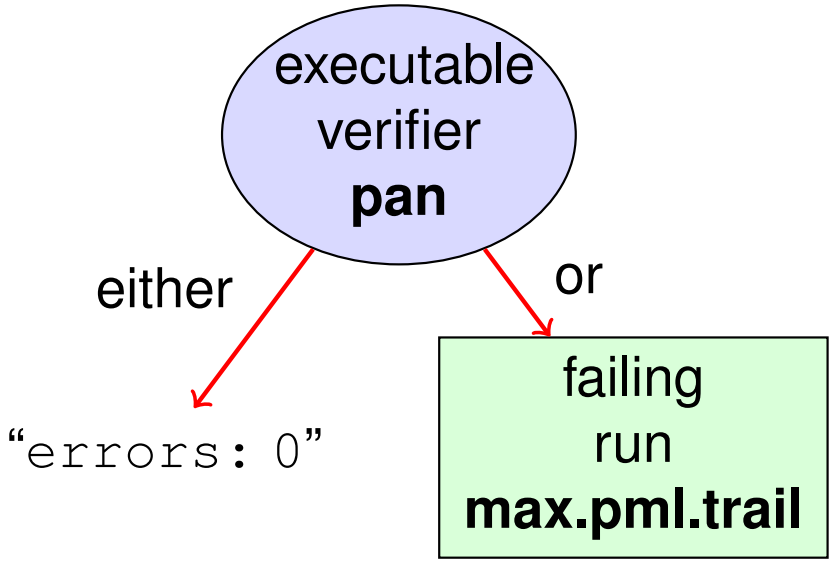

Command Line Execution

run verifier ***pan***

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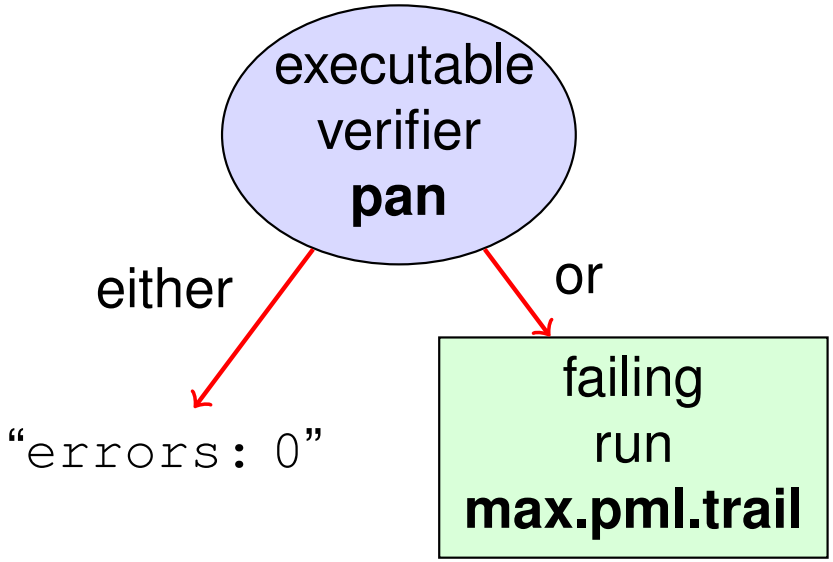
- prints "`errors: 0`" $\Rightarrow$ Correctness Property verified!

Run Verifier (= Model Check)



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- prints "`errors:` n" ($n > 0$)

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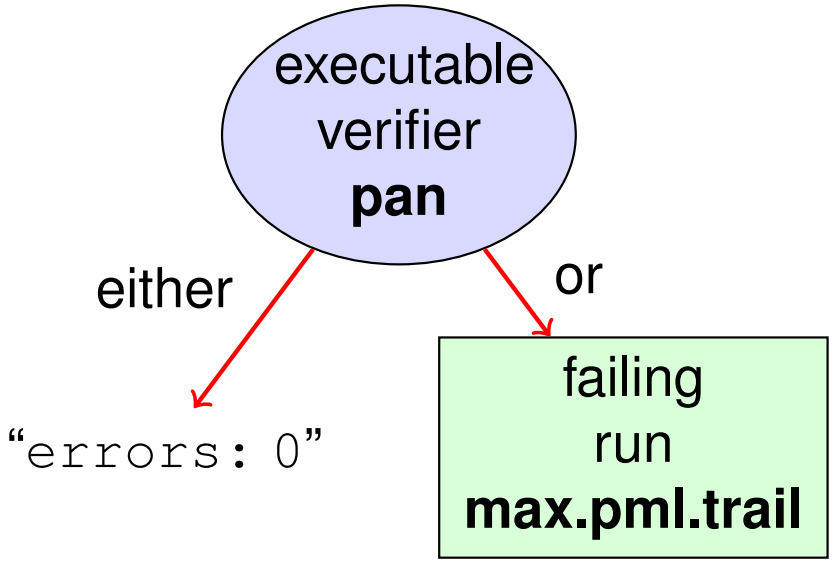

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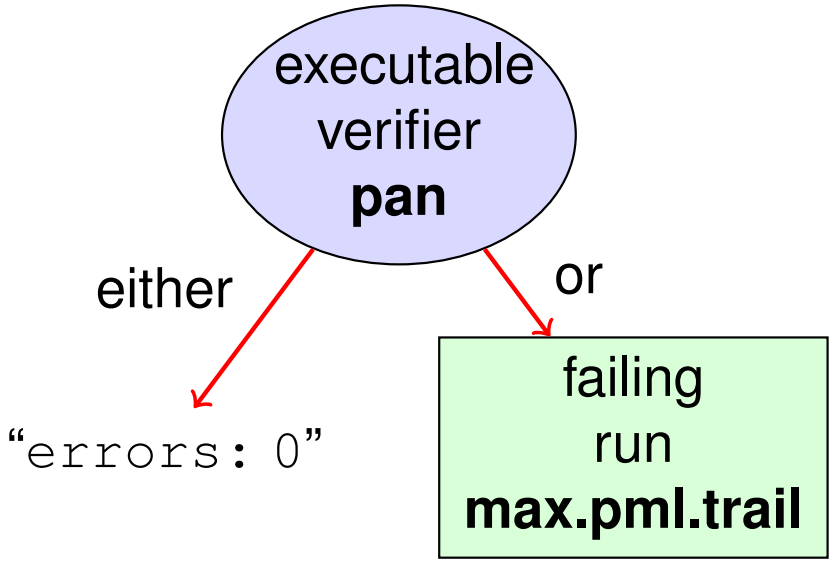

Command Line Execution

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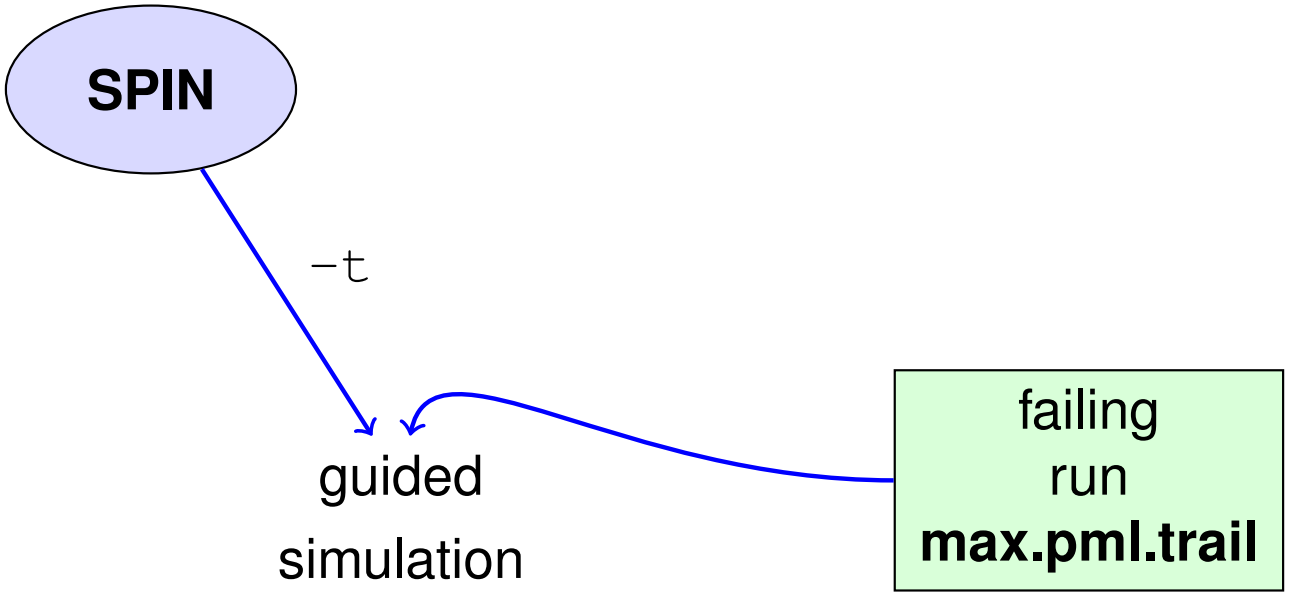
- prints "`errors: 0`", or
- prints "`errors:` n" ($n > 0$) $\Rightarrow$ counter example found!
  records failing run in **max.pml.trail**

Guided Simulation

To examine failing run: employ simulation mode, “guided” by trail file.



Command Line Execution

inject a fault, re-run verification, and then:

```
> spin -t -p -l max.pml
```

Output of Guided Simulation

can look like:

```
Starting P with pid 0
1: proc 0 (P) line  8 "max.pml" (state 1) [a = 1]
                P(0):a = 1
2: proc 0 (P) line 14 "max.pml" (state 7) [b = 2]
                P(0):b = 2
3: proc 0 (P) line 23 "max.pml" (state 13) [((a<=b))]
3: proc 0 (P) line 23 "max.pml" (state 14) [max = a]
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spin: text of failed assertion:
      assert(( ((a>b)) -> ((max==a)) : ((max==b)) ))
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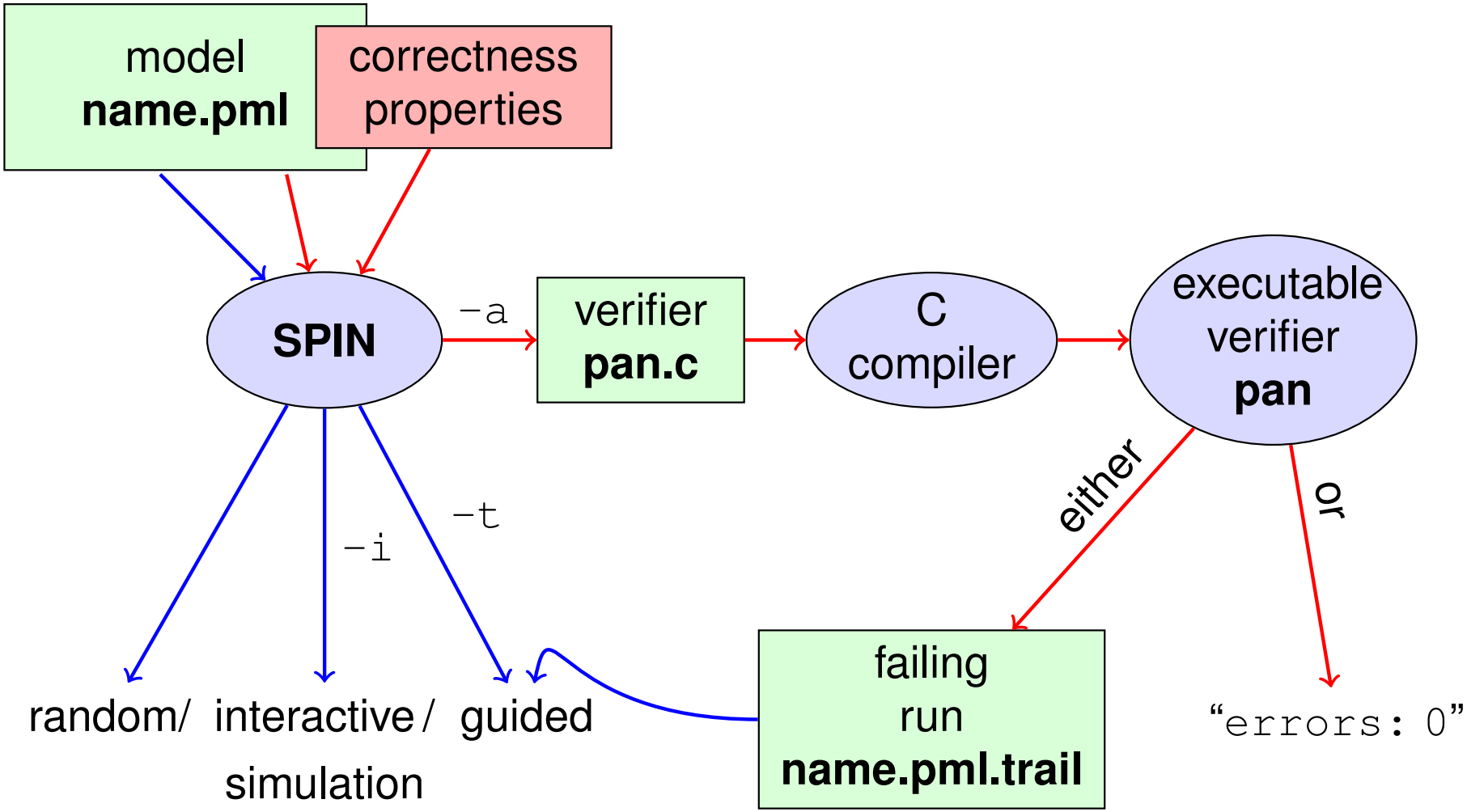
assignments in the run
values of variables whenever updated

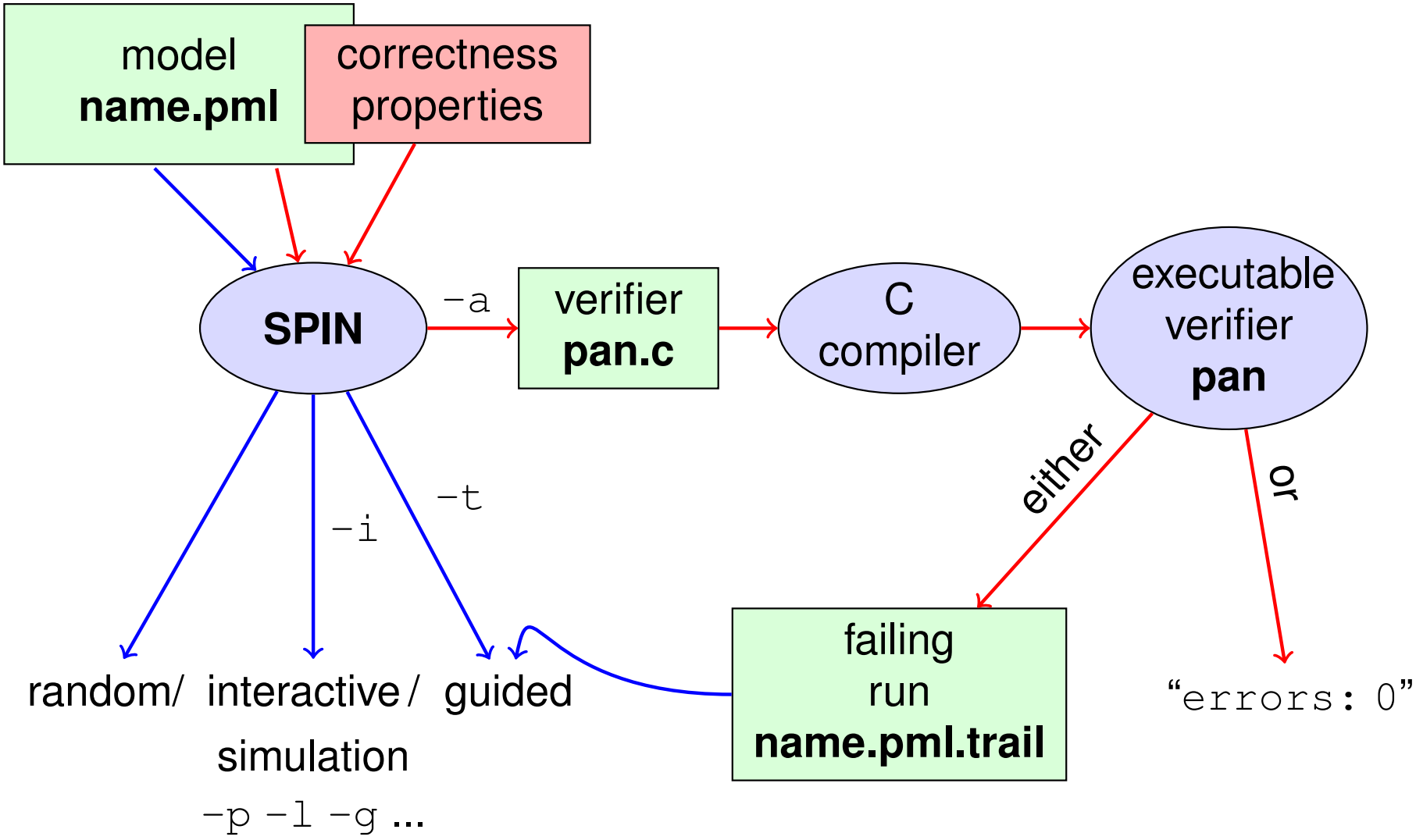
What did we do so far?

following whole cycle (most primitive example, assertions only)



What did we do so far?

following whole cycle (most primitive example, assertions only)



Further Examples: Integer Division

```
int dividend = 15;
int divisor  = 4;
int quotient, remainder;

quotient = 0;
remainder = dividend;
do
  :: remainder > divisor ->
     quotient++;
     remainder = remainder - divisor
  :: else ->
     break
od;
printf("%d divided by %d = %d, remainder = %d\n",
       dividend, divisor, quotient, remainder);
```

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```

simulate, put assertions, verify, change values, ...

Further Examples: Greatest Common Divisor

```
int x = 15, y = 20;
int a, b;
a = x; b = y;
do
  :: a > b -> a = a - b
  :: b > a -> b = b - a
  :: a == b -> break
od;
printf("The GCD of %d and %d = %d\n", x, y, a)
```

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int x = 15, y = 20;
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$\Rightarrow$ typical for model checking

Typical Command Lines

typical command line sequences:

random simulation

```
spin name.pml
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gcc -o pan pan.c
./pan
```

and in case of error

```
spin -t -p -l -g name.pml
```

SPIN Reference Card

Ben-Ari produced Spin Reference Card, summarizing

- typical command line sequences
- options for
  - SPIN
  - gcc
  - pan
- PROMELA
  - datatypes
  - operators
  - statements
  - guarded commands
  - processes
  - channels
- temproal logic syntax

Why SPIN?

- SPIN targets software, instead of hardware verification
- based on standard theory of ω-automata and linear temporal logic
- 2001 ACM Software Systems Award (other winning software systems include: Unix, TCP/IP, WWW, Tcl/Tk, Java)
- used for safety critical applications
- distributed freely as research tool, well-documented, actively maintained, large user-base in academia and in industry
- annual SPIN user workshops series held since 1995

Why SPIN? (Cont'd)

- PROMELA and SPIN are rather simple to use
- good to understand a few system really well, rather than many systems poorly
- availability of good course book (Ben-Ari)
- availability of front end JSPIN (also Ben-Ari)

What is JSPIN?

- graphical user interface for SPIN
- developed for pedagogical purposes
- written in Java
- simple user interface
- SPIN options automatically supplied
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- makes back-end calls transparent

JSPIN Demo

Command Line Execution

calling JSPIN

```
> java -jar /usr/local/jSpin/jSpin.jar
```

(with path adjusted to your setting)

or use shell script:

```
> jspin
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JSPIN **Demo**

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play around with similar examples ...

Catching A Different Type of Error

quoting from file **max2.pml**:

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/* after choosing a,b from {1,2,3} */
if
  :: a >= b -> max = a;
  :: b <= a -> max = b;
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generate and execute **pan**
⇒ reports "`errors: 1`"

Note: no **`assert`** in **max2.pml**.

Catching A Different Type of Error

Further inspection of **pan** output:

```
...
pan: invalid end state (at depth 1)
pan: wrote max2.pml.trail
...
```

Legal and Illegal Blocking

A process may legally block, as long as some other process can proceed.

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in **max1.pml**, no process can take over.

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- each location marked with an end label: "`end`*xxx*`:`"

End labels are not useful in **max1.pml**, but elsewhere, they are.
Example: `end.pml`

Literature for this Lecture

Ben-Ari Chapter 2, Sections 4.7.1, 4.7.2