

How banks can maintain stability

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Class-invariant based
reasoning with
semantic collaboration

Reasoning about OO

I'll present a framework for reasoning about the **functional correctness** of **object-oriented** programs based on **class (object) invariants**.

Reasoning about OO

Methodology: semantic collaboration

- includes an ownership scheme

Implementation: AutoProof verifier

- for simplicity, I will also use “AutoProof” to refer to the methodology

Reference language: Eiffel

- but practically everything applicable to Java/JML and similar OO languages

Main features of the framework

- Targets idiomatic OO structures (OO patterns)
- Flexible (semantic)
- Reasonably concise (defaults)
- Applicable to realistic implementations (data structure library)
- **Sequential** programs only



AutoProof in a nutshell

AutoProof is an **auto-active** verifier for Eiffel

- Prover for **functional** properties
- All-out support of **object-oriented idiomatic** structures (e.g. patterns)
 - Based on **class invariants**



Nadia Polikarpova



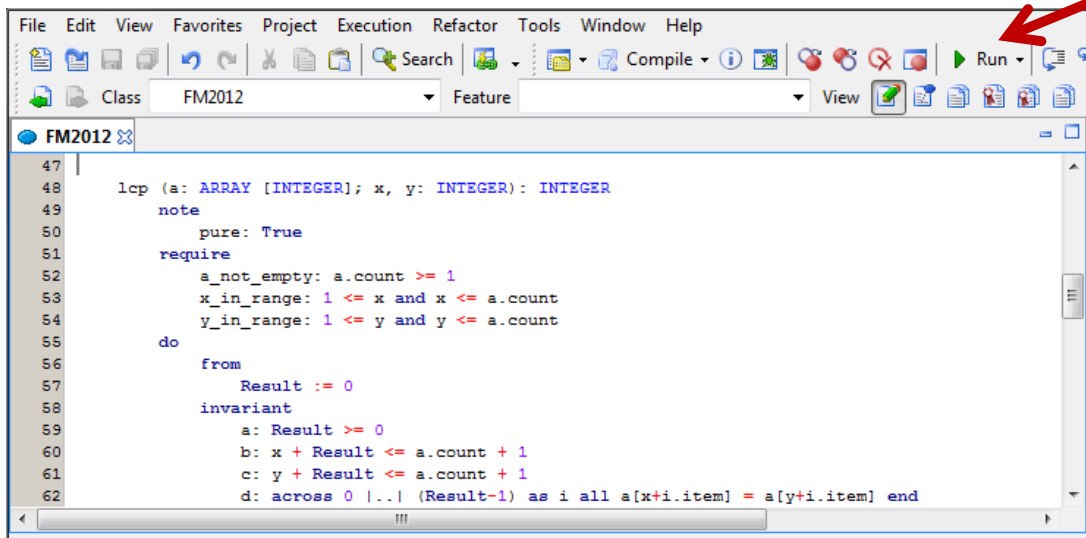
Julian Tschannen



Bertrand Meyer

Auto-active user/tool interaction

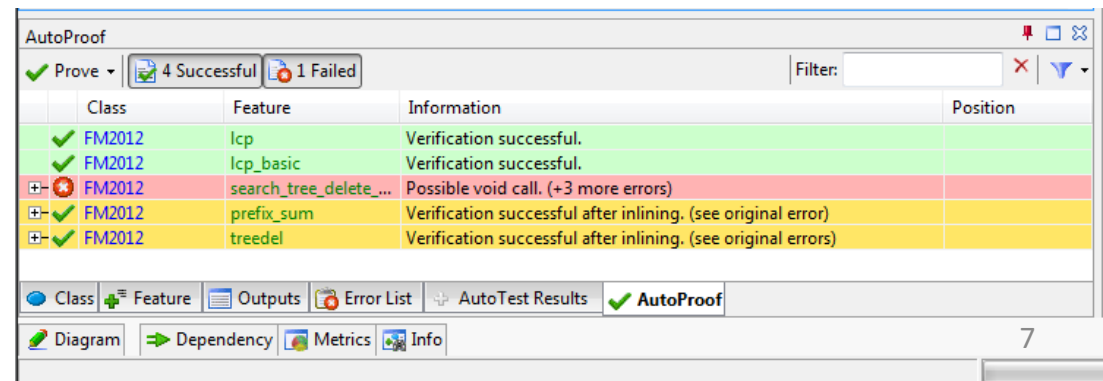
1. Code + Annotations



```
47 |
48 | lcp (a: ARRAY [INTEGER]; x, y: INTEGER): INTEGER
49 | note
50 |   pure: True
51 | require
52 |   a_not_empty: a.count >= 1
53 |   x_in_range: 1 <= x and x <= a.count
54 |   y_in_range: 1 <= y and y <= a.count
55 | do
56 |   from
57 |     Result := 0
58 |   invariant
59 |     a: Result >= 0
60 |     b: x + Result <= a.count + 1
61 |     c: y + Result <= a.count + 1
62 |     d: across 0 |..| (Result-1) as i all a[x+i.item] = a[y+i.item] end
```

2. Push button

3. Verification outcome



AutoProof

✓ Prove ▾ 4 Successful 1 Failed Filter: []

Class	Feature	Information	Position
✓ FM2012	lcp	Verification successful.	
✓ FM2012	lcp_basic	Verification successful.	
✗ FM2012	search_tree_delete_...	Possible void call. (+3 more errors)	
✗ FM2012	prefix_sum	Verification successful after inlining. (see original error)	
✗ FM2012	treedel	Verification successful after inlining. (see original errors)	

Class Feature Outputs Error List AutoTest Results ✓ AutoProof

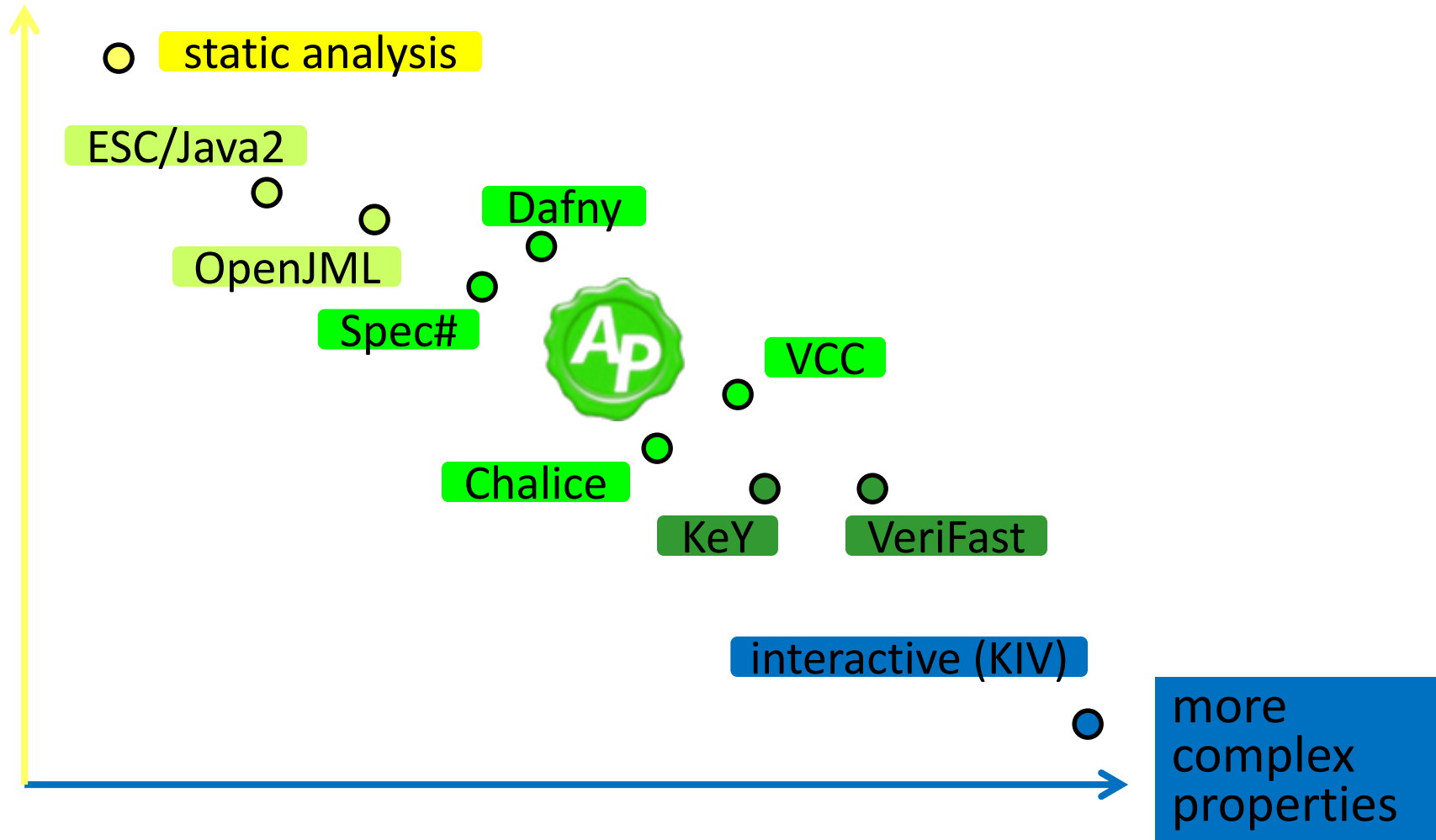
Diagram Dependency Metrics Info

7

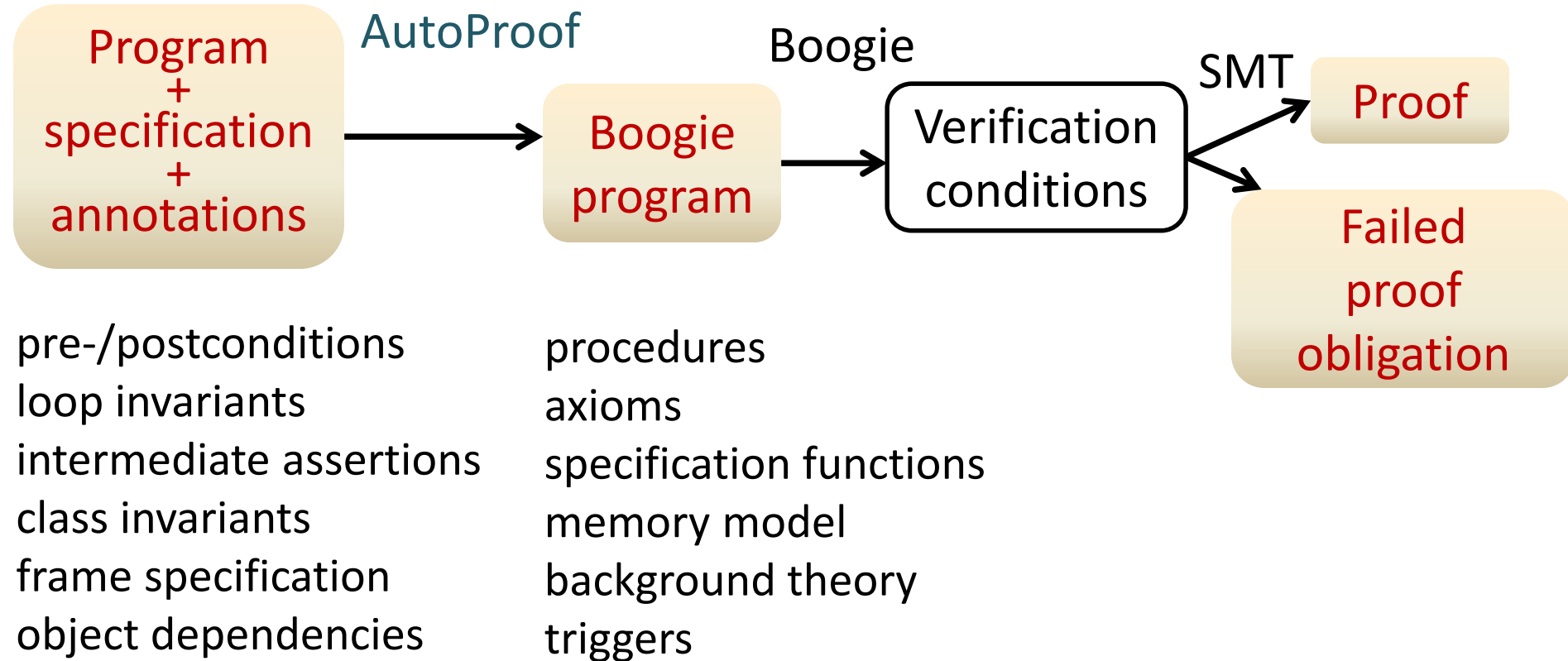
4. Correct/Revise

Sound program verifiers compared

more automation



How AutoProof works

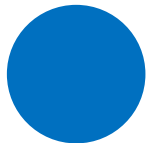


Reasoning with class invariants

Class invariants are a natural way to reason about object-oriented programs:

invariant = **consistency** of objects

ACCOUNT



```
invariant  
  balance >= 0
```

Demo: AutoProof warmup

AutoProof verifies a basic version of the bank
ACCOUNT class

deposit (amount: INTEGER)

withdraw (amount: INTEGER)

Follow this demo at:

<http://comcom.csail.mit.edu/e4pubs/#demo-key>

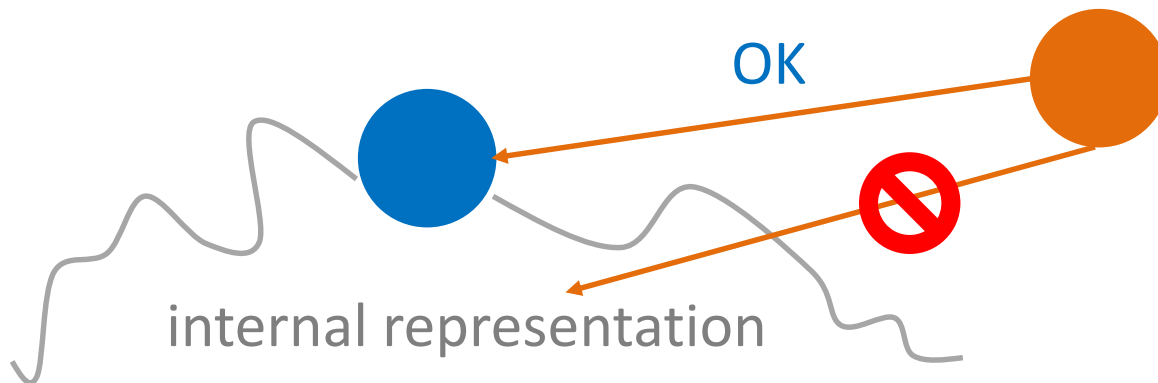
(Tab **account_warmup.e**)

Stability of invariant reasoning

Invariant-based reasoning should ensure **stability**:

stability = an operation can affect an object's **invariant** only if it modifies the object **explicitly**

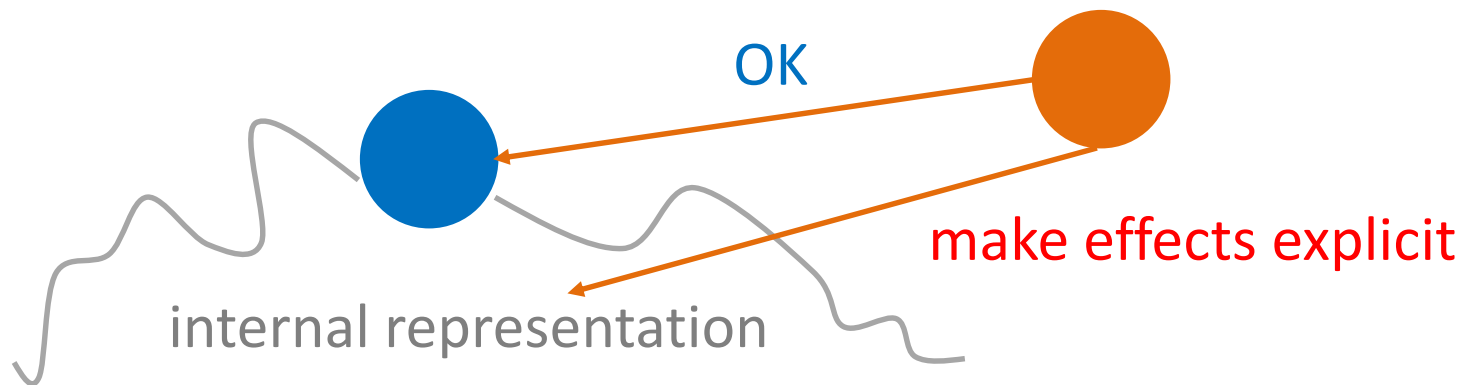
With stability, no one can invalidate an object **behind its back!**



Stability and encapsulation

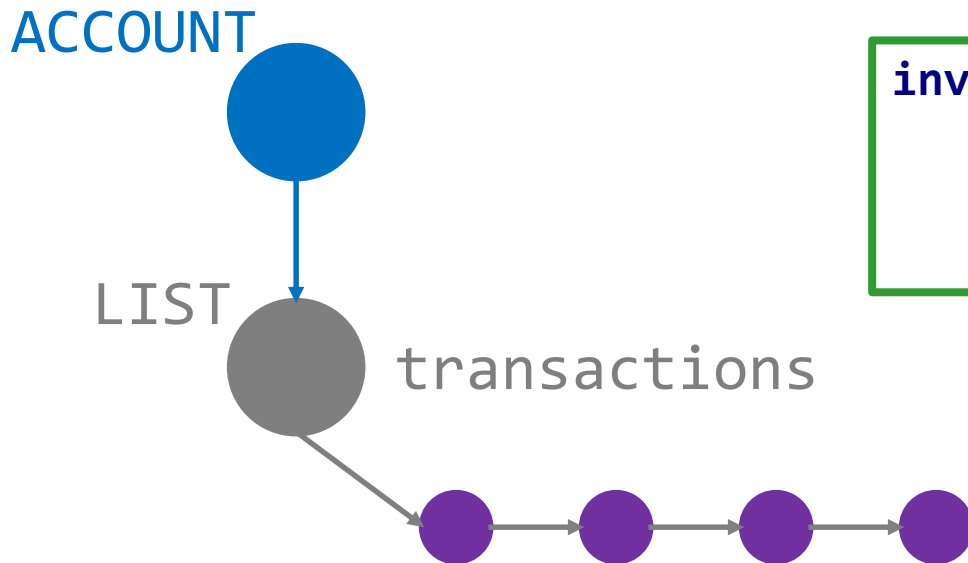
Invariant-based reasoning with stability:

- enforces **encapsulation**/information hiding
- simplifies client **reasoning**
- retains **flexibility**



Multi-object structures

Object-oriented programs involve **multiple objects** (duh!), whose consistency is often **mutually dependent**



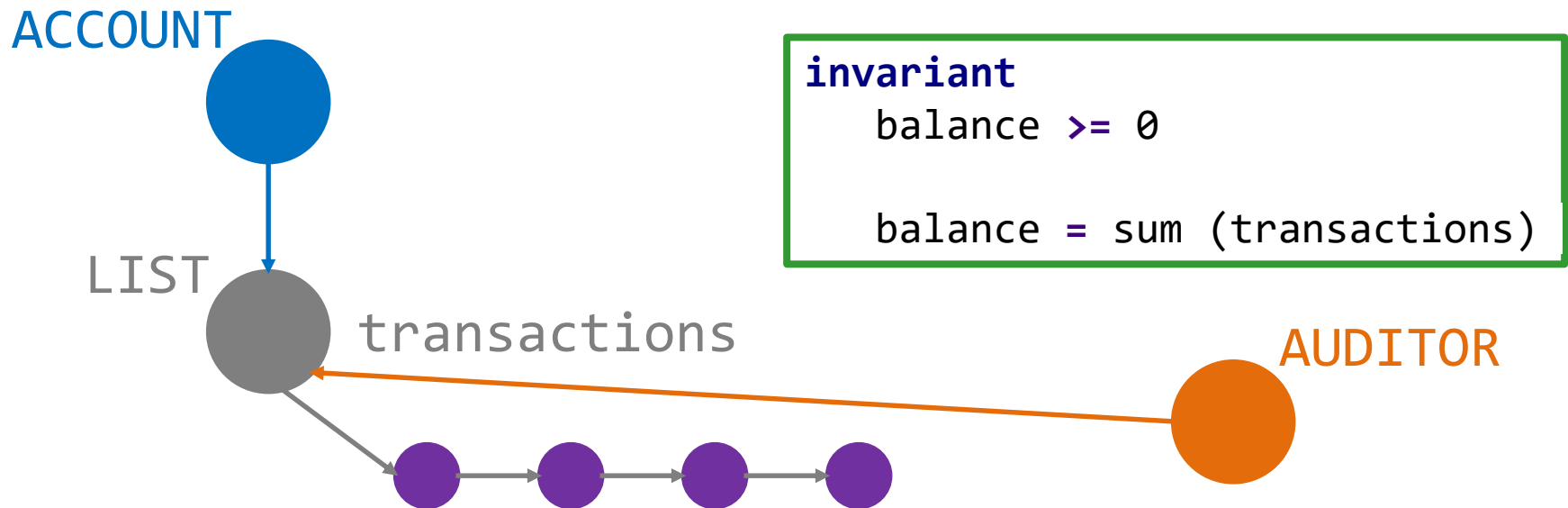
invariant

`balance >= 0`

`balance = sum (transactions)`

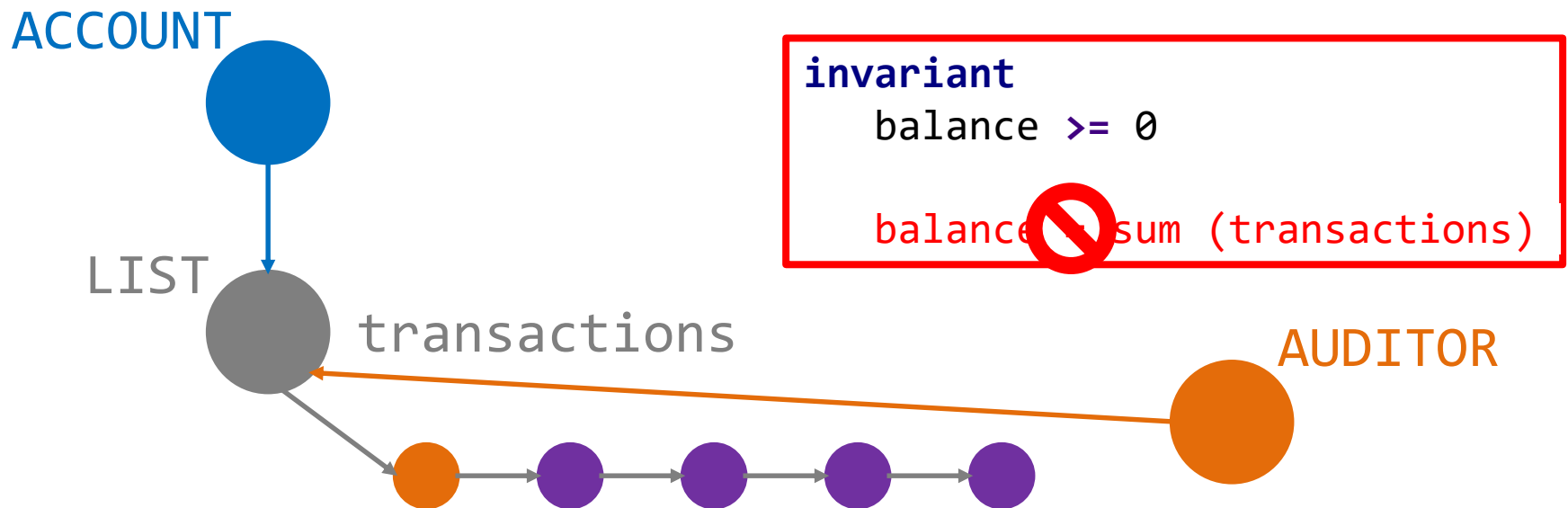
Consistency of multi-object structures

Mutually dependent object structures require extra care to enforce, and reason about, **consistency** (cmp. encapsulation)



Consistency of multi-object structures

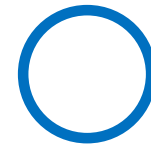
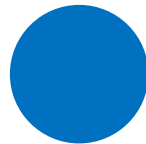
Mutually dependent object structures require extra care to enforce, and reason about, **consistency** (cmp. encapsulation)



Open and closed objects

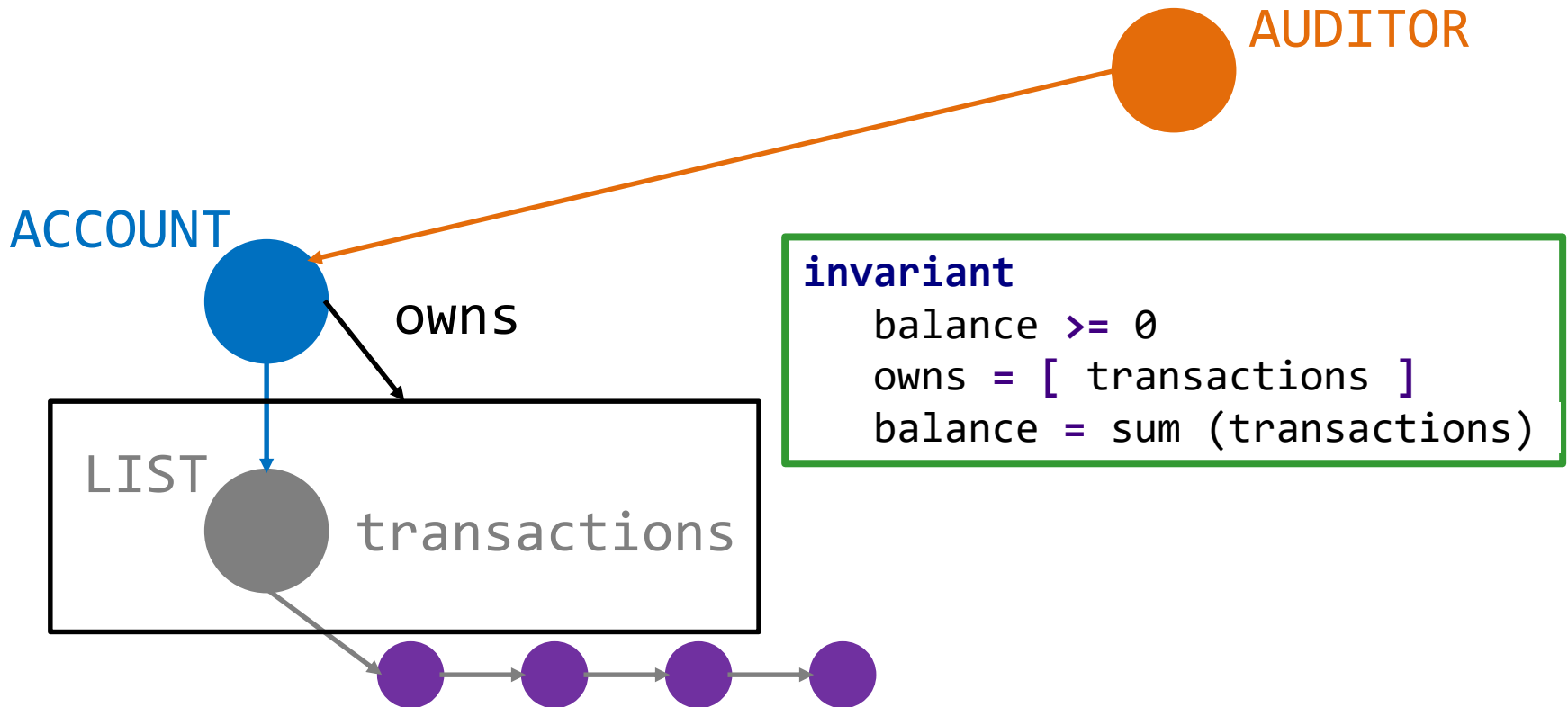
When (at which program points) must class invariants hold? To provide flexibility, objects in AutoProof can be **open** or **closed**

	CLOSED	OPEN
Object:	consistent	inconsistent
State:	stable	transient
Invariant:	holds	may not hold



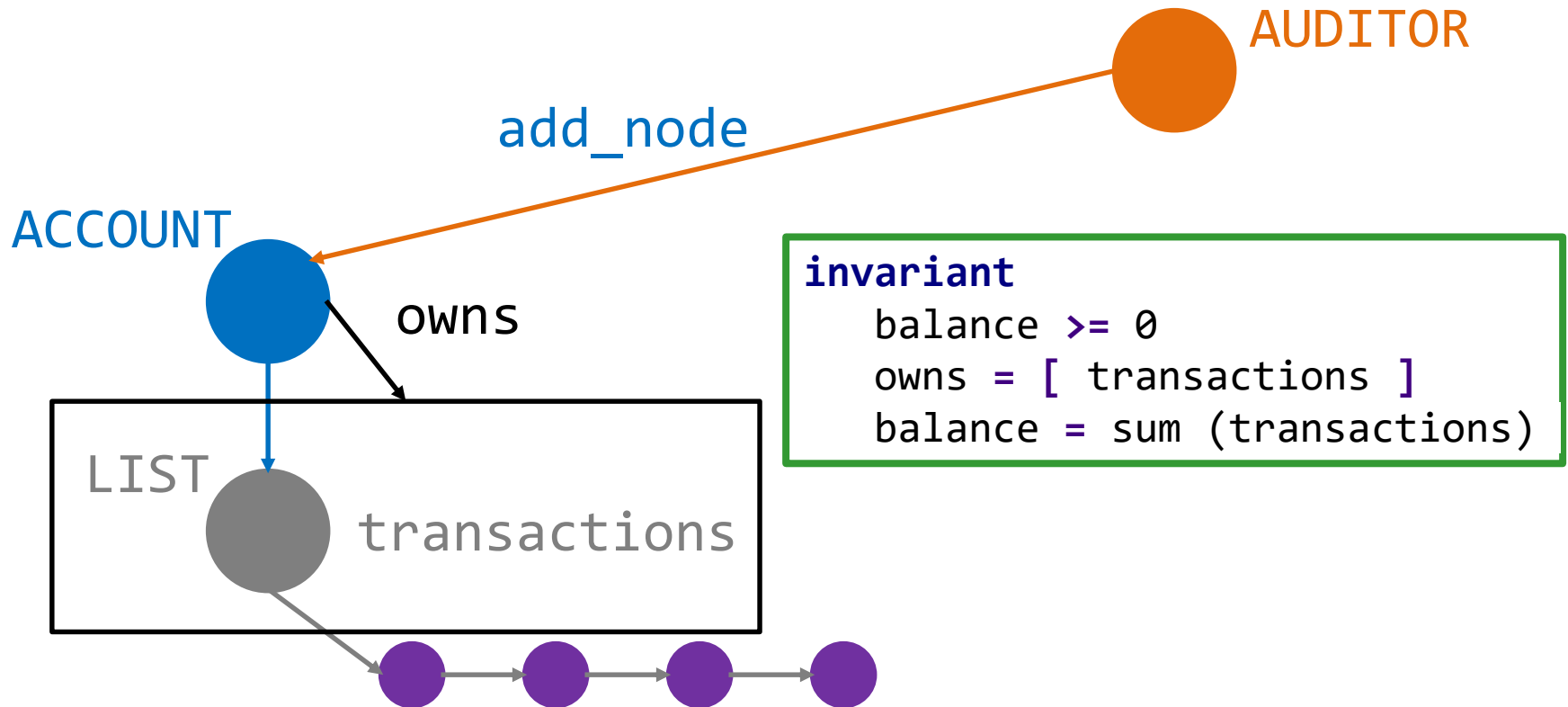
Ownership

For **hierarchical** object structures, AutoProof offers an **ownership** protocol



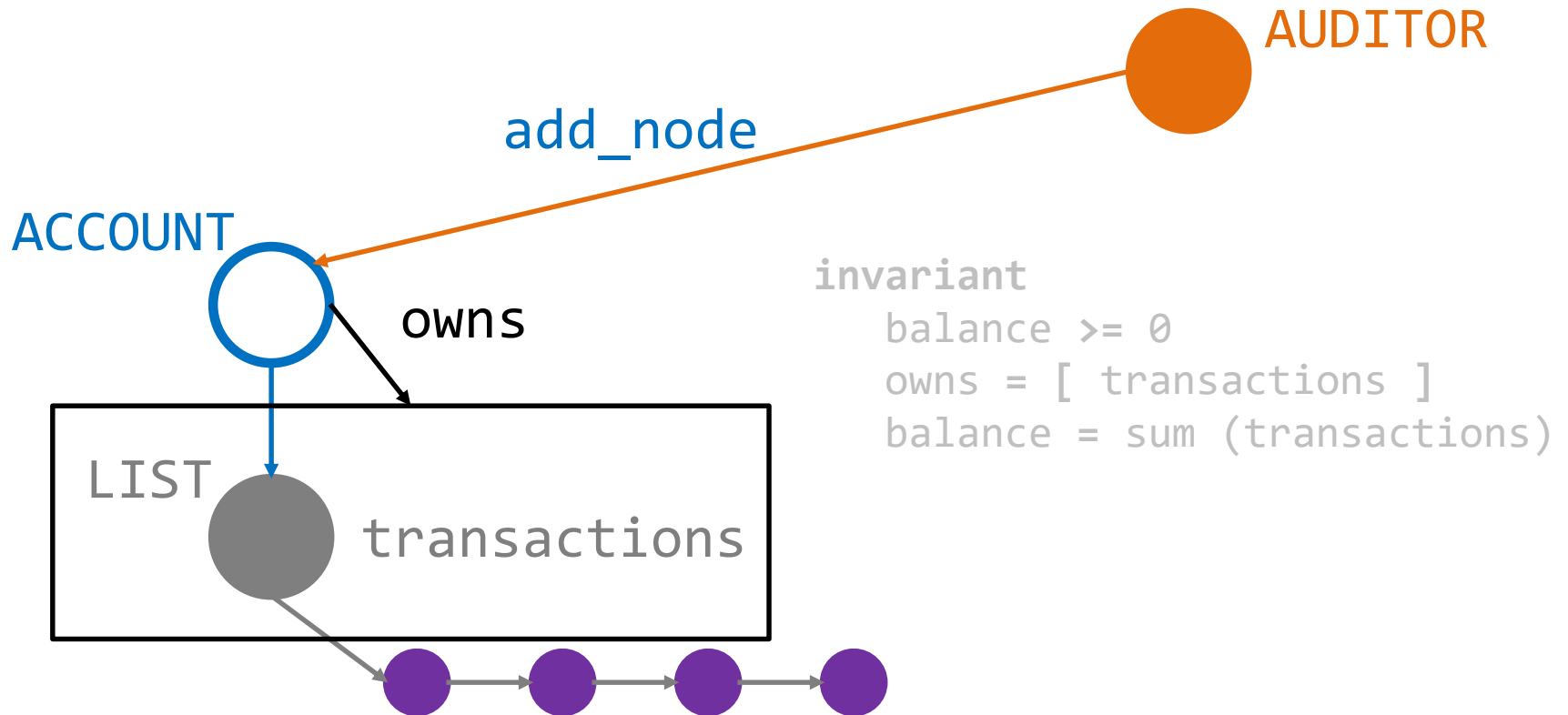
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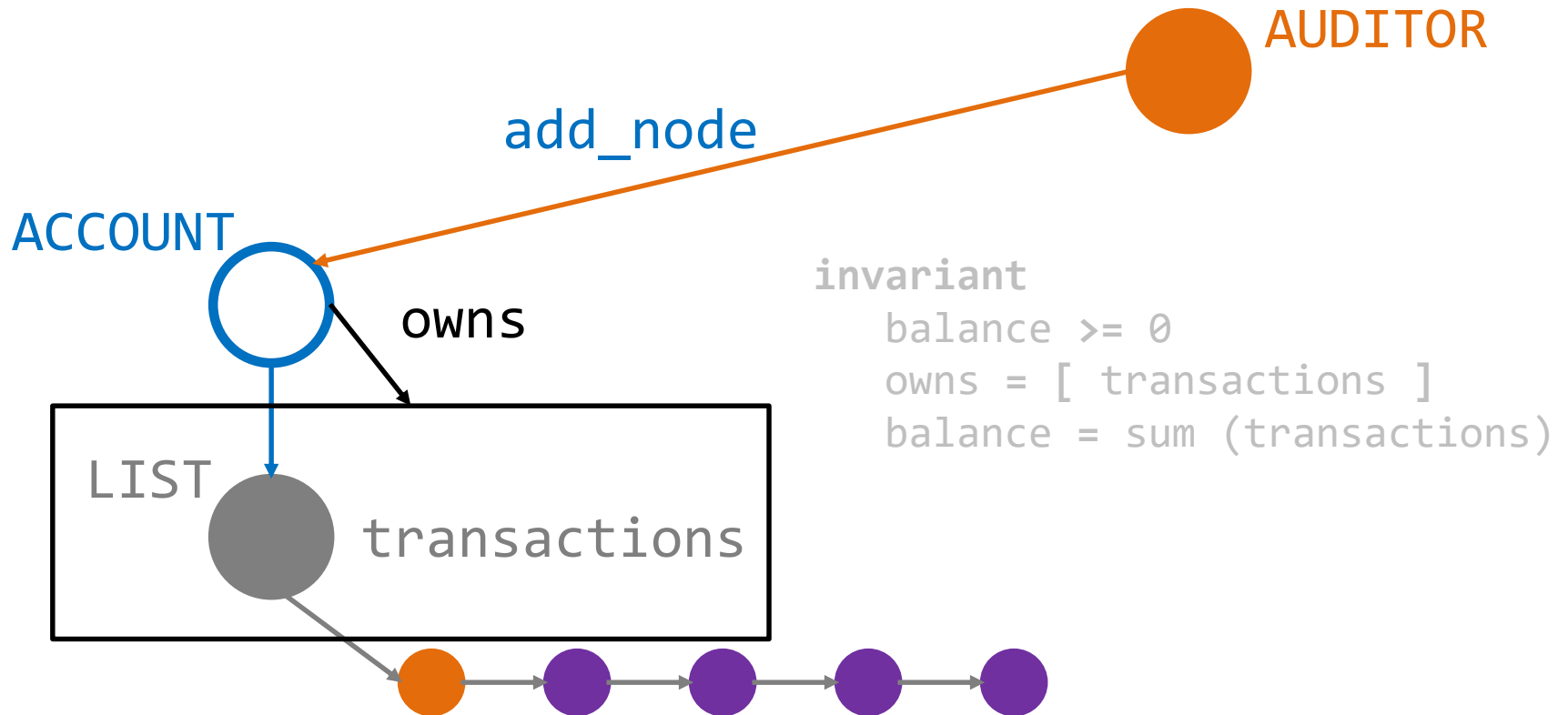
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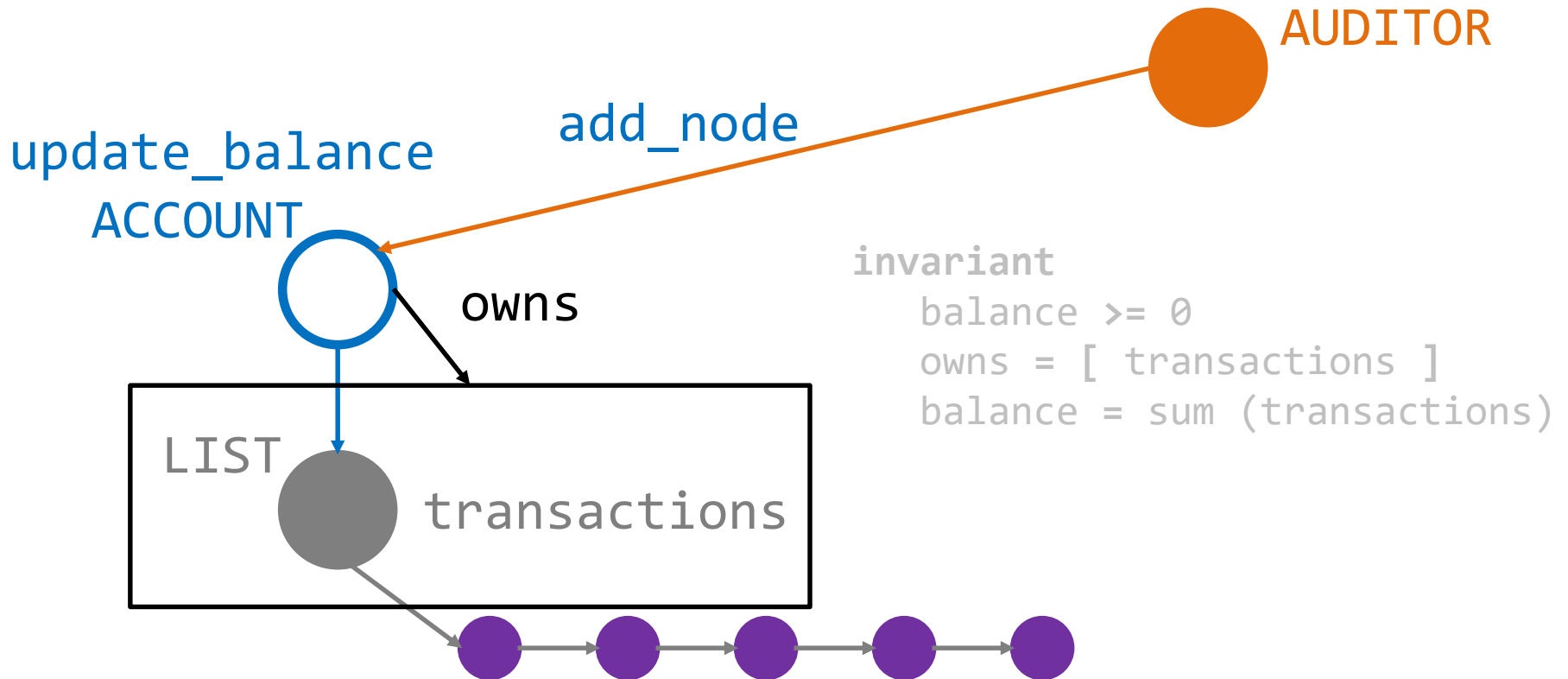
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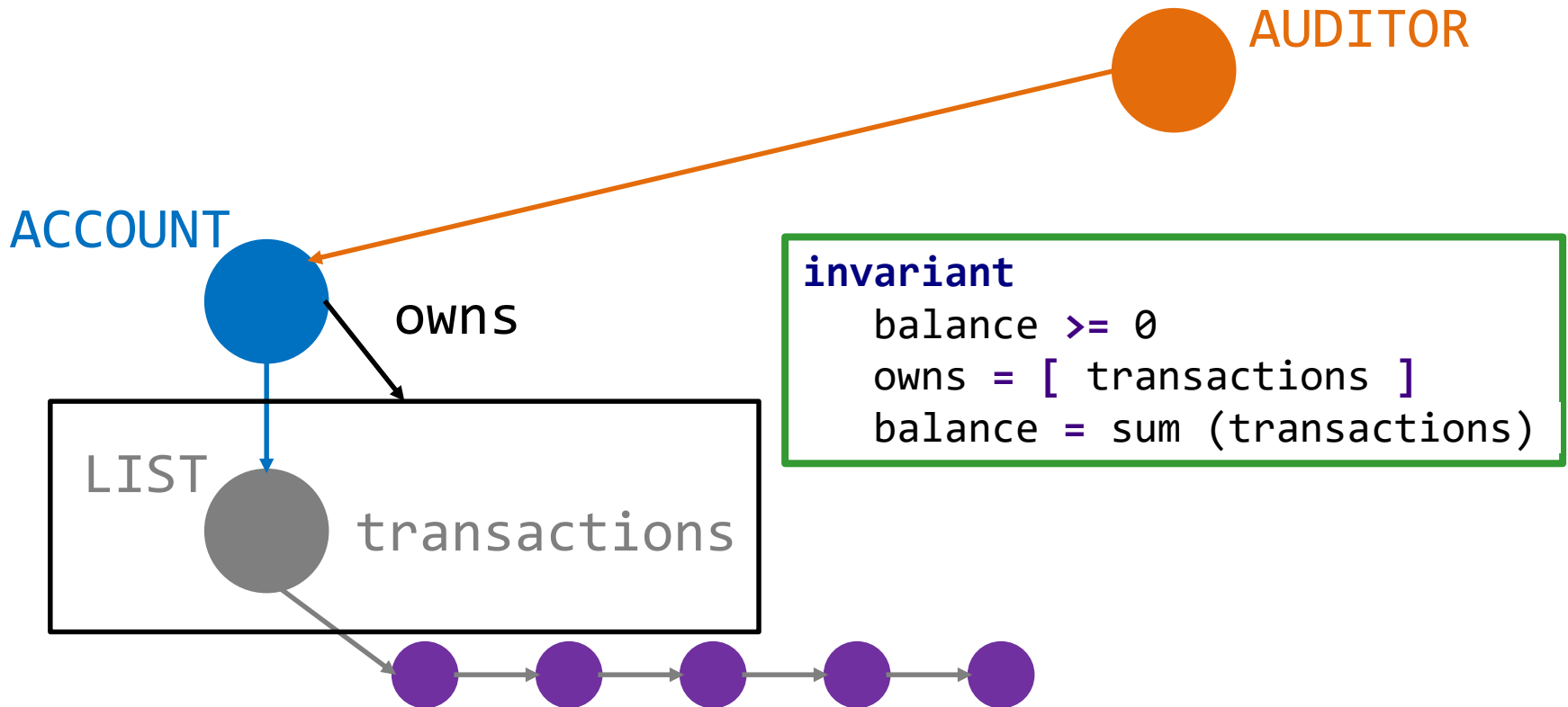
Ownership

For **hierarchical** object structures, AutoProof offers an **ownership** protocol



Ownership

For **hierarchical** object structures, AutoProof offers an **ownership** protocol



Demo: ownership in AutoProof

AutoProof verifies **deposit** and **withdraw** in **ACCOUNT** with an owned list of transactions

```
transactions: SIMPLE_LIST [INTEGER]
```

- History of transactions:
- positive integer = deposited amount
- negative integer = withdrawn amount
- latest transactions in back of list

Follow this demo at:

<http://comcom.csail.mit.edu/e4pubs/#demo-key>

(Tab **account_ownership.e**)

Wrapping and unwrapping

Combination on ownership and invariants:

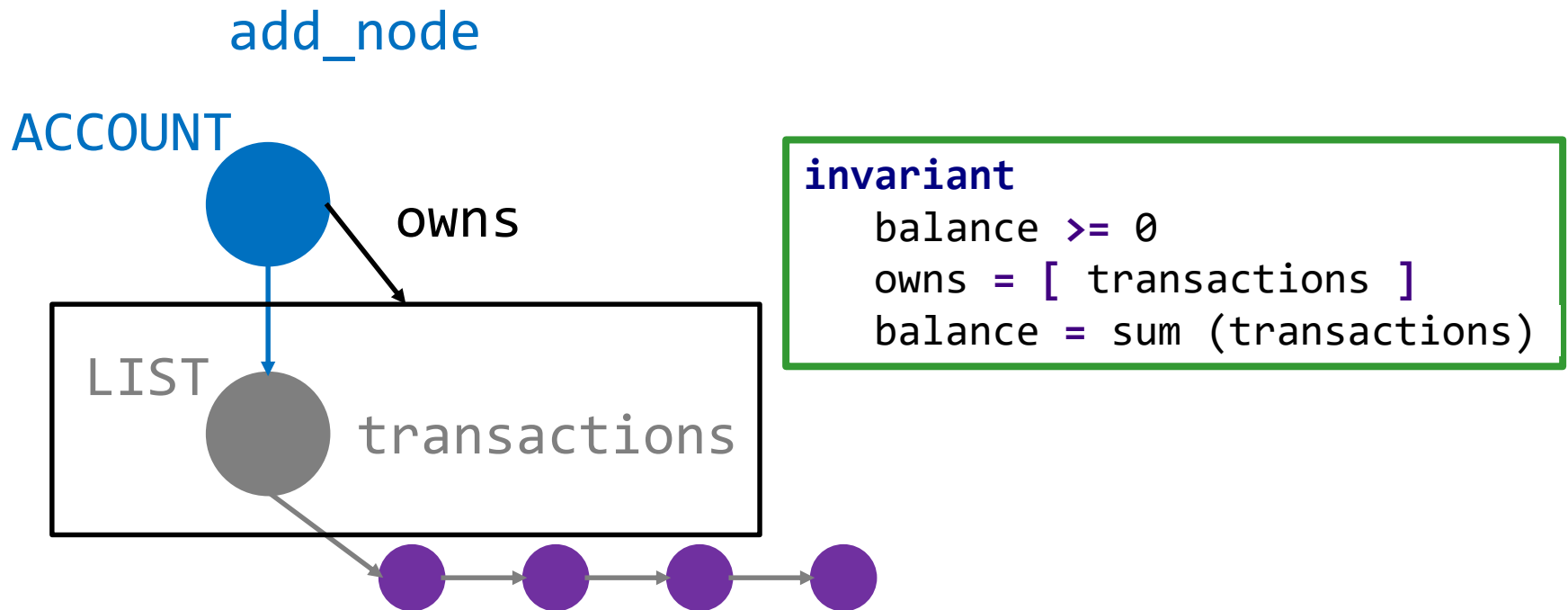
Wrapped object = closed and not owned

Unwrapped object = open (or owned)

	WRAPPED	UNWRAPPED
Invariant:	holds	may not hold
Clients:	any object	within owner
Modifications:	modify after unwrapping	wrap after modifying

Wrapping and unwrapping

Typical **modification pattern**:
unwrap, **modify**, **wrap** (check consistency)

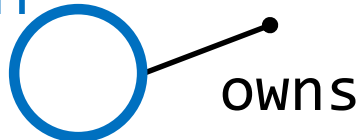


Wrapping and unwrapping

Typical **modification pattern**:
unwrap, **modify**, **wrap** (check consistency)

`add_node`: **unwrap**

ACCOUNT



`invariant`

`balance >= 0`

`owns = [transactions]`

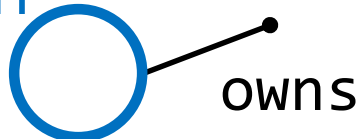
`balance = sum (transactions)`

Wrapping and unwrapping

Typical **modification pattern**:
unwrap, **modify**, **wrap** (check consistency)

`add_node`: **unwrap**; **modify**

ACCOUNT



`invariant`

`balance >= 0`

`owns = [transactions]`

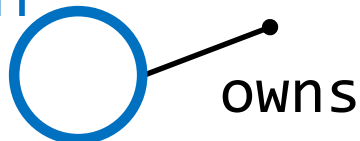
`balance = sum (transactions)`

Wrapping and unwrapping

Typical **modification pattern**:
unwrap, **modify**, **wrap** (check consistency)

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ACCOUNT



invariant

`balance >= 0`

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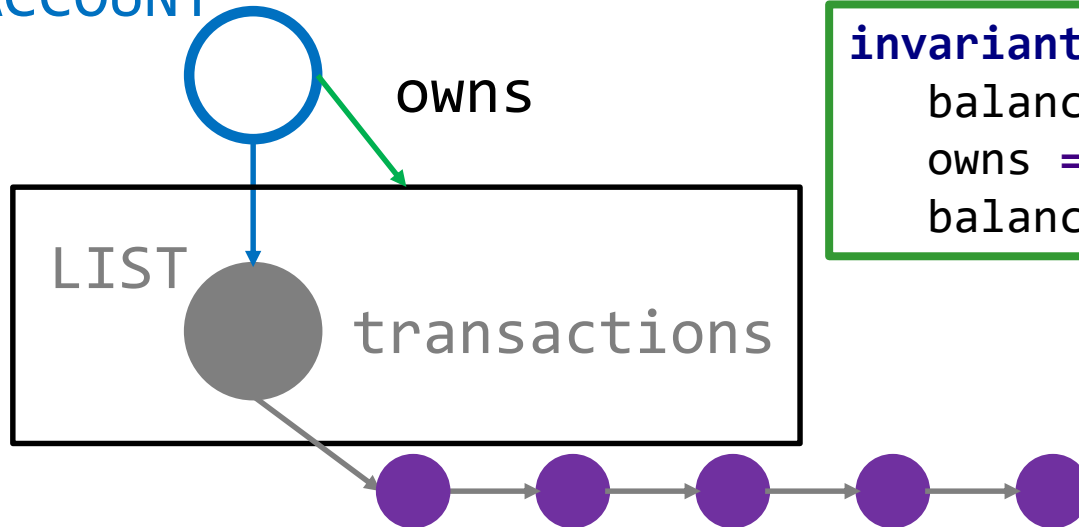
`balance = sum (transactions)`

Wrapping and unwrapping

Typical **modification pattern**:
unwrap, **modify**, **wrap** (check consistency)

`add_node`: **unwrap**; **modify**; **wrap** (check)

ACCOUNT



invariant

`balance >= 0`

`owns = [transactions]`

`balance = sum (transactions)`

Demo: ownership preserves stability

Ownership achieves stability when leaking references to the internal **transactions** list in **ACCOUNT**

```
leak_transactions: SIMPLE_LIST [INTEGER]
```

```
leak_transactions_unsafe: SIMPLE_LIST [INTEGER]
```

Follow this demo at:

<http://comcom.csail.mit.edu/e4pubs/#demo-key>

(Tabs **account_ownership.e** and **auditor.e**)

Semantic collaboration

For **collaborative** object structures, AutoProof offers a novel protocol: **semantic collaboration**

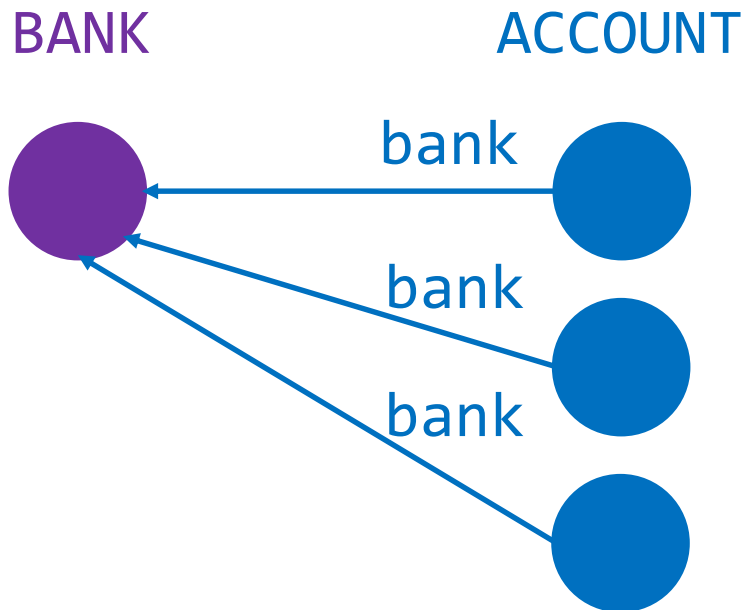


invariant

`interest_rate = bank.rate`

Semantic collaboration

For **collaborative** object structures, AutoProof offers a novel protocol: **semantic collaboration**

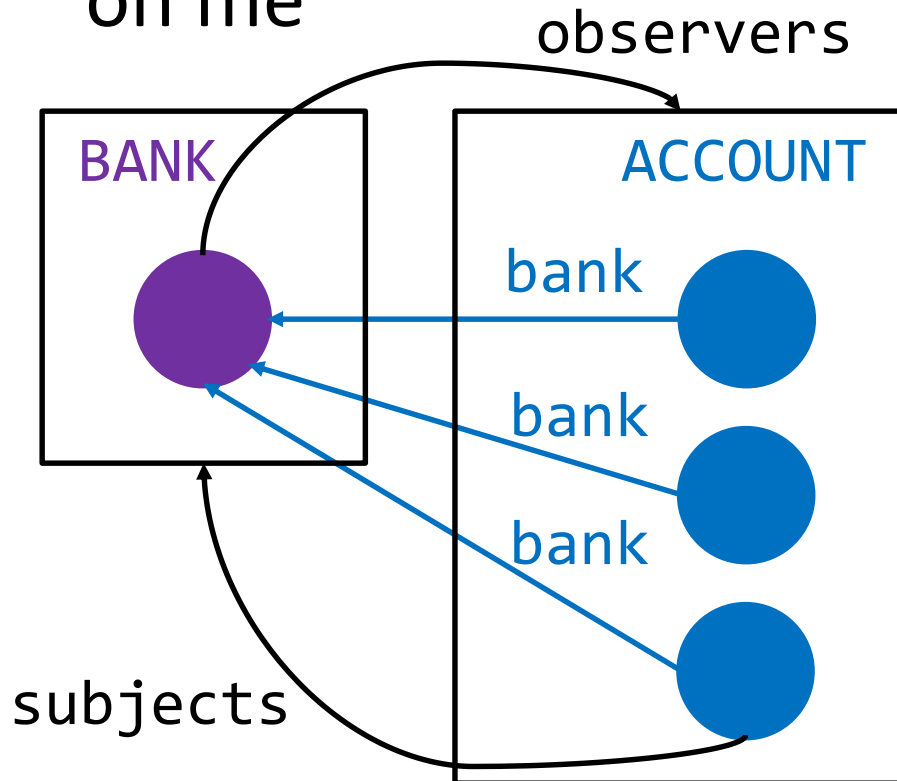


invariant

`interest_rate = bank.rate`

Semantic collaboration

- **Subjects** = objects my consistency depends on
- **Observers** = objects whose consistency depends on me

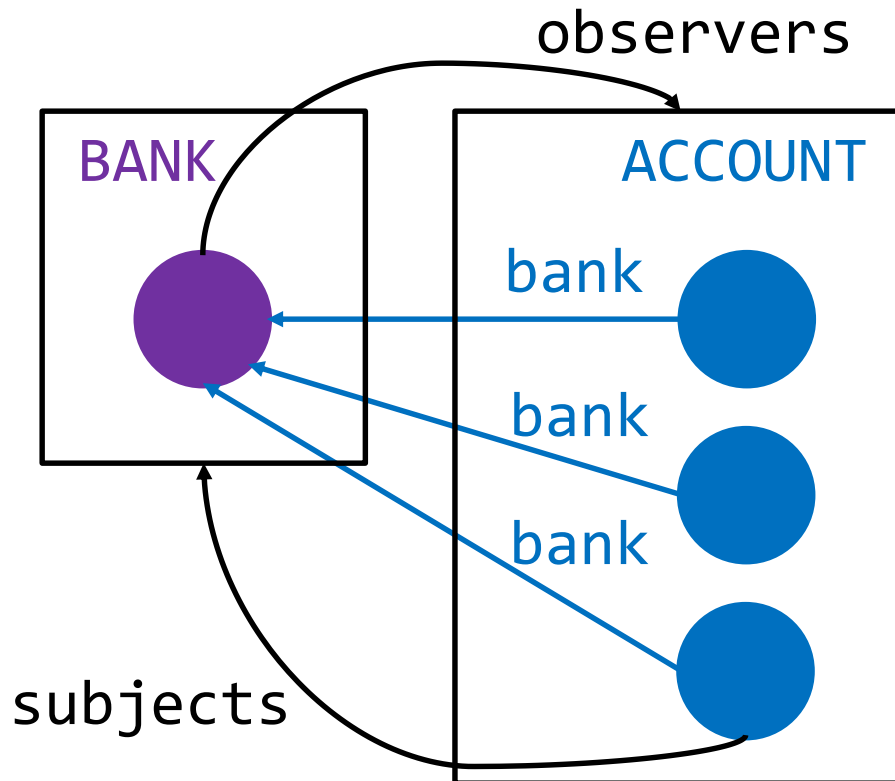


```
invariant  
subjects = [ bank ]  
Current in bank.observers  
  -- Implicit in AutoProof  
  
interest_rate = bank.rate
```

Semantic collaboration

The bank **changes the rate** (and notifies accounts)

update



invariant

subjects = [bank]

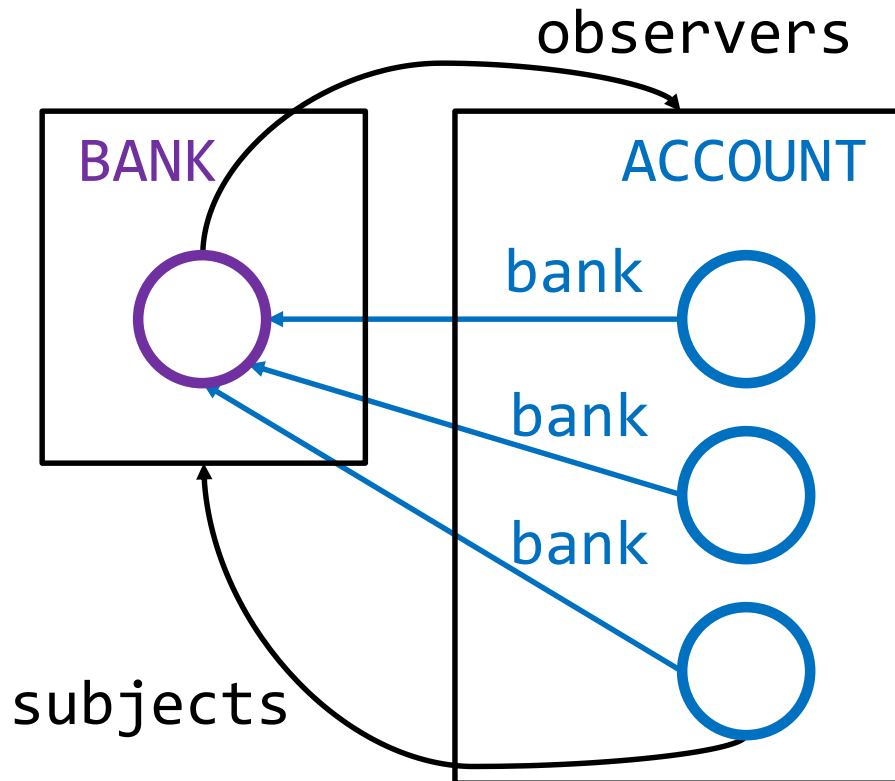
Current in bank.observers

interest_rate = bank.rate

Semantic collaboration

The bank **changes the rate** (and notifies accounts)

update: **open bank, observers**



invariant

subjects = [bank]

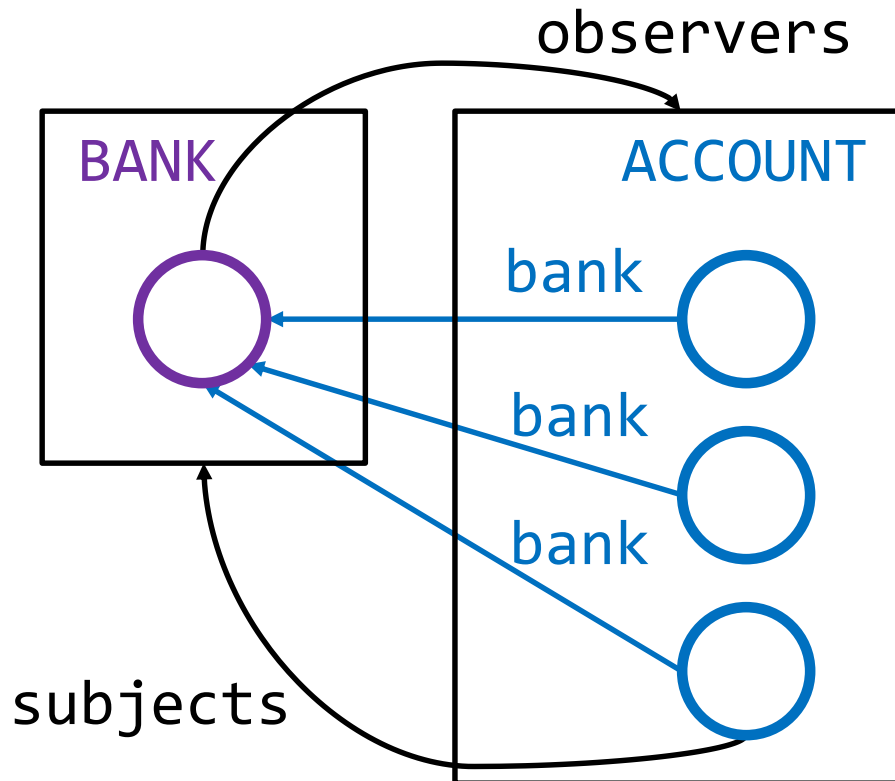
Current in bank.observers

interest_rate = bank.rate

Semantic collaboration

The bank **changes the rate** (and notifies accounts)

update: **set rate**



invariant

subjects = [bank]

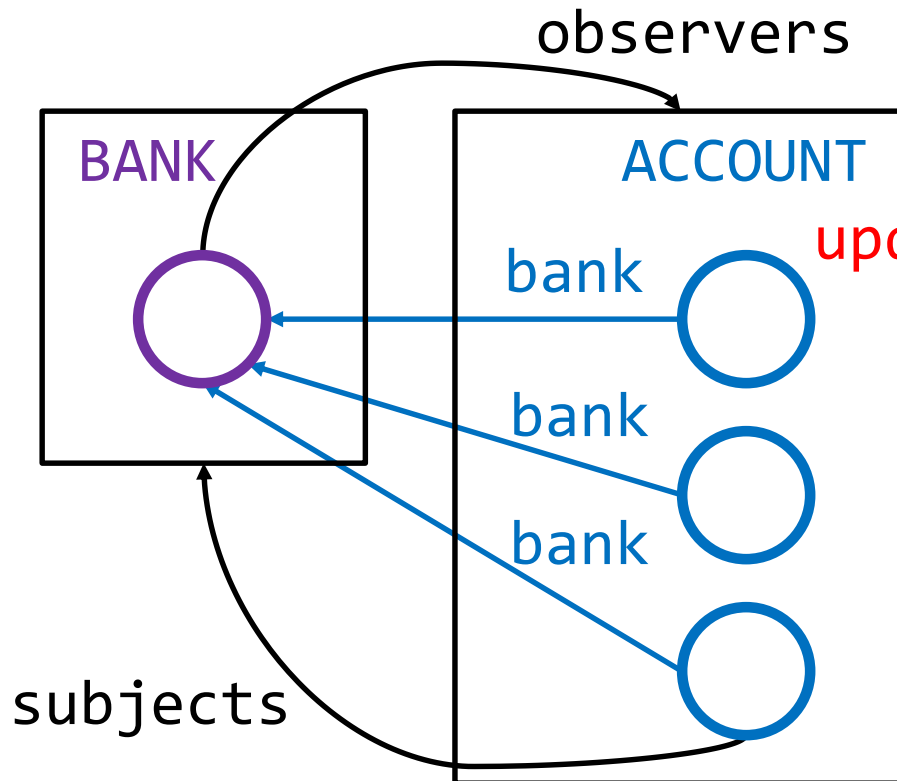
Current in bank.observers

interest_rate = **bank.rate**

Semantic collaboration

The bank **changes the rate** (and notifies accounts)

update: **set rate, notify all accounts**



invariant

subjects = [bank]

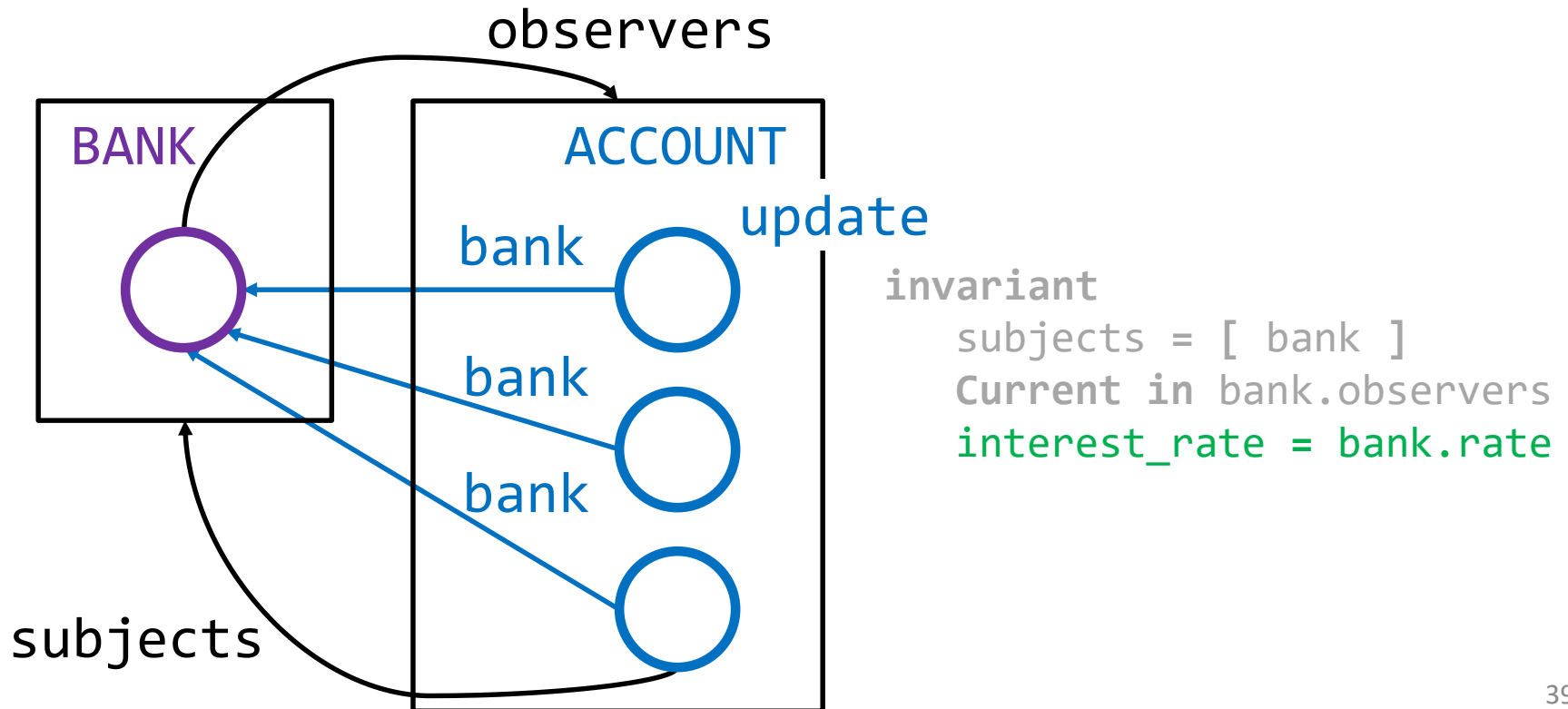
Current in bank.observers

interest_rate = **bank.rate**

Semantic collaboration

The bank **changes the rate** (and notifies accounts)

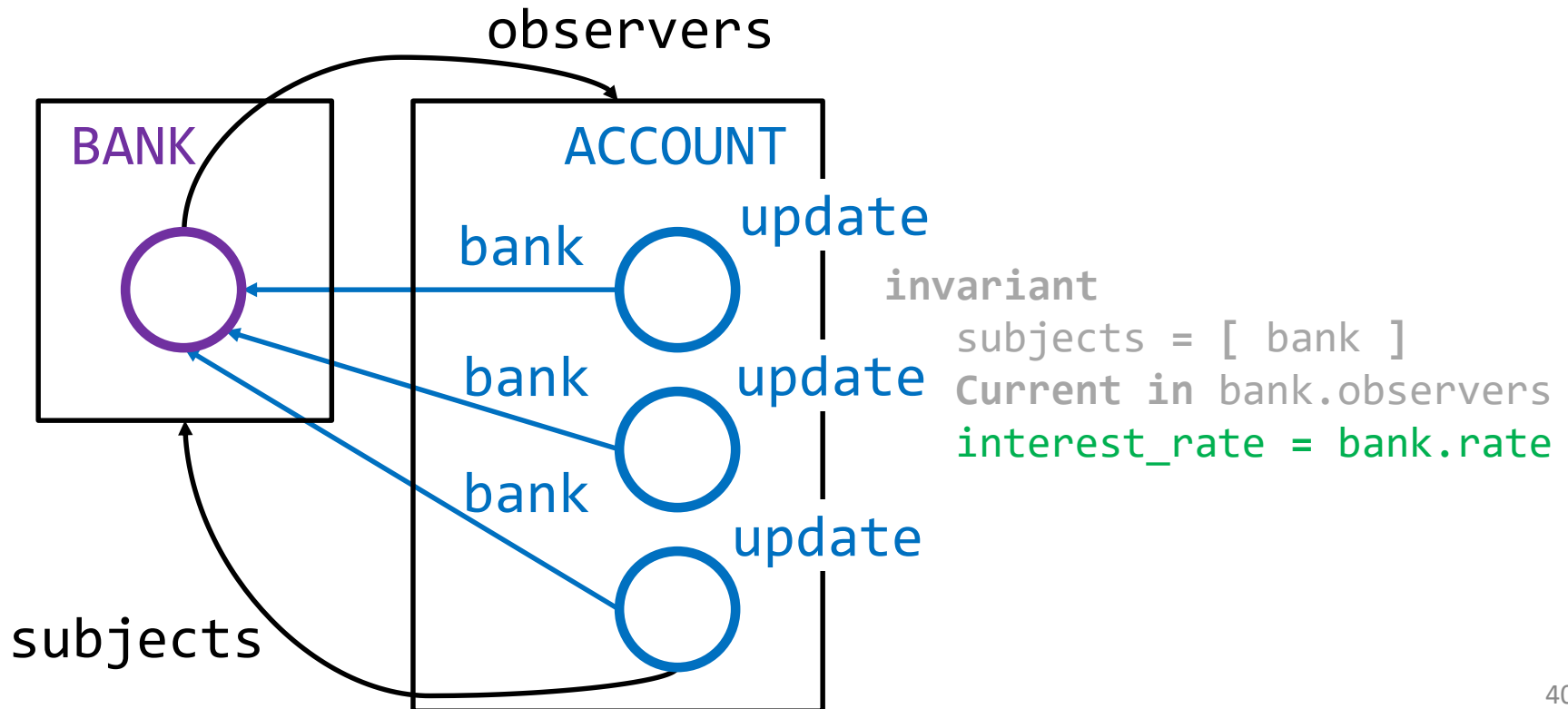
update: **set rate, notify all accounts**



Semantic collaboration

The bank **changes the rate** (and notifies accounts)

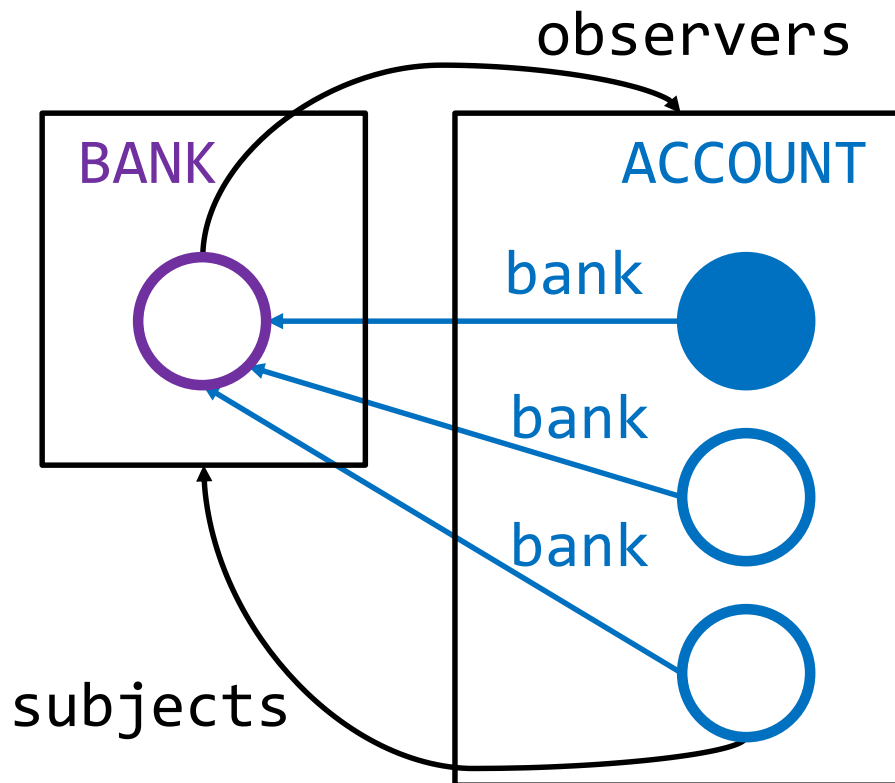
update: **set rate, notify all accounts**



Semantic collaboration

The bank **changes the rate** (and notifies accounts)

update: **wrap bank, all observers (check)**



invariant

subjects = [bank]

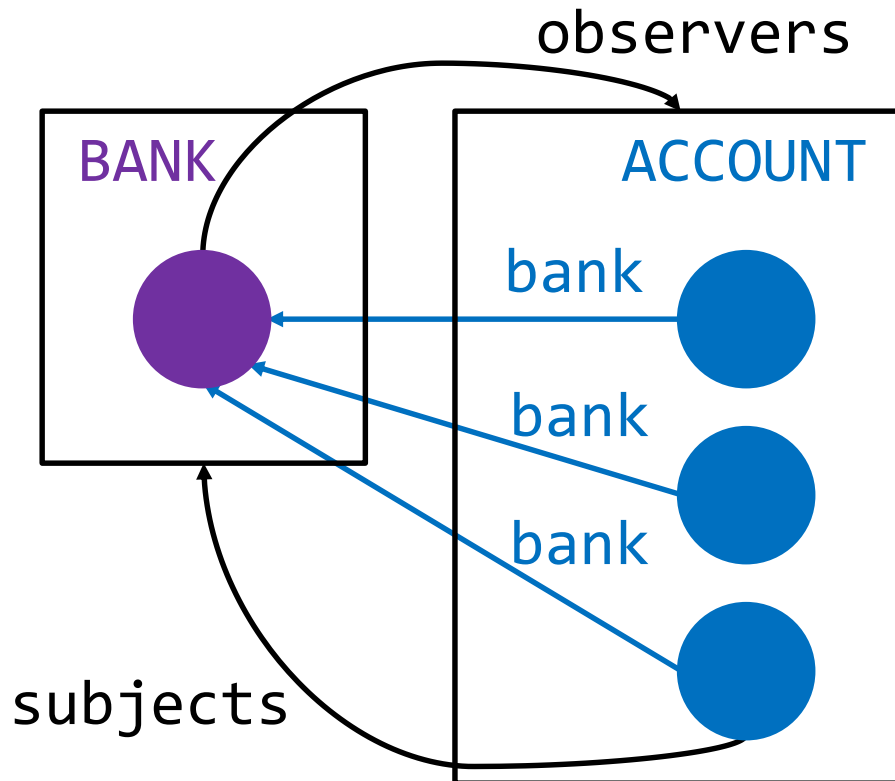
Current in bank.observers

interest_rate = bank.rate

Semantic collaboration

The bank **changes the rate** (and notifies accounts)

update: open, modify, wrap (check)



invariant

```
subjects = [ bank ]
```

```
Current in bank.observers
```

```
interest_rate = bank.rate
```

Demo: collaboration in AutoProof

AutoProof verifies `update_rate` in `ACCOUNT` and `change_master_rate` in `BANK` based on semantic collaboration features

```
subjects_definition: subjects = [ bank ]
```

```
consistent_rate: interest_rate = bank.master_rate
```

Follow this demo at:

<http://comcom.csail.mit.edu/e4pubs/#demo-key>

(Tabs `account_collaboration.e` and `bank.e`)

Wrapping and unwrapping

In hierarchical structures there is one typical modification pattern:

unwrap, modify, wrap (check consistency)

In collaborative structures, there is more flexibility:

- **unwrap, modify, wrap**
- **unwrap, modify, leave open** (invalidate)
- **share** responsibility for **restoring consistency** between subjects and observers

Data structures

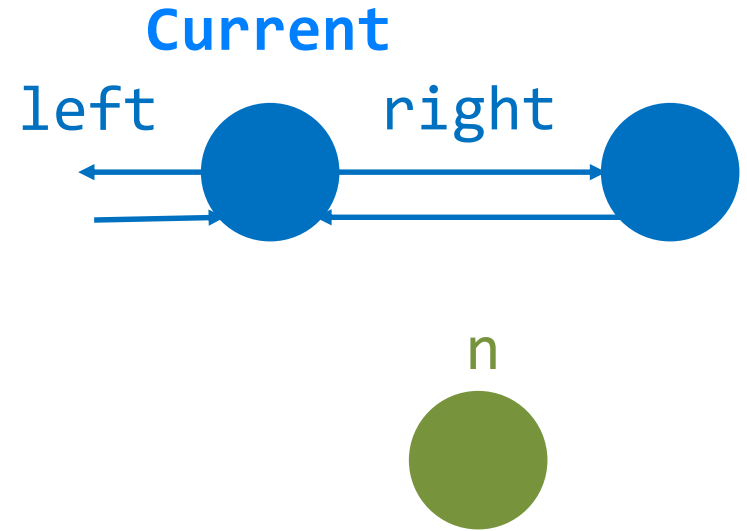
The features of semantic collaboration work well to reason about **data structure implementations**.

Data structures: doubly-linked list

As an example, let's outline **node insertion** in a **doubly-linked list**:

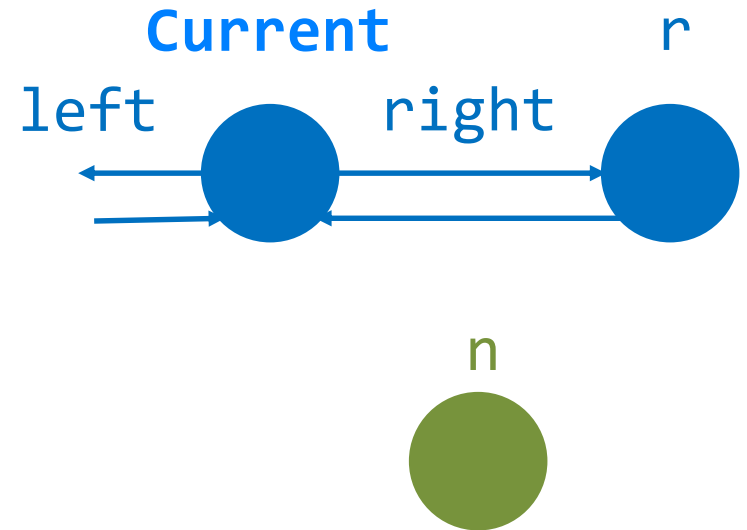
- A **singly** linked list is **hierarchical**: the head controls access to the whole list.
- A (circular) **doubly**-linked list is **collaborative**: every node depends on its neighbors, and they depend on it

Insert node **n** to right of **Current**



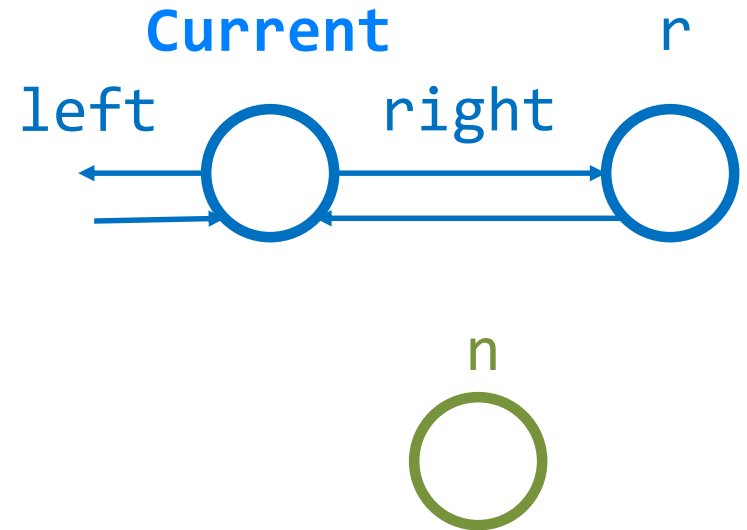
Insert node **n** to right of **Current**

```
var r := right
```



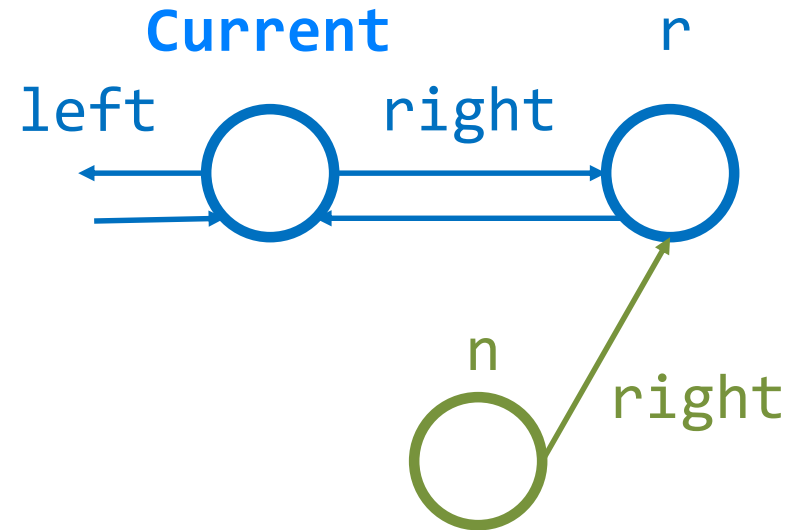
Insert node **n** to right of **Current**

```
var r := right  
unwrap Current, r, n
```



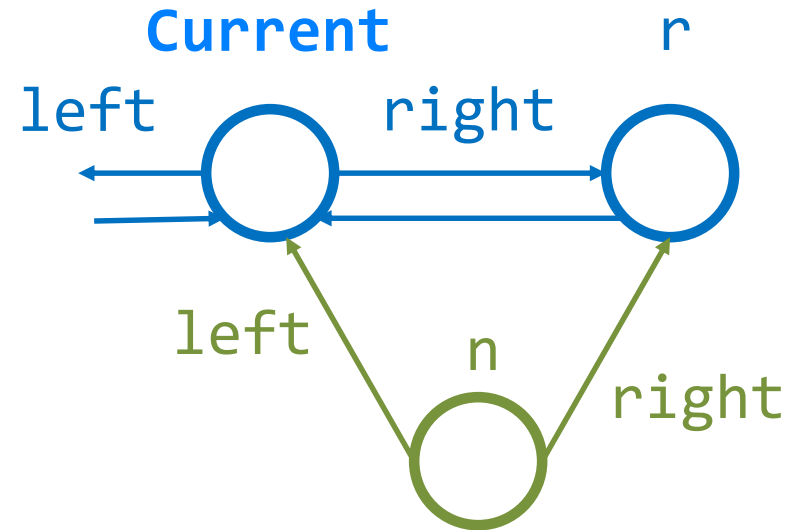
Insert node **n** to right of **Current**

```
var r := right  
unwrap Current, r, n  
n.right := r
```



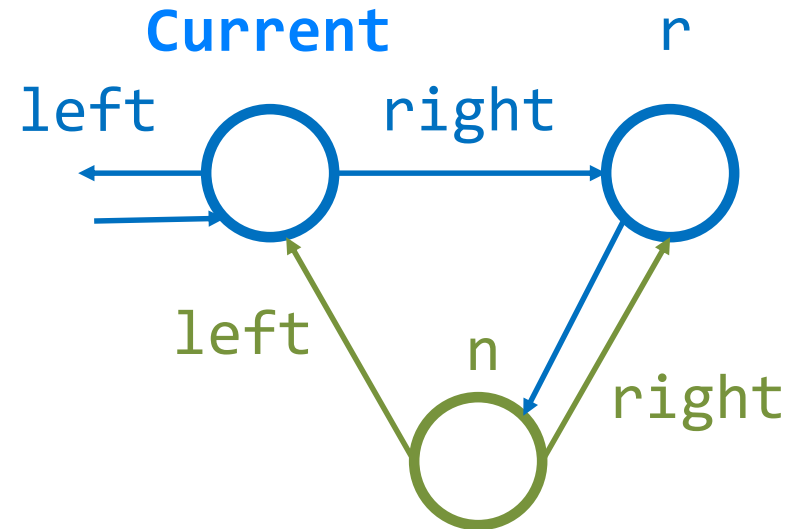
Insert node **n** to right of **Current**

```
var r := right  
unwrap Current, r, n  
n.right := r  
n.left := Current
```



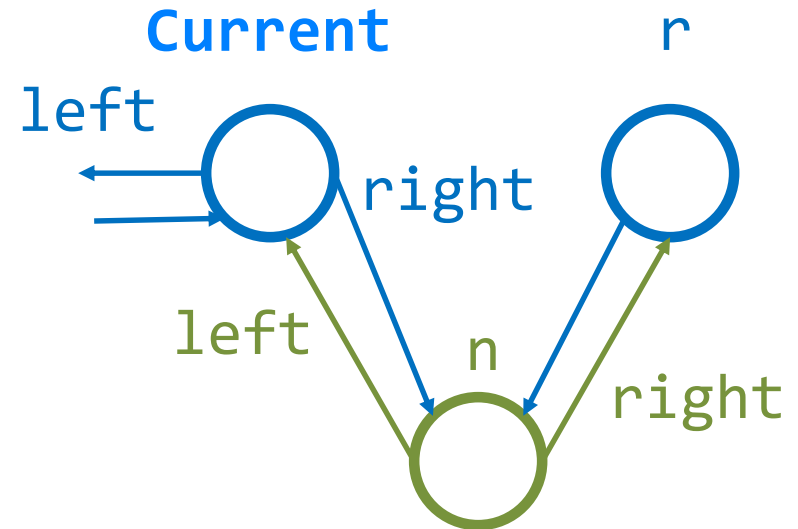
Insert node **n** to right of **Current**

```
var r := right
unwrap Current, r, n
n.right := r
n.left := Current
r.left := n
```



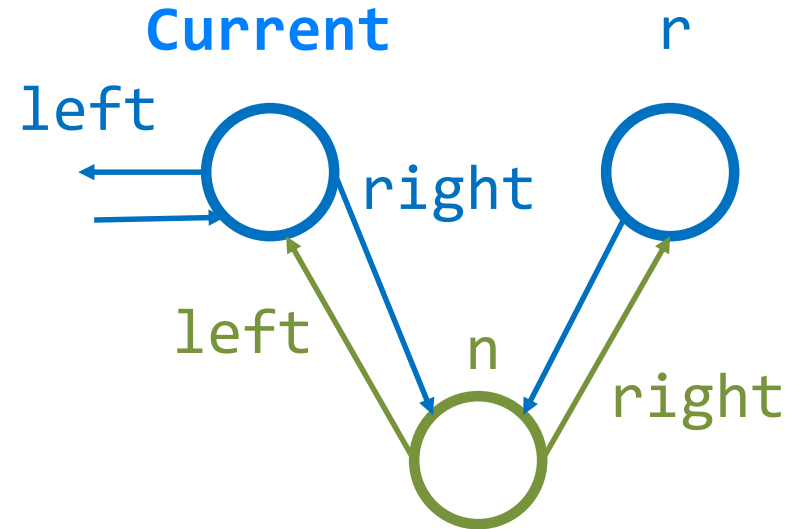
Insert node **n** to right of **Current**

```
var r := right
unwrap Current, r, n
n.right := r
n.left := Current
r.left := n
right := n
```



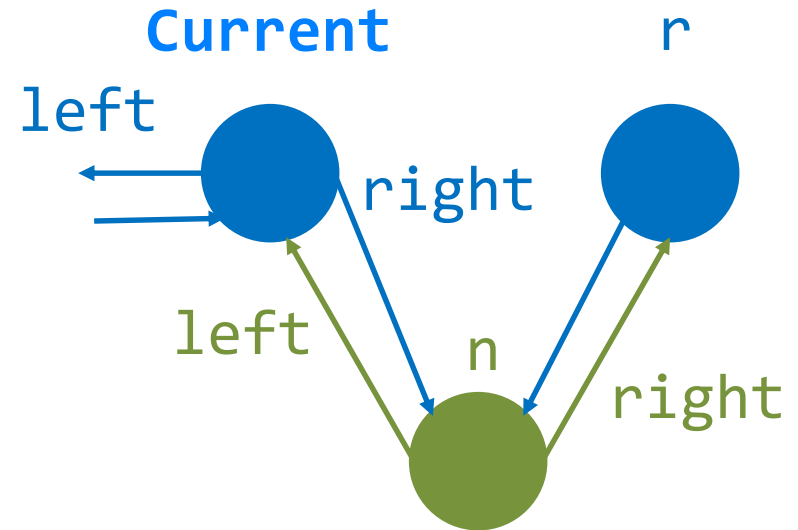
Insert node **n** to right of **Current**

```
var r := right
unwrap Current, r, n
n.right := r
n.left := Current
r.left := n
right := n
n.subjects, n.observers := [r, Current]
subjects, observers := [left, n]
r.subjects, r.observers := [n, r.right]
```



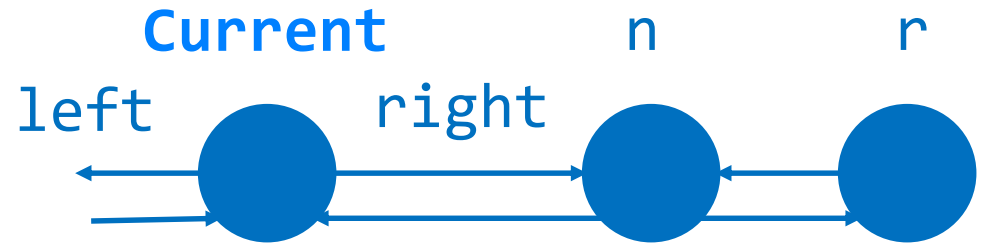
Insert node **n** to right of **Current**

```
var r := right
unwrap Current, r, n
n.right := r
n.left := Current
r.left := n
right := n
n.subjects, n.observers := [r, Current]
subjects, observers := [left, n]
r.subjects, r.observers := [n, r.right]
wrap Current, r, n
```



Insert node **n** to right of **Current**

```
var r := right
unwrap Current, r, n
n.right := r
n.left := Current
r.left := n
right := n
n.subjects, n.observers := [r, Current]
subjects, observers := [left, n]
r.subjects, r.observers := [n, r.right]
wrap Current, r, n
```



Attribute update guards

Who's responsible for checking that an update to an attribute satisfies the invariant?

a: A guard: $g(a', o)$

- every observer **o** of **Current** that satisfies the guard **g** is responsible for checking that updating **Current**'s attribute **a** to the value **a'** does not violate the invariant of **o**

Update guards in doubly-linked list

`right: NODE guard: 0 /= right`

When changing the value of attribute `right`:

- the `left` node checks that its invariant is **not violated** by changing `right` in the current node
 - the `left` node's invariant does not depend on `Current.right` (it remains wrapped)
- the current node checks that `right`'s invariant is **not violated** by changing `Current.right`
 - the `right` node is open when changing `Current.right` (invariant vacuously holds)
 - actual check performed when wrapping `right`

Demo: doubly-linked list

AutoProof verifies class `NODE`, representing the generic node of a doubly-linked list

```
insert_right (n: NODE)
```

```
-- Insert n to the right of Current.
```

Follow this demo at:

<http://comcom.csail.mit.edu/e4pubs/#demo-key>

(Tab `node.e`)

Proving realistic implementations

Semantic collaboration is part of a **verification framework** with features suitable to reason about realistic implementations:

- **model-based** specifications
 - completeness
- extensible **specification types** and MML library
- (abstract) **framing** with **inheritance**
- **modular** verification with **inheritance**
 - nonvariant, covariant methods
- finely-tuned **encoding** in AutoProof

AutoProof on realistic software

Verification benchmarks:

# programs	LOC	SPEC/CODE	Verification time
25	4400	Lines: 1.0 Tokens: 1.9	Total: 3.4 min Longest method: 12 sec Average method: < 1 sec

EiffelBase2 – a realistic container library:



# classes	LOC	SPEC/CODE	Verification time
46	8400	Lines: 1.4 Tokens: 2.7	Total: 7.2 min Longest method: 12 sec Average method: < 1 sec

Class-invariant based reasoning with **semantic** collaboration

