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# Introduction to Artificial Intelligence

## Planning

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**UNIVERSITÄT KOBLENZ-LANDAU**

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# Outline

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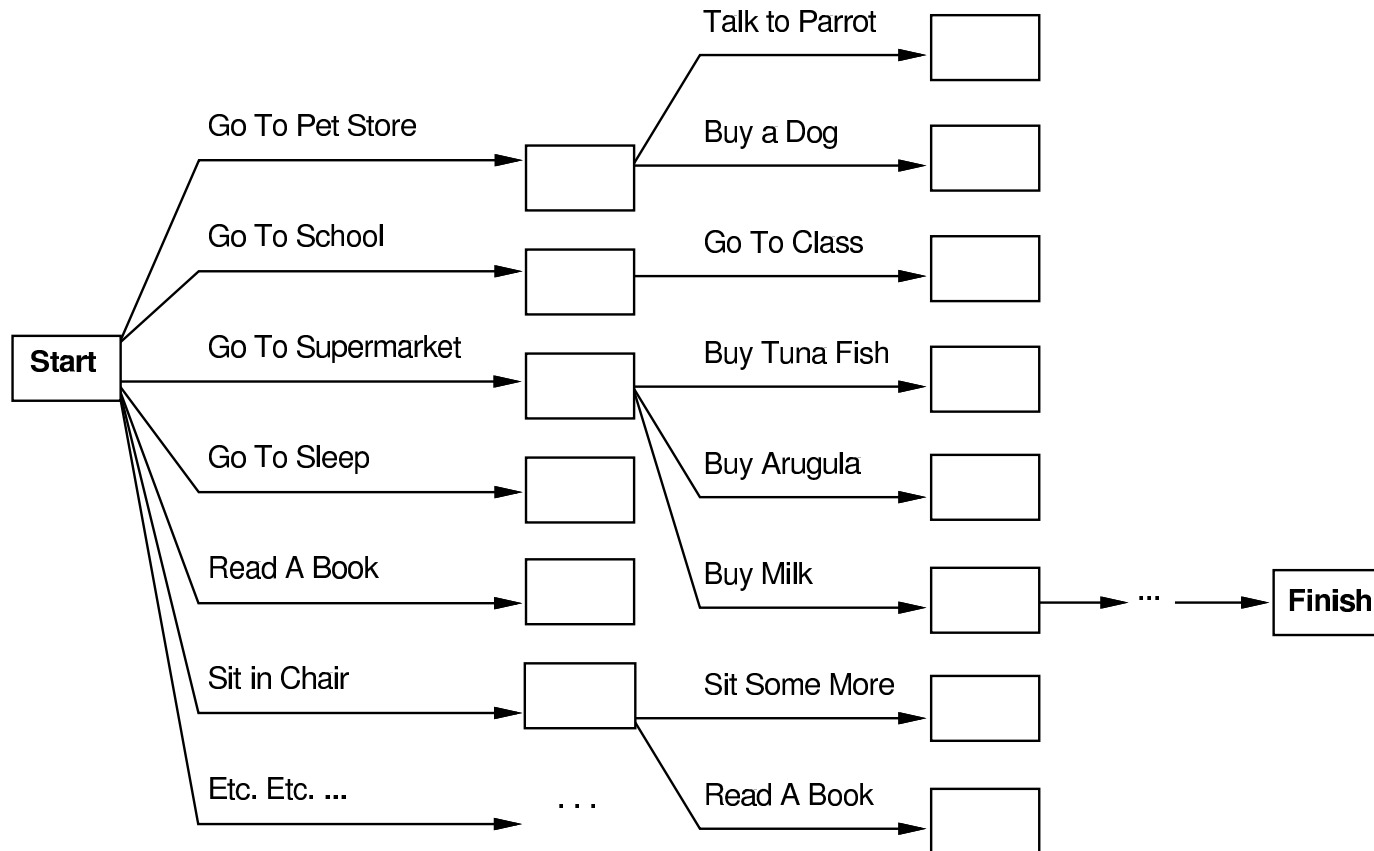
- **Search vs. planning**
- **STRIPS operators**
- **Partial-order planning**
- **The real world**
- **Conditional planning**
- **Monitoring and replanning**

# Search vs. Planning

Consider the following task

Get milk, bananas, and a cordless drill

Standard search algorithms seem to fail miserably



# Search vs. Planning

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- **Actions have requirements & consequences that should constrain applicability in a given state**
  - ⇒ **stronger interaction between actions and states needed**

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  - ⇒ **stronger interaction between actions and states needed**
- **Most parts of the world are independent of most other parts**
  - ⇒ **solve subgoals independently**

# Search vs. Planning

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- **Actions have requirements & consequences that should constrain applicability in a given state**  
⇒ **stronger interaction between actions and states needed**
- **Most parts of the world are independent of most other parts**  
⇒ **solve subgoals independently**
- **Human beings plan goal-directed; they construct important intermediate solutions first**  
⇒ **flexible sequence for construction of solution**

# Search vs. Planning

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## Planning systems do the following

- **Unify action and goal representation to allow selection (use logical language for both)**
- **Divide-and-conquer by subgoaling**
- **Relax requirement for sequential construction of solutions**

# STRIPS

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## STRIPS

STandford Research Institute Problem Solver

- Tidily arranged actions descriptions
- Restricted language (function-free literals)
- Efficient algorithms



# STRIPS: States

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States represented by:

Conjunction of ground (function-free) atoms

Example

*At(Home), Have(Bread)*

# STRIPS: States

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States represented by:

Conjunction of ground (function-free) atoms

**Example**

$At(Home), Have(Bread)$

Closed world assumption

Atoms that are not present are assumed to be false

**Example**

**State:**  $At(Home), Have(Bread)$

**Implicitly:**  $\neg Have(Milk), \neg Have(Bananas), \neg Have(Drill)$

# STRIPS: Operators

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Operator description consists of:

<b>Action name</b>	<b>Positive literal</b>	<i>Buy(Milk)</i>
<b>Precondition</b>	<b>Conjunction of positive literals</b>	<i>At(Shop) <math>\wedge</math> Sells(Shop, Milk)</i>
<b>Effect</b>	<b>Conjunction of literals</b>	<i>Have(Milk)</i>

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<b>Effect</b>	<b>Conjunction of literals</b>	<i>Have(Milk)</i>

Operator schema

Operator containing variables

*At(p) Sells(p,x)*

**Buy(x)**

*Have(x)*

# STRIPS: Operator Application

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## Operator applicability

Operator  $o$  applicable in state  $s$  if:

there is substitution  $Subst$  of the free variables such that

$$Subst(precond(o)) \subseteq s$$

# STRIPS: Operator Application

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there is substitution  $Subst$  of the free variables such that

$$Subst(precond(o)) \subseteq s$$

## Example

$Buy(x)$  is applicable in state

$$At(Shop) \wedge Sells(Shop, Milk) \wedge Have(Bread)$$

with substitution

$$Subst = \{ p/Shop, x/Milk \}$$

$At(p) \ Sells(p, x)$

**Buy(x)**

$Have(x)$

# STRIPS: Operator Application

---

## Resulting state

Computed from old state and literals in  $Subst(effect)$

- Positive literals are added to the state
- Negative literals are removed from the state
- All other literals remain unchanged  
(avoids the frame problem)

# STRIPS: Operator Application

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(avoids the frame problem)

## Formally

$$s' = (s \cup \{P \mid P \text{ a positive atom, } P \in Subst(effect(o))\}) \\ \setminus \{P \mid P \text{ a positive atom, } \neg P \in Subst(effect(o))\}$$



# STRIPS: Operator Application

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## Example

### Application of

*Drive(a, b)*

*precond:*  $At(a), Road(a, b)$

*effect:*  $At(b), \neg At(a)$

# STRIPS: Operator Application

---

## Example

### Application of

*Drive(a, b)*

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### to state

$At(Koblenz), Road(Koblenz, Landau)$

# STRIPS: Operator Application

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## Example

### Application of

*Drive(a, b)*

*precond:*  $At(a), Road(a, b)$

*effect:*  $At(b), \neg At(a)$

### to state

$At(Koblenz), Road(Koblenz, Landau)$

### results in

$At(Landau), Road(Koblenz, Landau)$

# State Space vs. Plan Space

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## Planning problem

Find a sequence of actions that make instance of the goal true

# State Space vs. Plan Space

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## Planning problem

Find a sequence of actions that make instance of the goal true

## Nodes in search space

**Standard search:** node = concrete world state

**Planning search:** node = partial plan

# State Space vs. Plan Space

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## Planning problem

Find a sequence of actions that make instance of the goal true

## Nodes in search space

**Standard search:** node = concrete world state

**Planning search:** node = partial plan

## (Partial) Plan consists of

- Set of operator applications  $S_i$
- Partial (temporal) order constraints  $S_i \prec S_j$
- Causal links  $S_i \xrightarrow{c} S_j$

**Meaning:** “ $S_i$  achieves  $c \in \text{precond}(S_j)$ ” (record purpose of steps)

# State Space vs. Plan Space

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## Operators on partial plans

- add an action and a causal link to achieve an open condition
- add a causal link from an existing action to an open condition
- add an order constraint to order one step w.r.t. another

## Open condition

A precondition of an action not yet causally linked

# State Space vs. Plan Space

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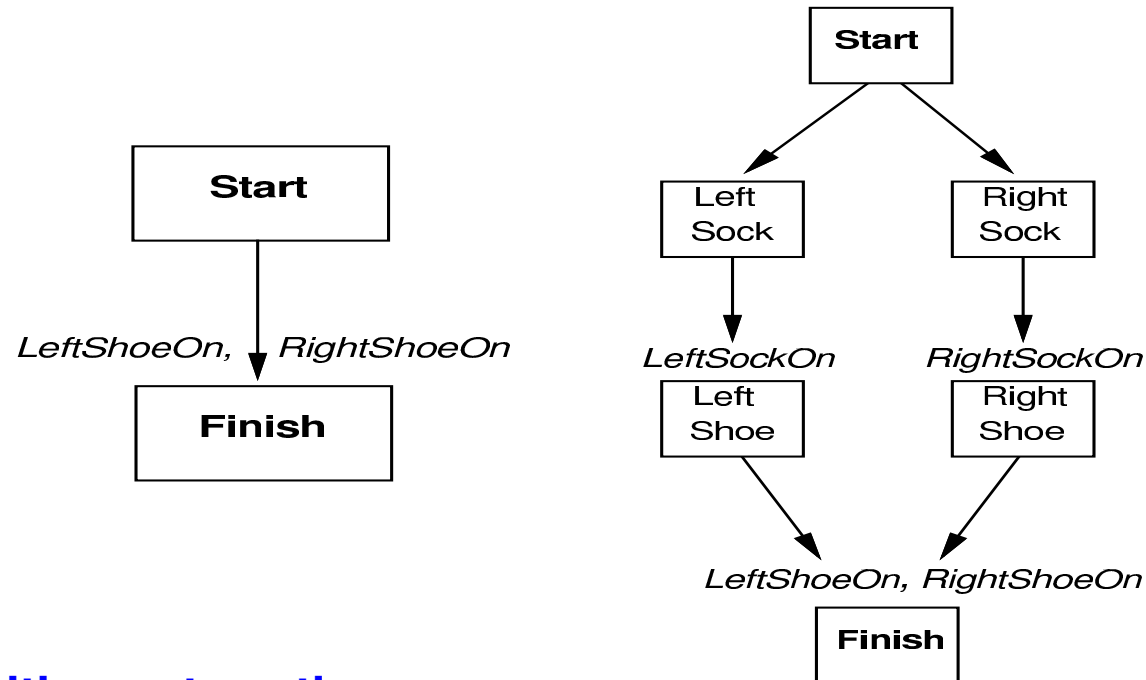
## Note

We move from incomplete/vague plans to complete, correct plans



# Partially Ordered Plans

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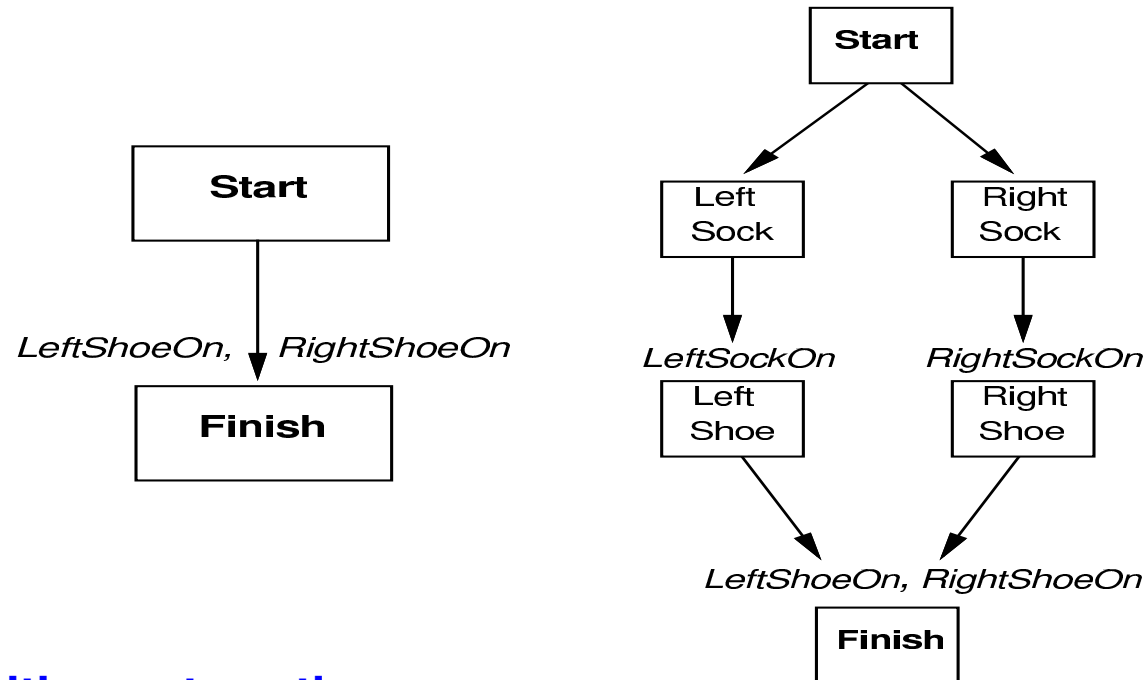
## Special steps with empty action

*Start* no precond, initial assumptions as effect)

*Finish* goal as precond, no effect

# Partially Ordered Plans

---



## Special steps with empty action

*Start* no precondition, initial assumptions as effect)

*Finish* goal as precondition, no effect

## Note

**Different paths in partial plan are *not* alternative plans, but alternative sequences of actions**

# Partially Ordered Plans

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## Complete plan

**A plan is complete iff every precondition is achieved**

# Partially Ordered Plans

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## Complete plan

A plan is complete iff every precondition is achieved

A precondition  $c$  of a step  $S_j$  is achieved (by  $S_i$ ) if

- $S_i \prec S_j$
- $c \in effect(S_i)$
- there is no  $S_k$  with  $S_i \prec S_k \prec S_j$  and  $\neg c \in effect(S_k)$   
(otherwise  $S_k$  is called a **clobberer** or **threat**)

# Partially Ordered Plans

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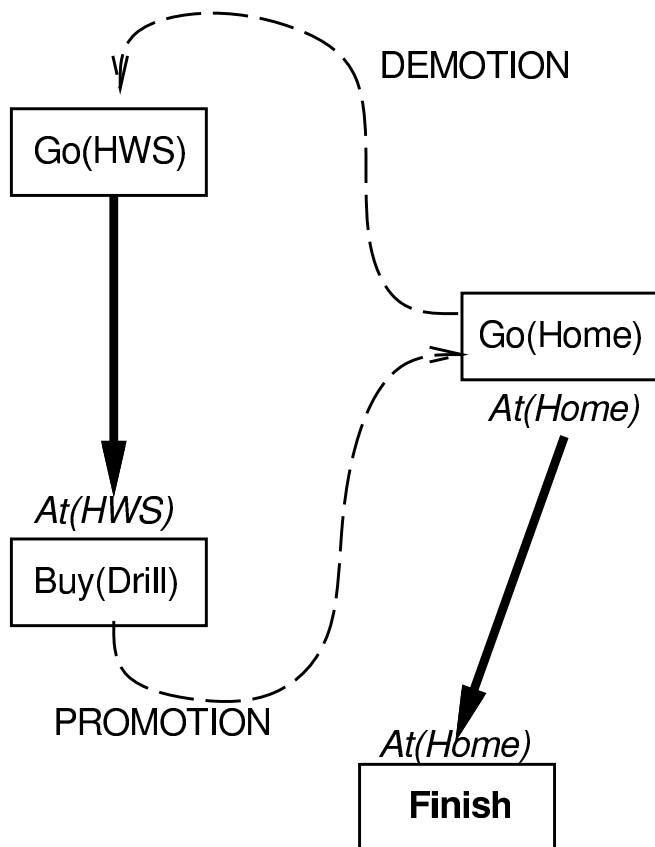
## Clobberer / threat

A potentially intervening step that destroys the condition achieved by a causal link

# Clobbering and Promotion/Demotion

## Example

$Go(Home)$  clobbers  $At(HWS)$



**Demotion**

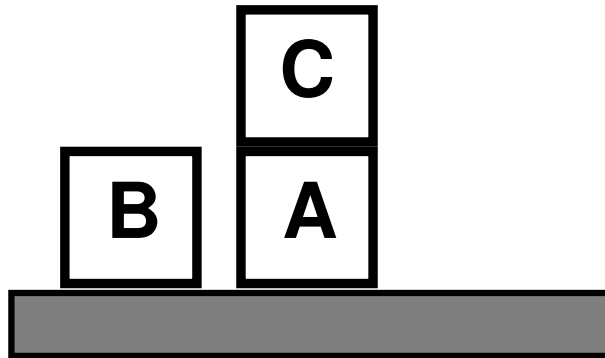
**Put before**  $Go(HWS)$

**Promotion**

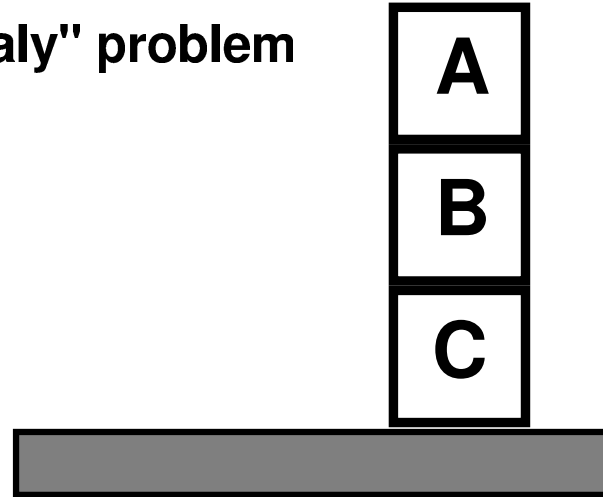
**Put after**  $Buy(Drill)$

# Example: Blocks world

"Sussman anomaly" problem



Start State



Goal State

$Clear(x) \ On(x,z) \ Clear(y)$

PutOn(x,y)

$\sim On(x,z) \ \sim Clear(y)$   
 $Clear(z) \ On(x,y)$

$Clear(x) \ On(x,z)$

PutOnTable(x)

$\sim On(x,z) \ Clear(z) \ On(x, Table)$

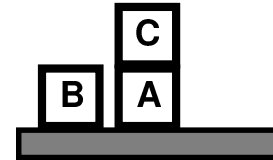
+ several inequality constraints

# Example: Blocks World

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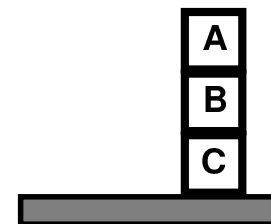
START

*On(C,A) On(A,Table) Cl(B) On(B,Table) Cl(C)*



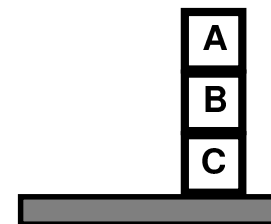
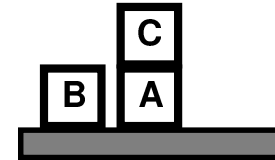
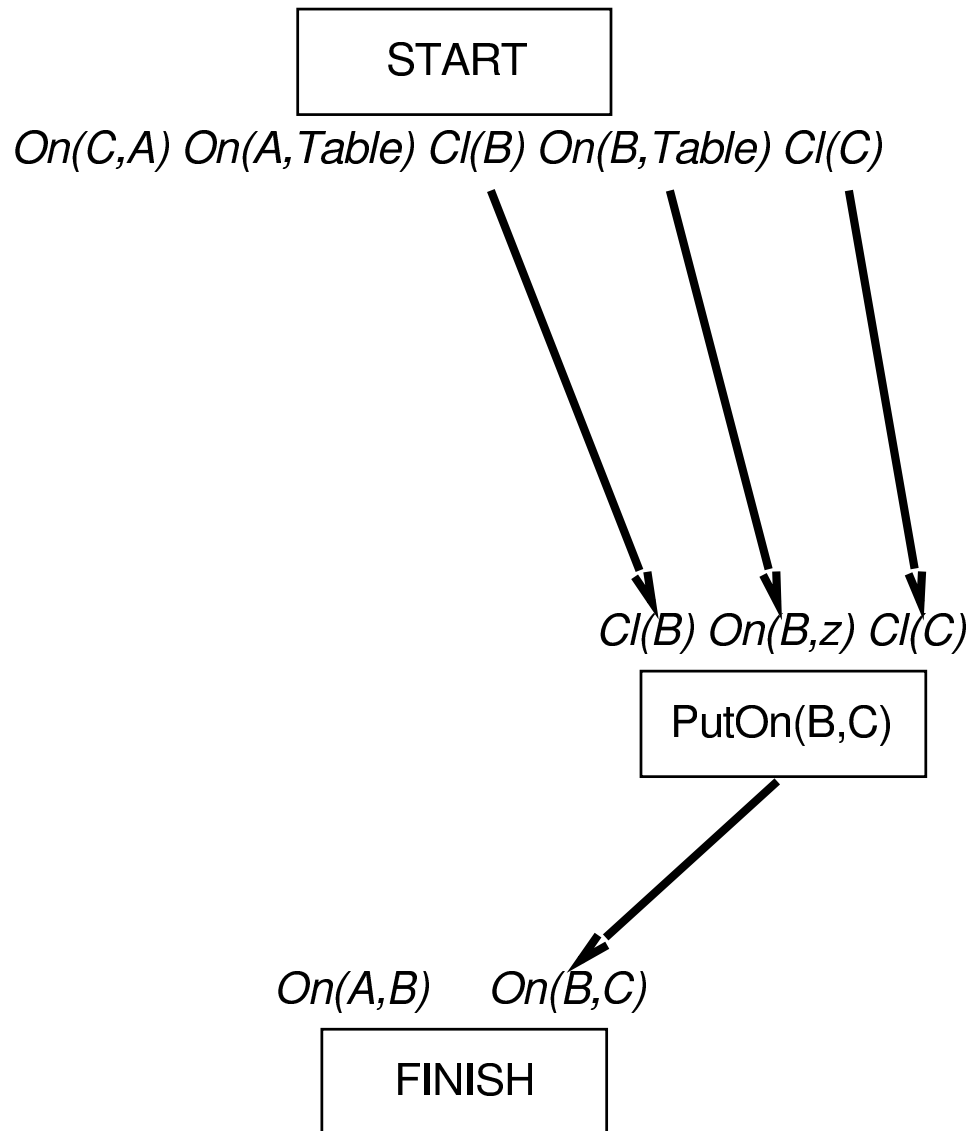
*On(A,B) On(B,C)*

FINISH

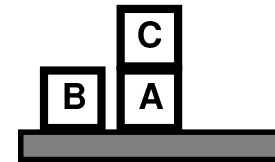
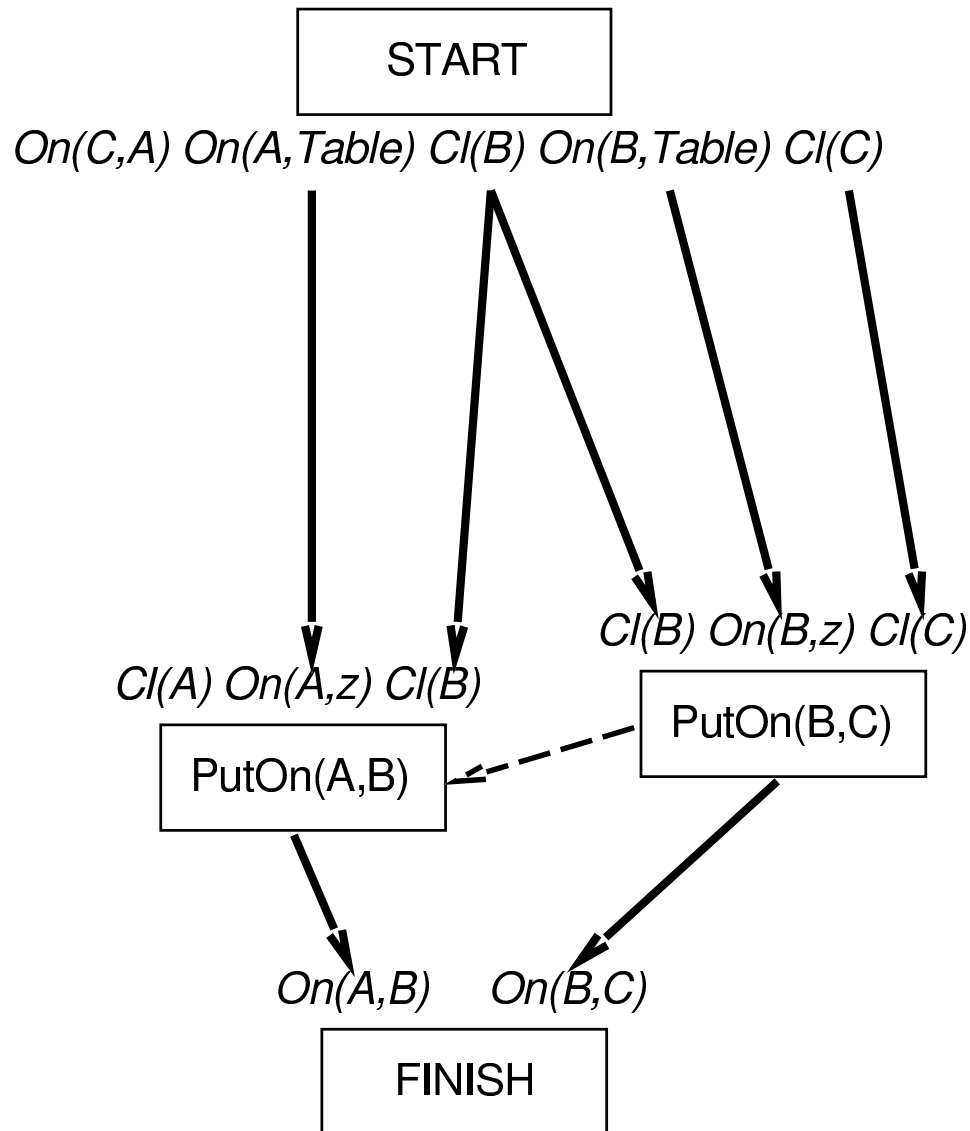




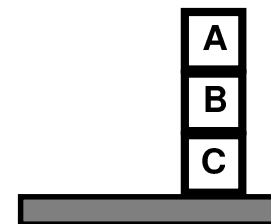
# Example: Blocks World



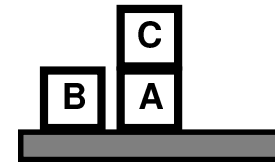
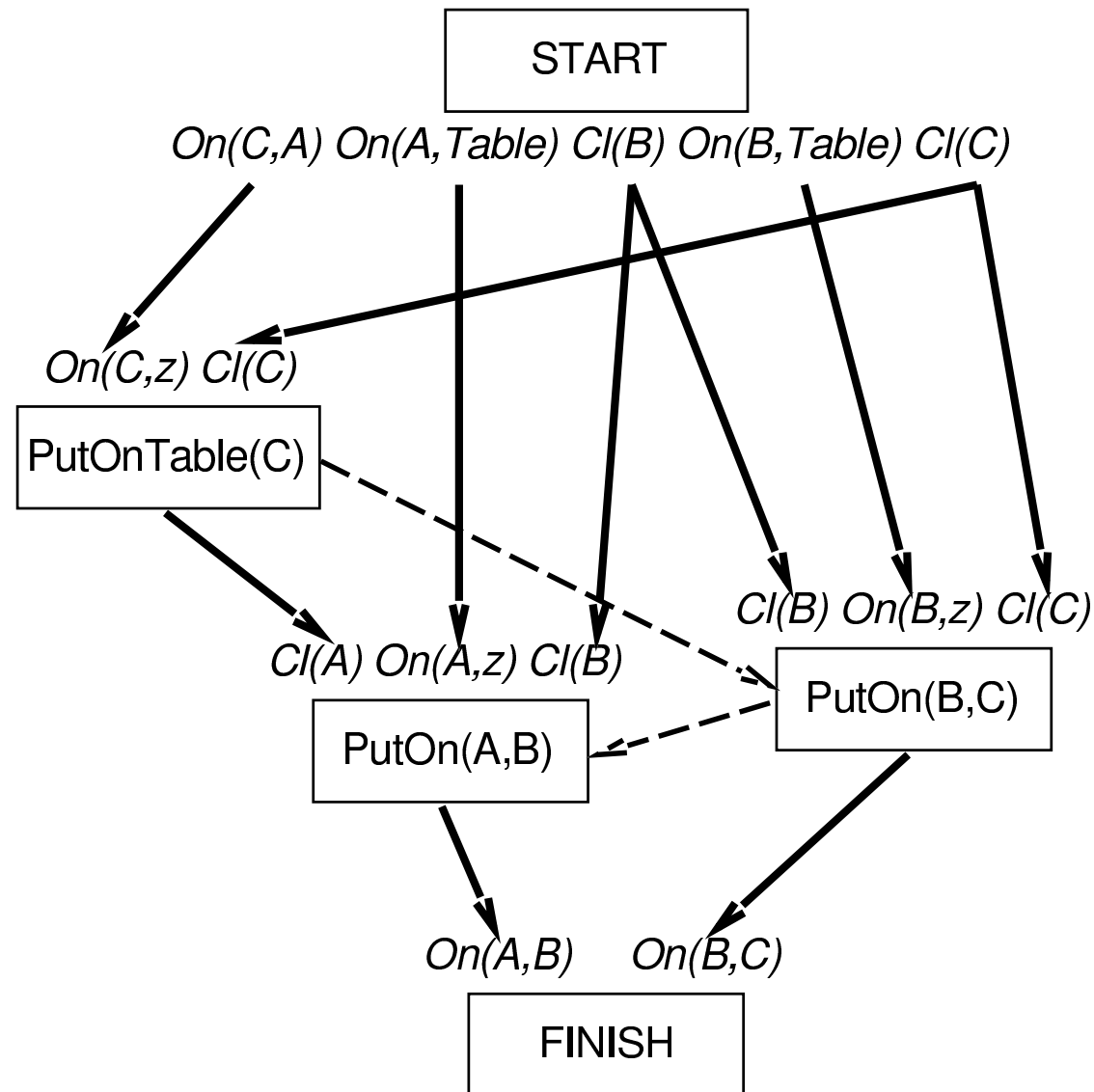
# Example: Blocks World



PutOn(A,B)  
clobbers Cl(B)  
=> order after  
PutOn(B,C)

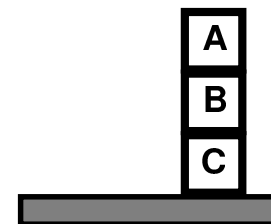


# Example: Blocks World



PutOn(A,B)  
clobbers Cl(B)  
=> order after  
PutOn(B,C)

PutOn(B,C)  
clobbers Cl(C)  
=> order after  
PutOnTable(C)



# POP (Partial Order Planner) Algorithm Sketch

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**function** POP(*initial, goal, operators*) **returns** *plan*

*plan*  $\leftarrow$  MAKE-MINIMAL-PLAN(*initial, goal*)

**loop do**

**if** SOLUTION?(*plan*) **then return** *plan*      % complete and consistent

$S_{need}, c \leftarrow$  SELECT-SUBGOAL(*plan*)

    CHOOSE-OPERATOR(*plan, operators, S<sub>need</sub>, c*)

    RESOLVE-THREATS(*plan*)

**end**

---

**function** SELECT-SUBGOAL(*plan*) **returns**  $S_{need}, c$

    pick a plan step  $S_{need}$  from STEPS(*plan*)

        with a precondition *c* that has not been achieved

**return**  $S_{need}, c$

# POP Algorithm (Cont'd)

---

**procedure** CHOOSE-OPERATOR( $plan, operators, S_{need}, c$ )

**choose** a step  $S_{add}$  from  $operators$  or  $STEPS(plan)$  that has  $c$  as an effect

**if** there is no such step **then fail**

add the causal link  $S_{add} \xrightarrow{c} S_{need}$  to  $LINKS(plan)$

add the ordering constraint  $S_{add} \prec S_{need}$  to  $ORDERINGS(plan)$

**if**  $S_{add}$  is a newly added step from  $operators$  **then**

    add  $S_{add}$  to  $STEPS(plan)$

    add  $Start \prec S_{add} \prec Finish$  to  $ORDERINGS(plan)$

# POP Algorithm (Cont'd)

---

**procedure** RESOLVE-THREATS(*plan*)

**for each**  $S_{threat}$  that threatens a link  $S_i \xrightarrow{c} S_j$  in LINKS(*plan*) **do**

**choose** either

*Demotion:* Add  $S_{threat} \prec S_i$  to ORDERINGS(*plan*)

*Promotion:* Add  $S_j \prec S_{threat}$  to ORDERINGS(*plan*)

**if not** CONSISTENT(*plan*) **then fail**

**end**

# Properties of POP

---

- **Non-deterministic search for plan, backtracks over choicepoints on failure:**
  - **choice of  $S_{add}$  to achieve  $S_{need}$**
  - **choice of promotion or demotion for clobberer**

# Properties of POP

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- **Sound and complete**



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- **There are extensions for:**  
**disjunction, universal quantification, negation, conditionals**

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- **There are extensions for:**  
**disjunction, universal quantification, negation, conditionals**
- **Efficient with good heuristics from problem description**  
**But: very sensitive to subgoal ordering**

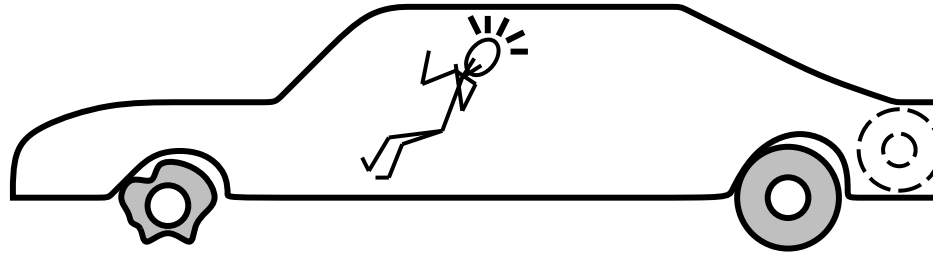
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  - **choice of promotion or demotion for clobberer**
- **Sound and complete**
- **There are extensions for:**  
**disjunction, universal quantification, negation, conditionals**
- **Efficient with good heuristics from problem description**  
**But: very sensitive to subgoal ordering**
- **Good for problems with loosely related subgoals**

# The Real World

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**START**

*~Flat(Spare) Intact(Spare) Off(Spare)  
On(Tire1) Flat(Tire1)*

*On(x) ~Flat(x)*

**FINISH**

*On(x)*

**Remove(x)**

*Off(x) ClearHub*

*Off(x) ClearHub*

**Puton(x)**

*On(x) ~ClearHub*

*Intact(x) Flat(x)*

**Inflate(x)**

*~Flat(x)*

# Things Go Wrong

---

## Incomplete information

● **Unknown preconditions**      **Example:** *Intact(Spare)?*

● **Disjunctive effects**

**Example:** *Inflate(x)* **causes**

*Inflated(x) ∨ SlowHiss(x) ∨ Burst(x) ∨ BrokenPump ∨ ...*

# Things Go Wrong

---

## Incomplete information

- **Unknown preconditions**      **Example:**  $Intact(Spare)?$

- **Disjunctive effects**

**Example:**  $Inflate(x)$  **causes**

$Inflated(x) \vee SlowHiss(x) \vee Burst(x) \vee BrokenPump \vee \dots$

## Incorrect information

- **Current state incorrect**      **Example:** spare NOT intact
- **Missing/incorrect postconditions in operators**

# Things Go Wrong

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## Incomplete information

- **Unknown preconditions**      **Example:** *Intact(Spare)?*

- **Disjunctive effects**

**Example:** *Inflate(x)* causes

*Inflated(x) ∨ SlowHiss(x) ∨ Burst(x) ∨ BrokenPump ∨ ...*

## Incorrect information

- **Current state incorrect**      **Example:** spare NOT intact

- **Missing/incorrect postconditions in operators**

## Qualification problem

- **Can never finish listing all the required preconditions and possible conditional outcomes of actions**

# Solutions

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## Conditional planning

- Plan to obtain information (**observation actions**)
- Subplan for each contingency

**Example:** [*Check(Tire1)*, **If**(*Intact(Tire1)*), [*Inflate(Tire1)*], [*CallHelp*])]

**Disadvantage:** Expensive because it plans for many unlikely cases



# Solutions

---

## Conditional planning

- Plan to obtain information (**observation actions**)
- Subplan for each contingency

**Example:**  $[Check(Tire1), \mathbf{If}(Intact(Tire1), [Inflate(Tire1)], [CallHelp])]$

**Disadvantage:** Expensive because it plans for many unlikely cases

## Monitoring/Replanning

- Assume normal states / outcomes
- Check progress **during execution**, replan if necessary

**Disadvantage:** Unanticipated outcomes may lead to failure

# Conditional Planning

---

## Execution of conditional plan

[... , **If**( $p$ , [*thenPlan*], [*elsePlan*]), ...]

**Check  $p$  against current knowledge base, execute *thenPlan* or *elsePlan***

# Conditional Planning

---

## Execution of conditional plan

[... , **If**( $p$ , [*thenPlan*], [*elsePlan*]), ...]

Check  $p$  against current knowledge base, execute *thenPlan* or *elsePlan*

## Conditional planning

Just like POP except:

If an open condition can be established by observation action

- add the action to the plan
- complete plan for each possible observation outcome
- insert conditional step with these subplans

**CheckTire(x)**

*KnowsIf(Intact(x))*

# Conditional Planning Example

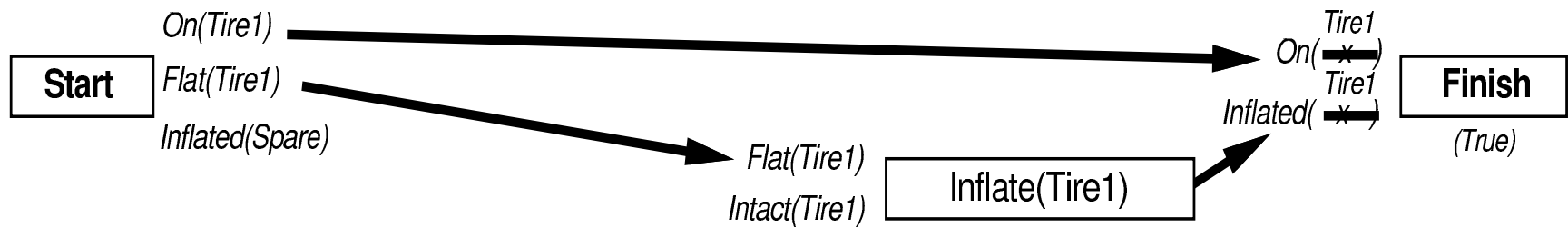
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**Start** *On(Tire1)*  
*Flat(Tire1)*  
*Inflated(Spare)*

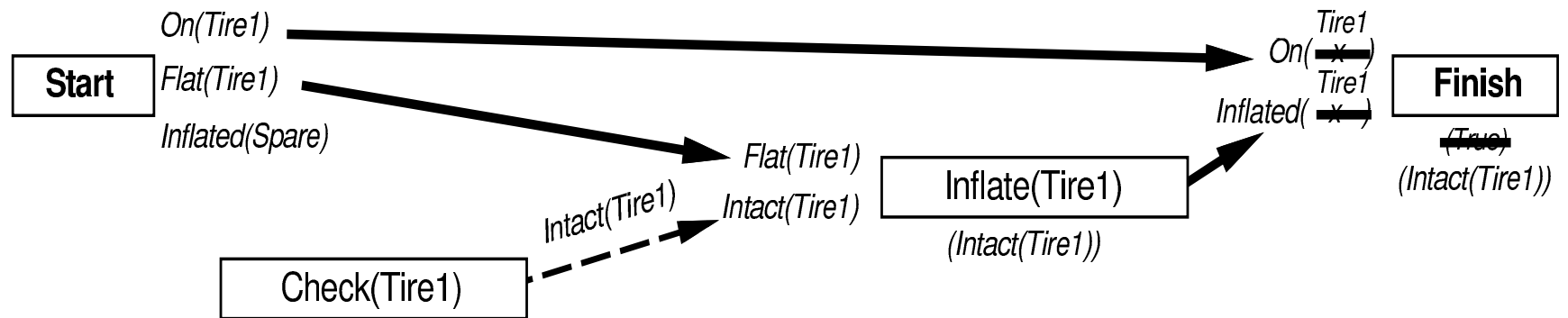
*On( x )* **Finish**  
*Inflated( x )*  
*(True)*

# Conditional Planning Example

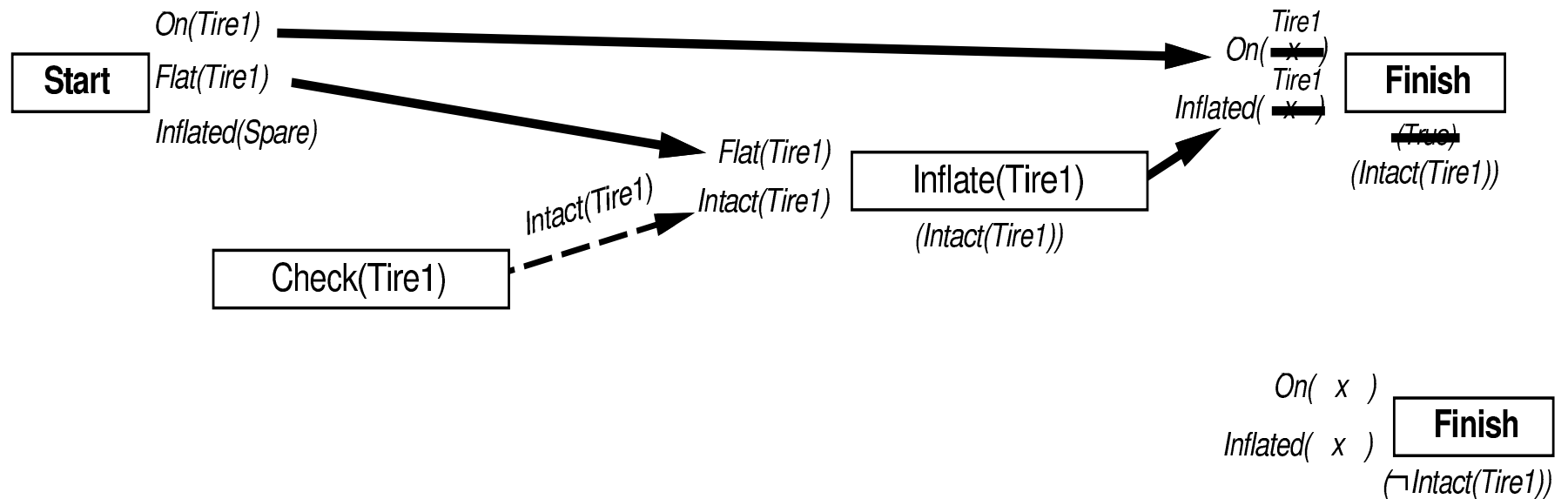
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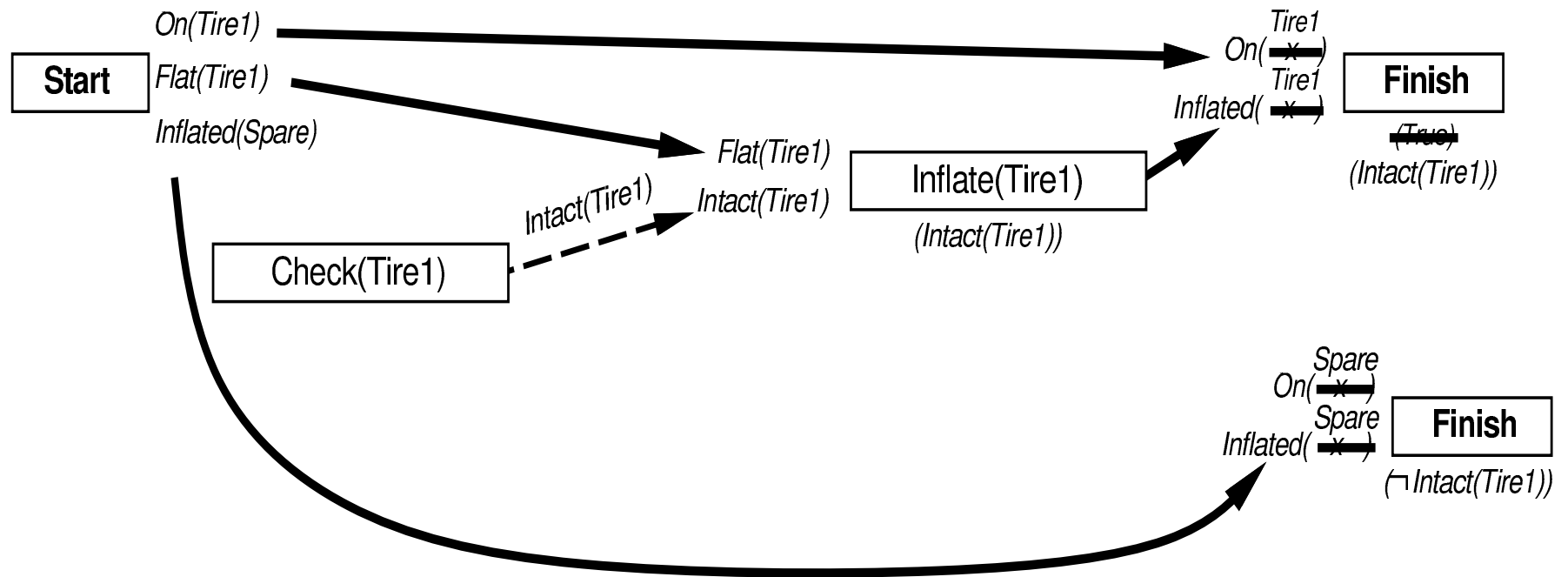
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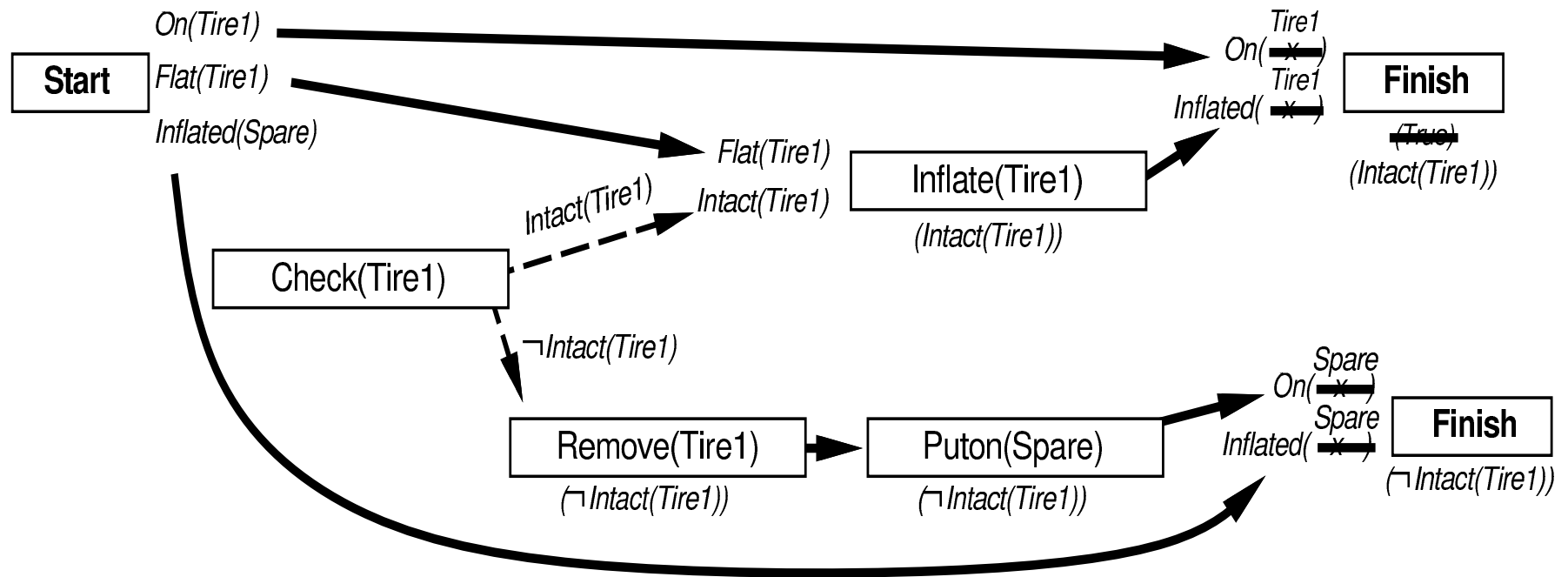


# Conditional Planning Example





# Conditional Planning Example



# Monitoring

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## Execution monitoring

**Failure:** Preconditions of remaining plan not met

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## Action monitoring

**Failure:** Preconditions of next action not met  
(or action itself fails, e.g., robot bump sensor)

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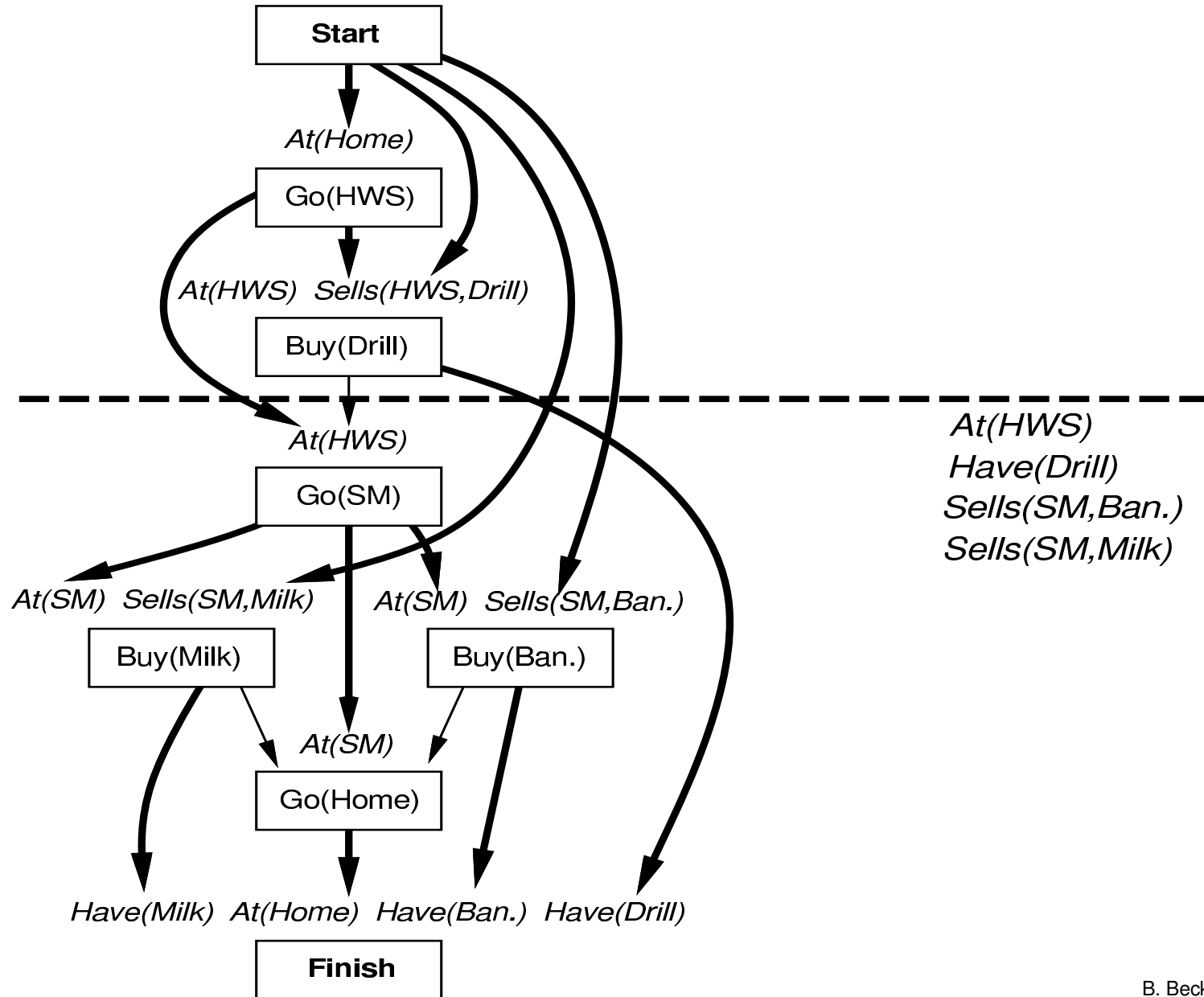
## Action monitoring

**Failure:** Preconditions of next action not met  
(or action itself fails, e.g., robot bump sensor)

## Consequence of failure

Need to **replan**

# Preconditions for Remaining Plan



# Replanning

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## Simplest

**On failure, replan from scratch**

# Replanning

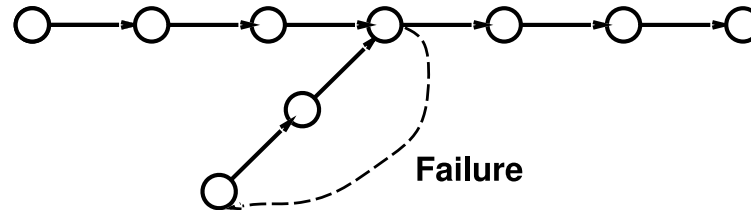
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## Simplest

On failure, replan from scratch

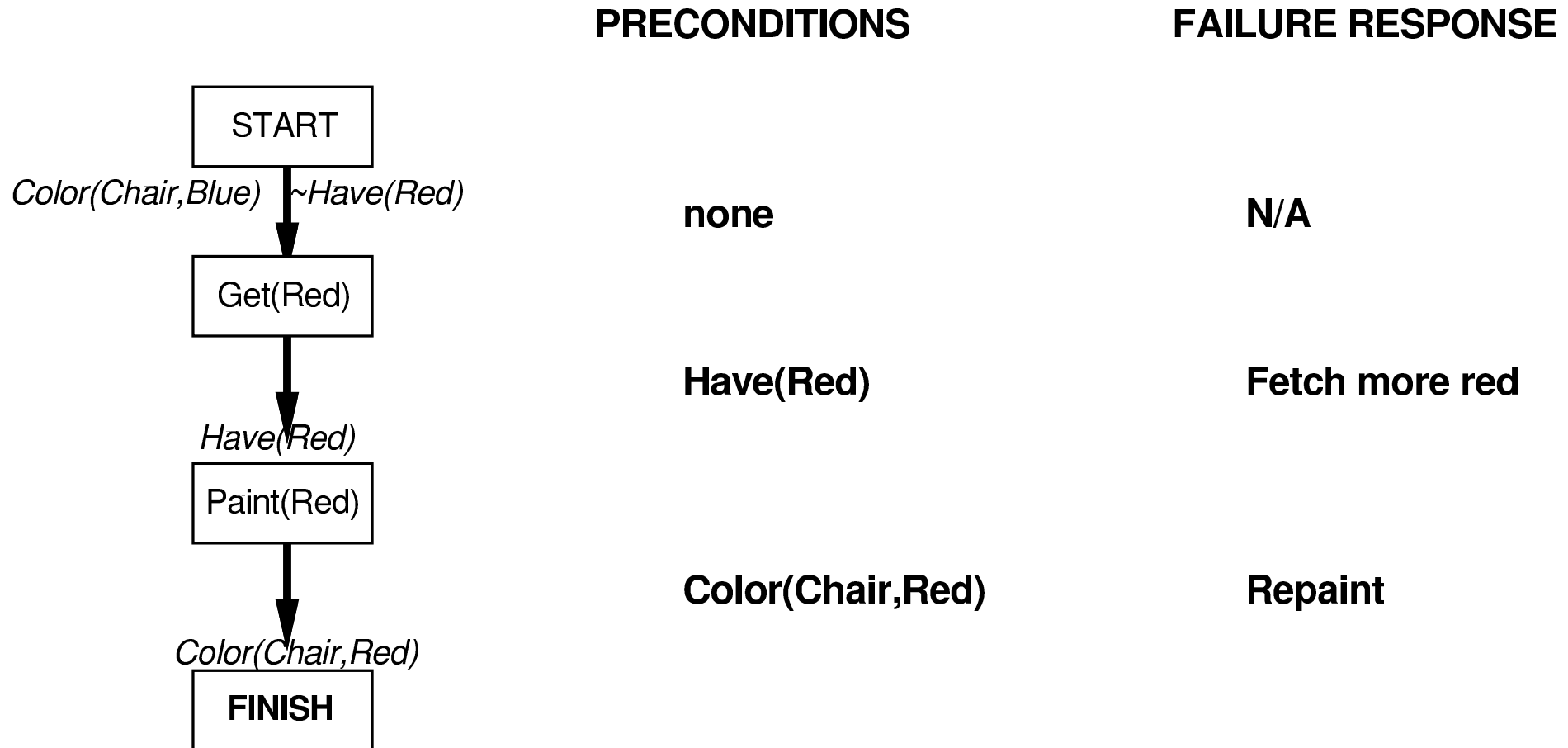
## Better

Plan to get back on track by reconnecting to best continuation



# Replanning: Example

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# Summary Planning

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- Differs from general problem search; subgoals solved independently
- STRIPS: restricted format for actions, logic-based
- Nodes in search space are partial plans
- POP algorithm
- Standard planning cannot cope with incomplete/incorrect information
- Conditional planning with sensing actions to complete information; expensive at planning stage
- Replanning based on monitoring of plan execution; expensive at execution stage