

# Formal Specification and Verification

## Introduction

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Based on a lecture by Wolfgang Ahrendt and Reiner Hähnle at  
Chalmers University, Göteborg

## Course Home Page

http:

`//www.uni-koblenz.de/~beckert/Lehre/Formale-Verifikation/`

Also linked from KLIPS

## Passing Criteria

- ▶ Written or oral exam
- ▶ Two lab hand-ins

## Course Structure

- ▶ Intro
- ▶ Propositional & Temporal Logic
- ▶ First-Order Logic
- ▶ Modeling & Verification with **PROMELA & SPIN**
- ▶ Modeling & Verification with **JML & KeY**

**PROMELA/SPIN** abstract programs, model checking, automatic

**JML/KeY** executable Java, deductive verification, semi-automatic

... more on this later!

# Motivation:

## Software Defects cause BIG Failures

Tiny faults in technical systems can have catastrophic consequences

### In particular, this goes for software systems

- ▶ Ariane 5
- ▶ Mars Climate Orbiter, Mars Sojourner
- ▶ London Ambulance Dispatch System
- ▶ Denver Airport Luggage Handling System
- ▶ Pentium-Bug
- ▶ NEDAP Voting Computer Attack

# Motivation:

## Software Defects cause OMNIPRESENT Failures

Ubiquitous Computing results in Ubiquitous Failures

**Software these days is inside just about anything:**

- ▶ Mobiles
- ▶ Smart devices
- ▶ Smart cards
- ▶ Cars

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⇒ software—and specification—quality is a growing legal issue

# Achieving Reliability in Engineering

## Some well-known strategies from civil engineering

- ▶ Precise calculations/estimations of forces, stress, etc.
- ▶ Hardware redundancy (“make it a bit stronger than necessary”)
- ▶ Robust design (single fault not catastrophic)
- ▶ Clear separation of subsystems  
Any air plane flies with dozens of known and minor defects
- ▶ Design follows patterns that are proven to work



# Why This Does Not Work For Software

- ▶ Software systems compute **non-continuous** functions  
Single bit-flip may change behaviour completely
- ▶ Redundancy as replication doesn't help against **bugs**  
Redundant SW development only viable in extreme cases
- ▶ No clear **separation** of subsystems  
Local failures often affect whole system
- ▶ Software designs have very high logic **complexity**
- ▶ Most SW engineers **untrained** to address correctness
- ▶ Cost efficiency favoured over reliability
- ▶ Design practice for reliable software in **immature** state  
for complex, particularly, distributed systems

# How to Ensure Software Correctness/Compliance?

A Central Strategy: **Testing**

(others: SW processes, reviews, libraries, ...)

**Testing against inherent SW errors (“bugs”)**

- ▶ design test configurations that hopefully are representative and
- ▶ ensure that the system behaves intentionally on them

**Testing against external faults**

- ▶ Inject faults (memory, communication) by simulation or radiation

# Limitations of Testing

- ▶ Testing shows the presence of errors, in general not their absence (exhaustive testing viable only for trivial systems)
- ▶ Representativeness of test cases/injected faults subjective  
How to test for the unexpected? Rare cases?
- ▶ Testing is labor intensive, hence expensive

# Formal Methods: The Scenario

- ▶ Rigorous methods used in system design and development
- ▶ Mathematics and symbolic logic  $\Rightarrow$  formal
- ▶ Increase confidence in a system
- ▶ Two aspects:
  - ▶ System implementation
  - ▶ System requirements
- ▶ Make formal model of both and use tools to prove mechanically that formal execution model satisfies formal requirements

# Formal Methods: The Vision

- ▶ Complement other analysis and design methods
- ▶ Are good at finding bugs  
(in code **and** specification)
- ▶ Reduce development (and test) time
- ▶ Can *ensure* certain **properties** of the system **model**
- ▶ Should ideally be as automatic as possible

# Formal Methods: Relation with Testing

- ▶ Run the system at chosen inputs and observe its behaviour
  - ▶ Randomly chosen (no guarantees, but can find bugs)
  - ▶ Intelligently chosen (by hand: **expensive!**)
  - ▶ Automatically chosen (need **formalized spec**)
- ▶ What about other inputs? (test **coverage**)
- ▶ What about the observation? (test **oracle**)

# Specification — What a System **Should** Do

- ▶ Simple properties
  - ▶ Safety properties  
Something bad will never happen (eg, mutual exclusion)
  - ▶ Liveness properties  
Something good will happen eventually
- ▶ General properties of concurrent/distributed systems
  - ▶ deadlock-free, no starvation, fairness
- ▶ Non-functional properties
  - ▶ Runtime, memory, usability, ...
- ▶ Full behavioural specification
  - ▶ Code satisfies a contract that describes its functionality
  - ▶ Data consistency, system invariants  
(in particular for efficient, i.e. redundant, data representations)
  - ▶ Modularity, encapsulation
  - ▶ Program equivalence
  - ▶ Refinement relation

# The Main Point of Formal Methods is **Not**

- ▶ To show “correctness” of entire systems  
What **IS** correctness? Always go for specific properties!
- ▶ To replace testing entirely
  - ▶ Formal methods work on models, on source code, or, at most, on bytecode level
  - ▶ Many non-formalizable properties
- ▶ To replace good design practices

There is no silver bullet!

- ▶ No correct system w/o clear requirements & good design
- ▶ One can't formally verify messy code with unclear specs



# But ...

- ▶ Formal proof can replace (infinitely) many test cases
- ▶ Formal methods can be used in automatic test case generation
- ▶ Formal methods improve the quality of specs (even without formal verification)
- ▶ Formal methods guarantee specific properties of a specific system model

# Formal Methods Aim at:

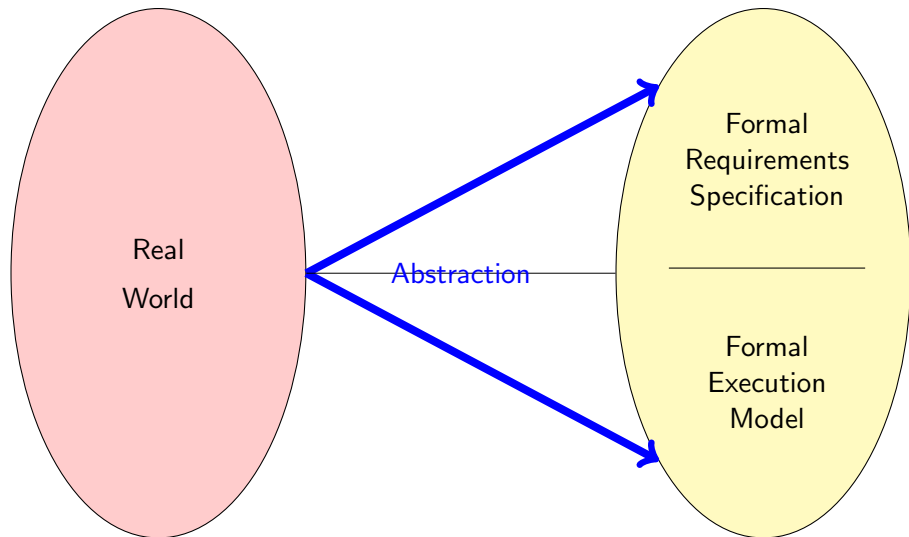
- ▶ **Saving money**  
Intel Pentium bug  
Smart cards in banking
- ▶ **Saving time**  
otherwise spent on heavy testing and maintenance
- ▶ **More complex products**  
Modern  $\mu$ -processors  
Fault tolerant software
- ▶ **Saving human lives**  
Avionics, X-by-wire  
Washing machine

# A Fundamental Fact

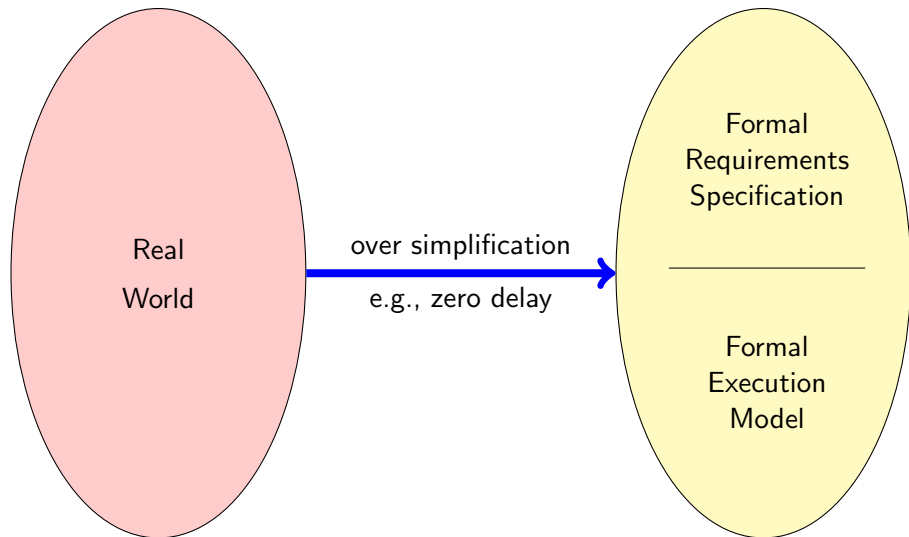
Formalisation of system requirements is hard

Let's see why ...

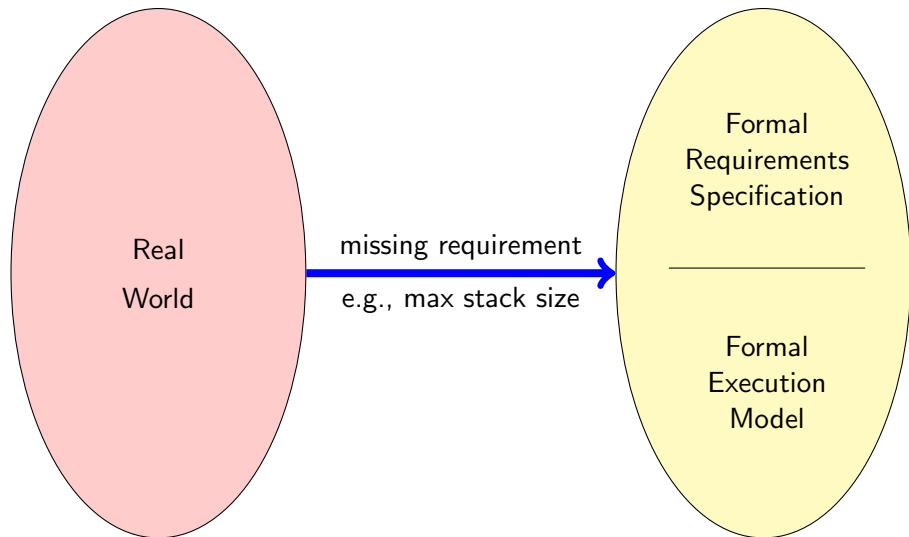
# Difficulties in Creating Formal Models



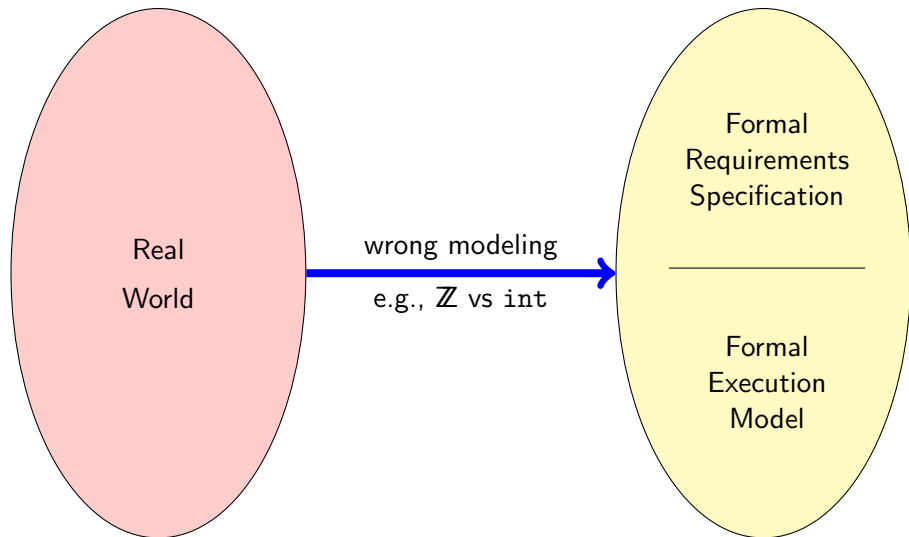
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# Difficulties in Creating Formal Models



# Formalization Helps to Find Bugs in Specs

- ▶ Wellformedness and consistency of formal specs machine-checkable
- ▶ Declared signature (symbols) helps to spot incomplete specs
- ▶ Failed verification of implementation against spec gives feedback on erroneous formalization

Errors in specifications are at least as common as errors in code



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Errors in specifications are at least as common as errors in code, but their discovery gives deep insights in (mis)conceptions of the system.

# Another Fundamental Fact

Proving properties of systems can be hard

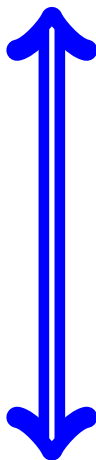
# Level of System (Implementation) Description

## ▶ Abstract level

- ▶ Finitely many states (finite datatypes)
- ▶ Tedious to program, worse to maintain
- ▶ Over-simplification, unfaithful modeling inevitable
- ▶ Automatic proofs are (in principle) possible

## ▶ Concrete level

- ▶ Infinite datatypes (pointer chains, dynamic arrays, streams)
- ▶ Complex datatypes and control structures, general programs
- ▶ Realistic programming model (e.g., Java)
- ▶ Automatic proofs (in general) impossible!



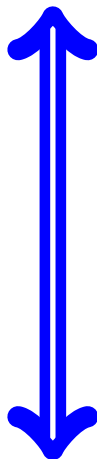
# Expressiveness of Specification

## ▶ Simple

- ▶ Simple or general properties
- ▶ Finitely many case distinctions
- ▶ Approximation, low precision
- ▶ Automatic proofs are (in principle) possible

## ▶ Complex

- ▶ Full behavioural specification
- ▶ Quantification over infinite domains
- ▶ High precision, tight modeling
- ▶ Automatic proofs (in general) impossible!



# Main Approaches

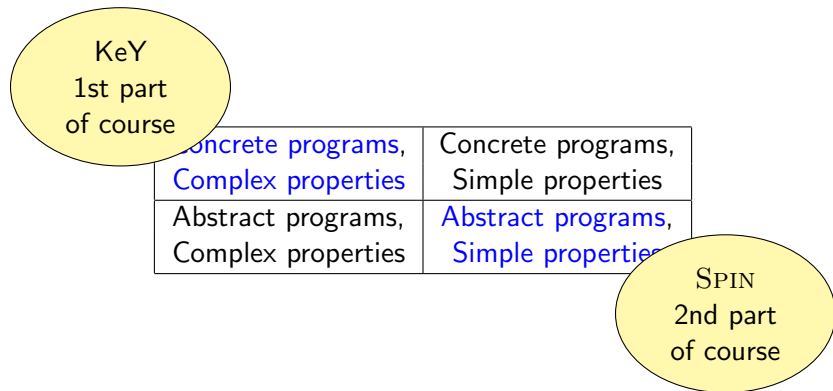
Concrete programs, Complex properties	Concrete programs, Simple properties
Abstract programs, Complex properties	Abstract programs, Simple properties

# Main Approaches

Concrete programs, Complex properties	Concrete programs, Simple properties
Abstract programs, Complex properties	Abstract programs, Simple properties

SPIN  
2nd part  
of course

# Main Approaches



- ▶ “Automatic” Proof

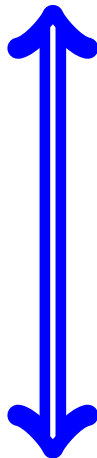
Perhaps better called “batch-mode” proof

- ▶ No interaction during verification necessary
- ▶ Proof may fail or result inconclusive  
Tuning of tool parameters necessary
- ▶ Formal specification still “by hand”

- ▶ “Semi-Automatic” Proof

Perhaps better called “interactive” proof

- ▶ Interaction may be required during proof
- ▶ Need certain knowledge of tool internals  
Intermediate inspection can be helpful, too
- ▶ Proof is checked by tool





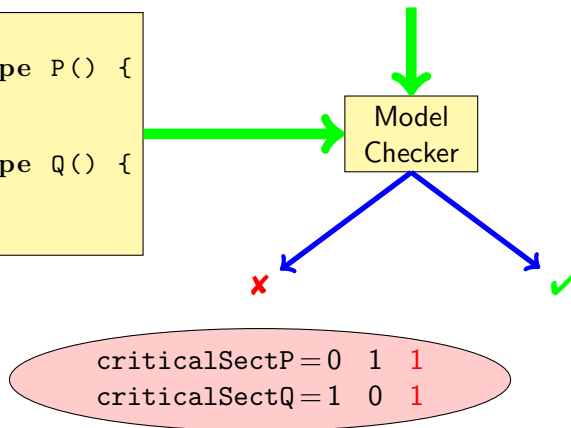
# Model Checking

## System Model

```
byte n = 0;  
active proctype P() {  
  n = 1;  
}  
active proctype Q() {  
  n = 2;  
}
```

## System Property

$[\ ] ! (\text{criticalSectP} \ \&\& \ \text{criticalSectQ})$



# Model Checking in Industry

- ▶ Hardware verification
  - ▶ Good match between limitations of technology and application
  - ▶ Intel, Motorola, AMD, ...
- ▶ Software verification
  - ▶ Specialized software: control systems, protocols
  - ▶ Typically no checking of executable source code, but of abstraction
  - ▶ Bell Labs, Ericsson, Microsoft

# Deductive Verification

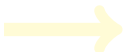
Java Code

Formal specification

# Deductive Verification

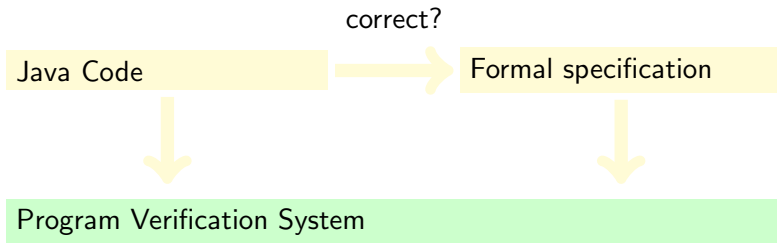
correct?

Java Code



Formal specification

# Deductive Verification



# Deductive Verification

correct ✓

Java Code



Formal specification



Program Verification System

# Deductive Verification

correct ✓

Java Code



Formal specification



Program Verification System

Proof rules establish relation “implementation conforms to specs”

**Computer support essential for verification of real programs**

`synchronized java.lang.StringBuffer append(char c)`

- ▶ ca. 15.000 proof steps
- ▶ ca. 200 case distinctions
- ▶ Two human interactions, ca. 1 minute computing time

# Deductive Verification in Industry

- ▶ Hardware verification
  - ▶ For complex systems, most of all floating-point processors
  - ▶ Intel, Motorola, AMD, . . .
- ▶ Software verification
  - ▶ Safety critical systems:
    - ▶ Paris driverless metro (Meteor)
    - ▶ Emergency closing system in North Sea
  - ▶ Libraries
  - ▶ Implementations of Protocols



# A Major Case Study with SPIN

## Checking feature interaction for telephone call processing software

- ▶ Software for PathStar<sup>TM</sup> server from Lucent Technologies
- ▶ Automated abstraction of unchanged C code into PROMELA
- ▶ Web interface, with SPIN as back-end, to:
  - ▶ track properties (ca. 20 temporal formulas)
  - ▶ invoke verification runs
  - ▶ report error traces
- ▶ Finds shortest possible error trace, reported as C execution trace
- ▶ Work farmed out to 16 computers, daily, overnight runs
- ▶ 18 months, 300 versions of system model, 75 bugs found
- ▶ strength: detection of undesired feature interactions (difficult with traditional testing)
- ▶ Main challenge: defining meaningful properties

# A Major Case Study with KeY

## Mondex Electronic Purse

- ▶ Specified and implemented by NatWest ca. 1996
- ▶ Original formal specs in **Z** and proofs by hand
- ▶ Reformulated specs in JML, implementation in Java Card
- ▶ Can be run on actual smart card
- ▶ Full functional verification
- ▶ Total effort 4 person months
- ▶ With correct invariants: proofs fully automatic
- ▶ Main challenge: **loop invariants, getting specs right**

# Tool Support is Essential

## Some Reasons for Using Tools

- ▶ Automate repetitive tasks
- ▶ Avoid clerical errors, etc.
- ▶ Cope with large/complex programs
- ▶ Make verification certifiable

## Tools are Used in this Course in Both Parts:

**SPIN** to verify PROMELA programs against Temporal Logic specs

**JSPIN** as a Java interface for SPIN

**Key** to verify Java (Card) programs against contracts in JML

Both are free and run on Windows/Unixes/Mac  
(will be available via course webpage)

**Install them on your computer!**

# Future Trends

- ▶ Design for formal verification
- ▶ Combining semi-automatic methods with SAT, theorem provers
- ▶ Combining static analysis of programs with automatic methods and with theorem provers
- ▶ Combining test and formal verification
- ▶ Integration of formal methods into SW development process
- ▶ Integration of formal method tools into CASE tools
- ▶ Applying formal methods to dependable systems design
- ▶ Scaling formal methods to open, distributed, adaptive systems

# Literature for this Lecture

- FM in SE** B. Beckert, R. Hähnle, T. Hoare, D. Smith, C. Green, S. Ranise, C. Tinelli, T. Ball, and S. K. Rajamani: Intelligent Systems and Formal Methods in Software Engineering. **IEEE Intelligent Systems**, 21(6):71–81, 2006.
- SPIN** Gerard J. Holzmann: A Verification Model of a Telephone Switch. In: **The Spin Model Checker**, pp 299–324, Chapter 14, Addison Wesley, 2004.
- KeY** R. Hähnle: A New Look at Formal Methods for Software Construction. In: B. Beckert, R. Hähnle, and P. Schmitt, editors. *Verification of Object-Oriented Software: The KeY Approach*, pp 1–18, vol 4334 of *LNCS*. Springer, 2006.

## Formal Methods ...

- ▶ Are (more and more) used in practice
- ▶ Can shorten development time
- ▶ Can push the limits of feasible complexity
- ▶ Can increase quality/reliability of systems dramatically

# Summary

## Formal Methods ...

- ▶ Are (more and more) used in practice
- ▶ Can shorten development time
- ▶ Can push the limits of feasible complexity
- ▶ Can increase quality/reliability of systems dramatically

Those responsible for software management should consider formal methods, especially within the realm of safety-critical, security-critical, and cost-intensive software

# You will gain experience in ...

... more than Formal Methods (in the strict sense)

- ▶ modelling, and modelling languages
- ▶ specification, and specification languages
- ▶ in depth analysis of possible system behaviour
- ▶ typical types of errors
- ▶ reasoning about system (mis)behaviour
- ▶ ...